# COMS30035, Machine learning: Classification and Neural Networks

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#### **Textbooks**

We will follow parts of the Chapter 4 and 5 of the Bishop book:

Bishop, C. M., Pattern recognition and machine learning (2006). Available for free here.

## Agenda

- Discriminant functions
- Logistic regression
- Perceptron
- Neural networks (multi-layer perceptron)
  - Architecture
  - The backpropagation algorithm
  - Gradient descent

See: [Chapter 5, Bishop]

#### Classification

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- It is the classical example of supervised learning
- Goal: Classify input data into one of K classes
- Model: Discriminant function:
  - A function that takes an input vector x and assigns it to class  $C_k$ . For simplicity we will focus on K = 2 and will first study linear functions (see Bishop for the general cases).

- ► The simplest linear discriminant (LD) is  $y(x) = w_0 + w^T x$ 
  - where y is used to predicted class C<sub>k</sub>, x is the input vector (feature values)
  - $\triangleright$   $w_0$  is a scalar, which we call bias
  - $\blacktriangleright$   $w_T$  is our vector of parameters, which we call weights

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- For K = 2: An input vector x is assigned to class  $C_1$  if  $y(x) \ge 0$  and to class  $C_2$  otherwise.

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- ▶ For K = 2: An input vector x is assigned to class  $C_1$  if  $y(x) \ge 0$  and to class  $C_2$  otherwise.
- Optimisation: least-squares (as for regression) <sup>1</sup>, where we want to minimise the cost or error function:

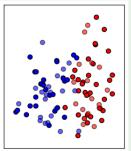
$$E = \frac{1}{2} \sum_{n=1}^{N} (\boldsymbol{w}^T \boldsymbol{x}_n + w_0 - t_n)^2$$
 where  $t_n$  are the targets/labels (e.g.  $t_1 = C_1$ ).

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# LD and linear separability

## Example

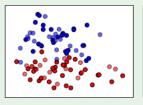
Linear separability is when two sets of points are separable by a line. We generated two sets of points using two Gaussians to illustrate this point, which can easily be fit by a LD. A *decision boundary* is the boundary that separates the two given classes, which our models will try to find.

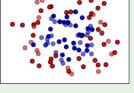


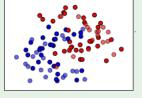
# Linear separability vs nonlinear separability

## Example

Which datasets **are** and **are not** linearly separable<sup>2</sup>?





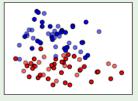


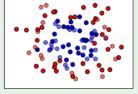
<sup>&</sup>lt;sup>2</sup>Example from Sklearn here.

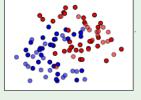
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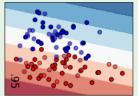
Only the first dataset is linearly separable!

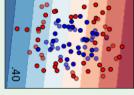
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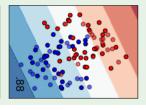
#### Linear discriminant

## Example

Using sklearn we fitted a LD to the data:



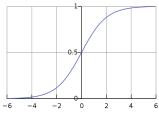




As expected, the LD model only does a good job in finding a good separation in the first dataset.

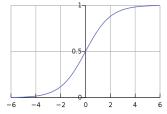
# Logistic regression

We use a logistic function to obtain the probability of class  $C_k$ :  $y(\mathbf{x}) = \sigma(\mathbf{w}^T \mathbf{x})$  where  $\sigma$  denotes the logistic sigmoid function (s-shaped), for example:



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- ▶ such that when  $y \rightarrow 0$  we choose class 1 and  $y \rightarrow 1$  class 2.
- Taking a probabilistic view:  $p(C_1|\mathbf{x}) = y(\mathbf{x})$ , and  $p(C_2|\mathbf{x}) = 1 p(C_1|\mathbf{x})$ .

