

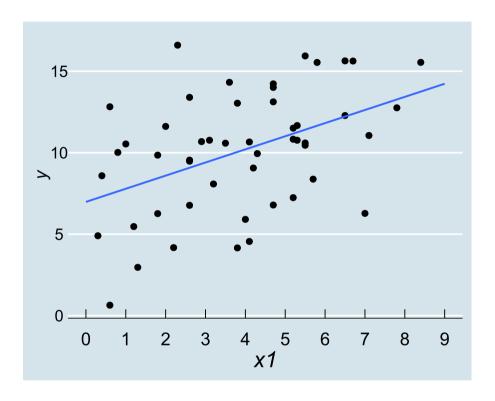
Week 11: Some Kind of End to the Course

Univariate Statistics and Methodology using R

Department of Psychology The University of Edinburgh Part 1

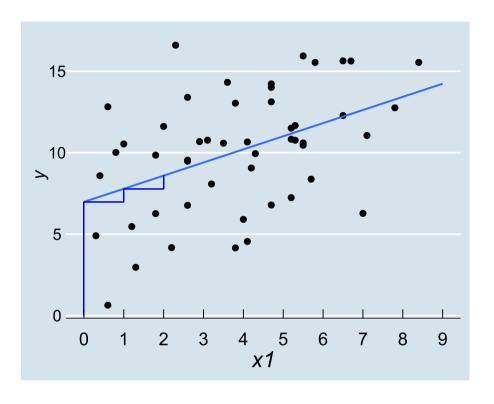
Week 7 - 10 Recap

Describing a pattern with a line



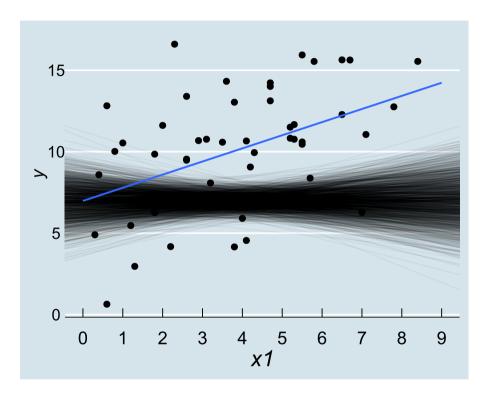
```
ggplot(df, aes(x = x1, y = y)) +
  geom_point()
```

Coefficients describe the line



$$y_i = b_0 + b_1(x_{1i}) + \varepsilon_i$$

We can test the coefficients

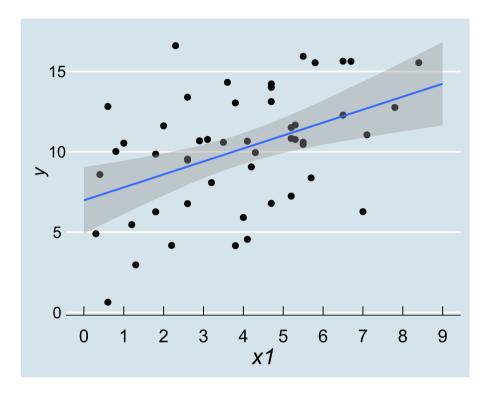


$$y_i = b_0 + \textcolor{red}{b_1}(x_{1i}) + \varepsilon_i$$

In the "null universe" where $b_1=0$, when sampling this many people, what is the probability that we will find a relationship at least as extreme as the one we *have* found?

```
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 6.982 1.026 6.81 1.5e-08 ***
## x1 0.806 0.234 3.45 0.0012 **
```

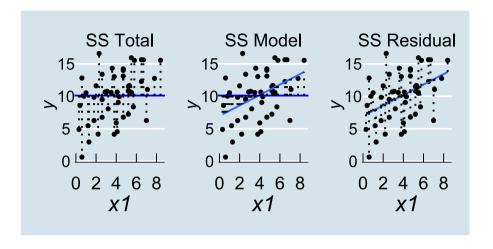
We can test the coefficients



$$y_i = b_0 + extstyle{b_1}(x_{1i}) + arepsilon_i$$

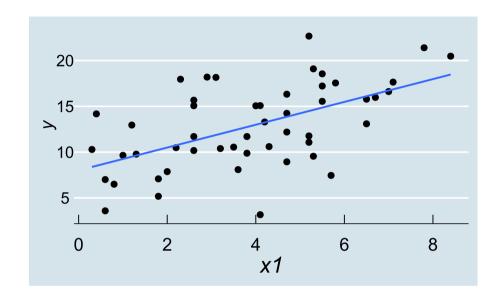
Plausible range of values for b_1 :

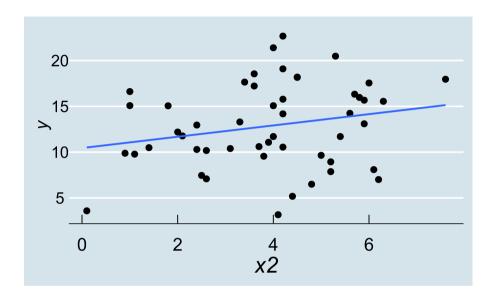
We can test the model



```
##
## Multiple R-squared: 0.199, Adjusted R-squared: 0.182
## F-statistic: 11.9 on 1 and 48 DF, p-value: 0.00118
```

