TYPE SYSTEM

$$x: \forall \overline{a}. \ A \in \Gamma \quad \frac{}{\Gamma \vdash x: A[\overline{B}/\overline{a}]} \quad (TVar)$$

$$\frac{\Gamma \vdash M: B \to A \quad \Gamma \vdash N: B}{\Gamma \vdash MN: A} \quad (TApp)$$

$$x \notin \text{dom } \Gamma \quad \frac{\Gamma \cup \{x: B\} \vdash M: A}{\Gamma \vdash \lambda x. M: B \to A} \quad (TAbs)$$

1

SUBFORMULA PROPERTY

Theorem (The Subformula Property)

Suppose Γ assigns only monotypes to its subjects and suppose M is in β -normal form and $\Gamma \vdash M$: A. Then the derivation of this judgement is unique and all of the types mentioned in the derivation are substrings of the types mentioned in the conclusion.