#### Follow MLE recipe:

1. Define likelihood: For a data set  $\{x_n, t_n\}$ , where the targets  $t_n \in \{0, 1\}$ 

we have 
$$p(t|w) = \prod_{n=1}^{N} y_n^{t_n} (1 - y_n)^{1-t_n}$$
 where  $y_n = p(C_1|x_n)$ . <sup>3</sup>

<sup>&</sup>lt;sup>3</sup>The exponent selects the probability of the target class (i.e. if  $t_n = 1$  we get  $y_n$ ; if  $t_n = 0$  we get  $1 - y_n$ ).

<sup>&</sup>lt;sup>4</sup>Note that we used the logarithm product and power rule.

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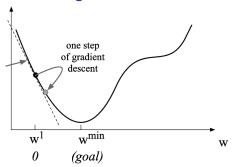
4. Now we can use Eq. above to directly update **w** using the data x.

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## MLE using Gradient Descent



- Start with random weight values
- We want to adjust each weight w to minimise negative log likelihood: move downhill to the minimum
- ► The derivative represents the slope:  $\frac{d \ln p(t|\mathbf{w})}{d\mathbf{w}} = \sum_{n=1}^{N} (y_n t_n) x_n$
- ▶ Increase or decrease w by a small amount in the downward direction

More details on calculating the derivative:

1. From here 
$$-\ln p(\mathbf{t}|\mathbf{w}) = -\sum_{n=1}^{N} \{t_n \ln y_n + (1-t_n) \ln (1-y_n)\}$$

<sup>&</sup>lt;sup>6</sup>We used the chain rule and  $d \ln(x) = 1/x$ . We also used the derivative of the sigmoid  $dy_n = y(1 - y_n)$ .

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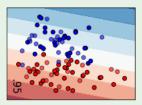
4. And in turn to 
$$\sum_{n=1}^{N} \{y_n - t_n\} x_n^{-7}$$

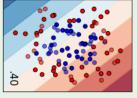
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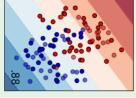
## Logistic regression

#### Example

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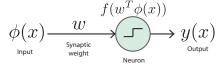






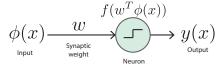
As you can see the results are very similar to LD, but because of probabilistic formulation we have an explicit probability of belonging to one or the other class (not shown); this can be very useful in real-world applications (e.g. self-driving cars or cancer detection).

- It is the very beginning of neural network models in ML!
- It is directly inspired on how neurons process information:



<sup>&</sup>lt;sup>8</sup>Intuitively we want to improve our chances of having  $t_n = y_n = -1$  or  $t_n = y_n = 1$ , which will both decrease our error function.

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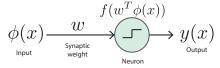


It is an example of a linear discriminant model given by  $y(\mathbf{x}) = f(\mathbf{w}^T \phi(\mathbf{x}))$ 

with a nonlinear activation function 
$$f(a) = \begin{cases} +1, & a \ge 0 \\ -1, & a < 0 \end{cases}$$

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- ▶ Here the target  $t = \{+1, -1\}$ .
- And we aim to mimimise the following error  $-\sum_{n=1}^{N} \mathbf{w}^{T} \phi_{n} t_{n}^{8}$

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## Example



## The Perceptron of Rosenblatt (1962)

The perceptron played an important role in the history of machine learning (Rosenblatt 1962). Indeed it represents the very start of the current *deep learning* revolution. Frank Rosenblatt used IBM and special-purpose hardware for a parallel implementation of perceptron learning. Rosenblatt's work was criticized by Marvin Minksy, who showed that such models could only learn *linearly separable problems*. However, this limitation is only true in the case of single layers!

source: Bishop p193.

## Quiz and video time!



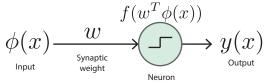
Watch this very cool video about the perceptron <sup>9</sup>.