More predictors

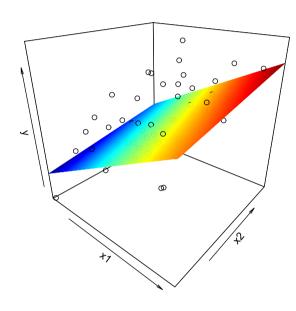




More predictors (2)

$$y_i = b_0 + b_1(x_{1i}) + b_2(x_{2i}) + \varepsilon_i$$

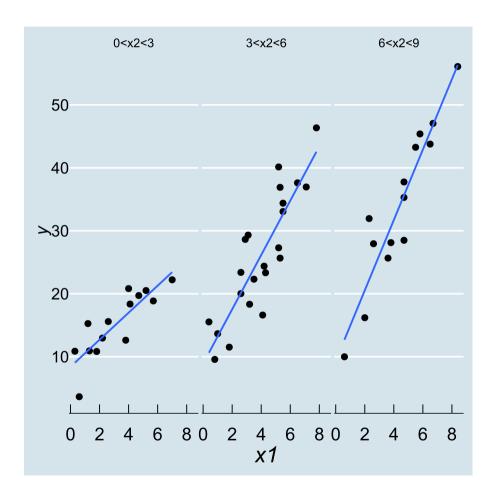
More predictors (3)

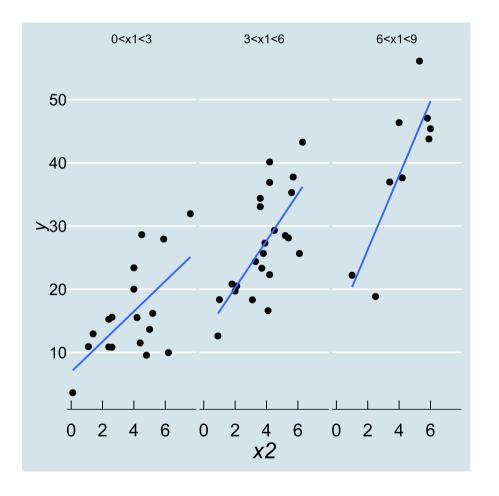


Even more predictors...

$$y_i = b_0 + b_1(x_{1i}) + b_2(x_{2i}) + \ldots + b_k(x_{ki}) + arepsilon_i$$

associations that depend on other things

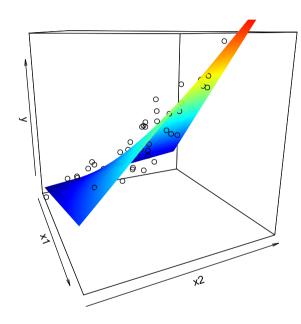




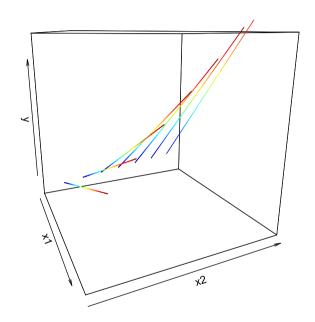
interactions

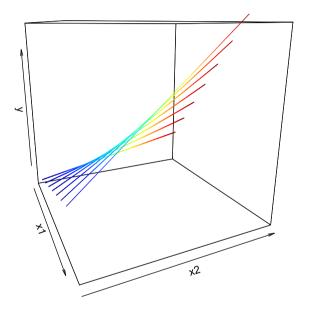
$$y_i = b_0 + b_1(x_{1i}) + b_2(x_{2i}) + b_3(x_{1i} \cdot x_{2i}) + arepsilon_i$$

interactions



interactions (2)

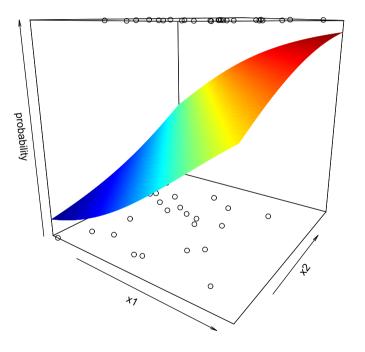




other outcomes

$$ln(rac{p}{1-p}) = b_0 + b_1(x_{1i}) + b_2(x_{2i})$$

$$ln(rac{p}{1-p}) \, \Rightarrow \, rac{p}{1-p} \, \Rightarrow \, p$$



Checking Assumptions: Linear Models

required

- linearity of relationship
- for the *residuals*:
 - normality
 - homogeneity of variance
 - independence

desirable

- uncorrelated predictors
- no "bad" (overly influential) observations

Checking Assumptions: Logit Models

required

- linearity of relationship between IVs and log-odds
- for the residuals:
 - normality
 - homogeneity of variance
 - o independence

desirable

- uncorrelated predictors
- no "bad" (overly influential) observations
- large samples (due to maximum likelihood fitting)

