The Procedure

- 1. Bob chooses prime numbers p, q so that pq = n > c, where c is the size of the largest message they expect to encrypt. n is called the key length.
- 2. Bob chooses e, d by first computing $\varphi(n) = (p-1)(q-1)$, then choosing e so that $\gcd(e, \varphi(n)) = 1$. Bob can then release the keypair (e, n), and now each Alice, Bob, and Eve have their own step to perform.

Bob: computes the multiplicative inverse of $e \pmod{\varphi(n)}$, using Wolfram-Alpha, in order to find his private key d.

Alice: chooses a message which is converted to a large natural number M. We have many ways of doing this, however for the purpose of this exercise we will use $a=1,b=2,\ldots,z=26$, and a space is 00. For messages longer than a single character, simply combine the letters. For example, a message "abc" will be encoded with M=010203. Alice encrypts her message text with Wolfram-Alpha using $M^e\pmod{n}$, and reveals it to both Bob and Eve.

Eve: uses Wolfram-Alpha to attempt to factor n, and if successful, uses the p, q she finds in order to find d (see Bob's instructions above).

3. Now Bob and Eve (if successful) should reveal the decrypted messages; and confirm whether they recieved it.

Exercise 1

For the first exercise, delegate who will be Bob, Alice, and Eve, and perform the procedure with p = 2 and q = 13. This is exactly enough to encrypt a message of one character. Fill out the following:

- 1. What was the message sent by Alice?
- 2. What was Bob able to decrypt?
- 3. What was Eve able to encrypt?
- 4. How secure was the message?
- 5. How private was the message?

Exercise 2

For the second exercise, use bigprimes org or some other random site to choose some primes p, q with 6 digits. This is guaranteed to be enough for a 5-letter message, and could be 6 if the primes are large enough. All participants will need Wolfram-Alpha.

- 1. What was the message sent by Alice?
- 2. What was Bob able to decrypt?
- 3. What was Eve able to encrypt?
- 4. How secure was the message?
- 5. How private was the message?

Exercise 3

For the final exercise, use bigprimes org or some other random site to choose some primes p, q with enough digits that Bob and Alice can agree that Eve will not be able to factor n using Wolfram (How can they check this!). It may

- 1. What was the message sent by Alice?
- 2. What was Bob able to decrypt?
- 3. What was Eve able to encrypt?
- 4. How secure was the message?
- 5. How private was the message?