Go to Blackboard unit page » Quizzes » Week 1 » Classification and neural networks

[Should take you less than 5 minutes]

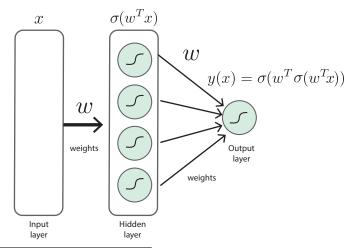
<sup>&</sup>lt;sup>9</sup>Note the comment at the end – it underlies all the recent successes using deep learning!

From a single layer perceptron:



However these and other linear (or near-linear) models have limited expressibility due to the *curse of dimensionality*.

To a Multiple Layer Perceptron (MLP) 10:



<sup>&</sup>lt;sup>10</sup>Although, we call it perceptron, it typically uses logistic sigmoid activation functions (continous nonlinearities), instead of step-wise discontinous nonlinearities.

- Neural networks are at heart composite functions of linear-nonlinear functions.
- ▶ Deep learning<sup>11</sup> refers to neural networks (or MLPs) with more than 1 hidden layer
- ► They can be applied in any form of learning, but we will focus on supervised learning and classification in particular

<sup>&</sup>lt;sup>11</sup> If you would like to learn more take our Applied Deep Learning unit in your 4th year.

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- ► They can be applied in any form of learning, but we will focus on supervised learning and classification in particular
- ► MLP recipe <sup>12</sup>:
  - ▶ Define architecture (e.g. how many hidden layers and neurons) <sup>13</sup>
  - Define cost function (e.g. mean squared error)
  - Optimise network using backprop:
    - 1. Forward pass calculate activations; generate  $y_k$
    - 2. Calculate error/cost function
    - 3. Backward pass use backprop to update parameters

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# Neural networks – forward pass step-by-step

- 1. Calculate activations of the hidden layer h:  $a_j = \sum_{i=1}^D w_{ji} x_i^{(h)} + w_{j0}^{(h)}$  [linear]
- 2. Pass it through a nonlinear function:  $z_i = \sigma(a_i)$  [nonlinear<sup>14</sup>]

<sup>&</sup>lt;sup>14</sup>In MLP we typically use sigmoid functions.

<sup>&</sup>lt;sup>15</sup>For classification problems we use a sigmoid at the output, where each output neuron codes for one class.

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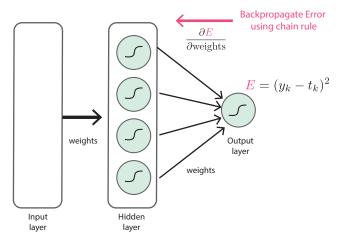
5. All together: 
$$y_k = \sigma \left( \sum_{i=1}^{D} w_{kj} \, \sigma \left( \sum_{i=1}^{D} w_{ji} x_i^{(h)} + w_{j0}^{(h)} \right) + w_{k0}^{(o)} \right)$$

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We now need to optimise our weights, and as before we use derivatives to find a solution. Effectively backpropagating the output error signal across the network – backpropagation algorithm.



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 $<sup>^{16}\</sup>sigma'$  denotes the derivative of the sigmoid activation function.

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- 2. Use the *chain rule* to compute the gradients w.r.t.  $\boldsymbol{w}$ ,  $\frac{dE}{dw}$
- 3. For the output weights  $w_{kj}$  we get:

$$\frac{\partial E}{\partial w_{kj}} = \frac{\partial \dot{E}}{\partial y_k} \frac{\partial y_k}{\partial \sigma} \frac{\partial \sigma}{\partial w_{kj}} = \sigma'(y_n - t_n) z_j^{16}$$

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We now need to optimise our weights, and as before we use derivatives to find a solution. Effectively backpropagating the output error signal across the network – backpropagation algorithm.