End of Part 1

Part 2

Common Tests as linear models

usmr <- read_csv("https://uoepsy.github.io/data/usmr2022.csv")</pre>

lm vs correlation

regression, continuous predictor

```
summary(lm(sleeprating ~ height, data = usmr))
##
## Call:
## lm(formula = sleeprating ~ height, data = usmr)
##
## Residuals:
     Min
             10 Median
  -65.42 -11.66 5.52 16.96 36.16
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 18.785
                           46.879
                                      0.4
                                              0.69
## height
                 0.279
                            0.278
                                      1.0
                                              0.32
## Residual standard error: 22.6 on 76 degrees of freedom
## (2 observations deleted due to missingness)
## Multiple R-squared: 0.013, Adjusted R-squared: 4.73e-05
## F-statistic: 1 on 1 and 76 DF, p-value: 0.32
```

Correlation

```
##
## Pearson's product-moment correlation
##
## data: usmr$height and usmr$sleeprating
## t = 1, df = 76, p-value = 0.3
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.1112 0.3284
## sample estimates:
## cor
## 0.1142
```

lm vs t.test

regression, intercept

```
summary(lm(height ~ 1, data = usmr))
##
## Call:
## lm(formula = height ~ 1, data = usmr)
##
## Residuals:
      Min
               1Q Median
                                      Max
## -15.407 -7.607 -0.107 7.523 20.893
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 168.11
                            1.04
                                     162 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 9.22 on 78 degrees of freedom
## (1 observation deleted due to missingness)
```

one sample t.test

```
##
## One Sample t-test
##
## data: usmr$height
## t = 162, df = 78, p-value <2e-16
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## 166.0 170.2
## sample estimates:
## mean of x
## 168.1</pre>
```

lm vs t.test (2)

regression, binary predictor

```
summary(lm(height ~ catdog, data = usmr))
##
## Call:
## lm(formula = height ~ catdog, data = usmr)
##
## Residuals:
               1Q Median
      Min
## -13.655 -7.501 0.499
                           8.399 19.499
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 166.36
                            1.55 107.60 <2e-16 ***
## catdogdog
                  3.15
                            2.07
                                   1.52
                                             0.13
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 9.15 on 77 degrees of freedom
## (1 observation deleted due to missingness)
## Multiple R-squared: 0.0291, Adjusted R-squared: 0.0165
## F-statistic: 2.31 on 1 and 77 DF, p-value: 0.133
```

two sample t.test

lm vs Traditional ANOVA

regression, binary predictor

```
summary(lm(height ~ eyecolour, data = usmr))
##
## Call:
## lm(formula = height ~ eyecolour, data = usmr)
##
## Residuals:
             1Q Median
     Min
                                 Max
## -17.55 -5.77
                  0.00
                         6.79 17.75
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
                  170.254
## (Intercept)
                               2.183
                                       77.99
                                               <2e-16 ***
## eyecolourbrown -3.682
                               2.609
                                       -1.41
                                                 0.16
## eyecolourgreen
                    2.717
                               4.125
                                        0.66
                                                 0.51
## evecolourgrev
                   -0.254
                               9.515
                                       -0.03
                                                 0.98
## eyecolourhazel
                   -2.404
                               3.935
                                       -0.61
                                                 0.54
## eyecolourother
                   -4.834
                               5.775
                                       -0.84
                                                 0.41
## Signif. codes: 0 '***' 0.001 '**' 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 9.26 on 73 degrees of freedom
## (1 observation deleted due to missingness)
## Multiple R-squared: 0.0563, Adjusted R-squared: -0.00837
## F-statistic: 0.871 on 5 and 73 DF, p-value: 0.505
```

anova

lm vs Traditional ANOVA

If you should say to a mathematical statistician that you have discovered that linear multiple regression and the analysis of variance (and covariance) are identical systems, he would mutter something like "Of course—general linear model," and you might have trouble maintaining his attention. If you should say this to a typical psychologist, you would be met with incredulity, or worse. Yet it is true, and in its truth lie possibilities for more relevant and therefore more powerful research data.

Cohen (1968)

History

Multiple Regression

- introduced c. 1900 in biological and behavioural sciences
- aligned to "natural variation" in observations
- tells us that means (\bar{y}) are related to groups (g_1, g_2, \ldots, g_n)
- both produce *F*-ratios, discussed in different language, but identical

ANOVA

- introduced c. 1920 in agricultural research
- aligned to experimentation and manipulation
- ullet tells us that groups $\overline{(g_1,g_2,\ldots,g_n)}$ have different means $(ar{y})$

Why Teach LM/Regression?

- LM has less restrictive assumptions
 - o especially true for unbalanced designs/missing data
- LM is far better at dealing with covariates
 - o can arbitrarily mix continuous and discrete predictors
- LM is the gateway to other powerful tools
 - mixed models and factor analysis (→ MSMR)
 - o structural equation models

Goodbye!