- 1. Compute the error (or cost) function: e.g.:  $E = \frac{1}{2} \sum_{n=1}^{N} (y(x_n, w) t_n)^2$
- 2. Use the *chain rule* to compute the gradients w.r.t.  $\boldsymbol{w}$ ,  $\frac{dE}{dw}$
- 3. For the output weights  $w_{kj}$  we get:

$$\frac{\partial E}{\partial w_{kj}} = \frac{\partial \dot{E}}{\partial y_k} \frac{\partial y_k}{\partial \sigma} \frac{\partial \sigma}{\partial w_{kj}} = \sigma'(y_n - t_n) z_j^{16}$$

4. Whereas for the input weights  $w_{ji}$  we get:

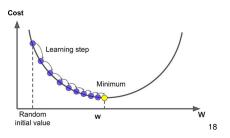
$$\frac{\partial E}{\partial w_{ji}} = \frac{\partial E}{\partial y_k} \frac{\partial y_k}{\partial \sigma} \frac{\partial \sigma}{\partial z_j} \frac{\partial z_j}{\partial \sigma} \frac{\partial \sigma}{\partial w_{ji}} = \sigma'(y_n - t_n) w_{kj}^T \sigma' x_i^{17}$$

 $<sup>^{16}\</sup>sigma'$  denotes the derivative of the sigmoid activation function.

<sup>&</sup>lt;sup>17</sup>Note that the updates for the bias terms  $w_0$  do not depend on the activity of the previous layer  $z_i$  and  $x_i$ .

# Neural networks - gradient descent 19

In many ML methods is common to iteratively update the parameters by descending the gradient.

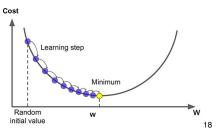


<sup>18</sup> Figure from https://mc.ai/an-introduction-to-gradient-descent-2/

<sup>19</sup> Its called descent because we are minimising the cost function, so descending on the function landscape, which can be quite hilly!

# Neural networks - gradient descent 19

In many ML methods is common to iteratively update the parameters by descending the gradient.



In our neural network this means to update the weights using:

- $ightharpoonup w_{ji} = w_{ji} \Delta w_{ji}$ , where  $\Delta w_{ji} = \sigma'(y_n t_n) w_{kj}^T \sigma' x_i$
- $ightharpoonup w_{kj} = w_{kj} \Delta w_{kj}$ , where  $\Delta w_{kj} = \sigma'(y_n t_n)z_j$
- This is often done in mini-batches using a small number of samples to compute Δw.

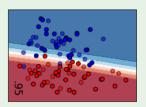
<sup>18</sup> Figure from https://mc.ai/an-introduction-to-gradient-descent-2/

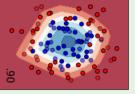
<sup>19</sup> Its called descent because we are minimising the cost function, so descending on the function landscape, which can be quite hilly!

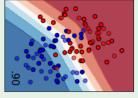
#### Neural networks

#### Example

Using sklearn we fitted a MLP classifier to the data:

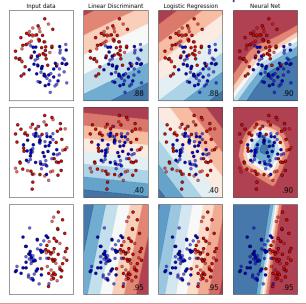






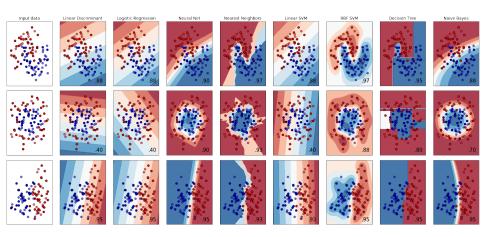
As you can see a MLP (with one hidden layer) can indeed perform very well in nonlinear classification problems. Note, however, because MLPs are highly flexible models they can easily *overfit* the data. To prevent this methods such as *early stopping* (stop when test performance starts decreasing) and *dropout* (randomly drop units in the network) are used.

# Classification methods — overall comparison [Input data Linear Discriminant Logistic Regression Neural Net



## Classification methods - overall comparison [including

methods from the upcoming lectures]



# Tasks

▶ Post questions Teams > QA channel or bring them to the next lecture

#### **Tasks**

- Post questions Teams > QA channel or bring them to the next lecture
- Next lab (Week 2): Neural nets and SVMs
  - 1. See link to lab 2 on BB