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HOW THE DUTCH AND THE ENGLISH ADOPTED
MULTIREGIONAL MODELS FOR SUBNATIONAL
POPULATION PROJECTION

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HOW THE DUTCH AND THE ENGLISH
ADOPTED MULTIREGIONAL MODELS
FOR SUBNATIONAL POPULATION PROJECTION

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CONTENTS

Contents
List of Tables
List of Figures
Abstract

1. INTRODUCTION

2. FORECASTING REQUIREMENTS

- 2.1 Population numbers, age disaggregation and time intervals
- 2.2 Detailed inputs and outputs
- 2.3 An example of projection outputs
- 2.4 A specific or a general model?
- 2.5 Issues concerned with the spatial units adopted
- 2.6 Summary of the user's requirements for a subnational population projection model

3. MULTIREGIONAL POPULATION MODELLING: THE BARE NECESSITIES

- 3.1 The case for multiregional population modelling
- 3.2 Migration concepts and projection models
- 3.3 The role of population accounts
- 3.4 Transition accounts
- 3.5 Movement accounts
- 3.6 Age matters
- 3.7 Summary of the modelling requirements for a subnational population projection model

4. THE DATA BASES

- 4.1 The data base for the Netherlands
- 4.2 The data base for the United Kingdom

5. THE PROJECTION MODELS

- 5.1 MUDEA: a multiregional model for the Netherlands
 - 5.1.1 The model
 - 5.1.2 Inputs
 - 5.1.3 Outputs
- 5.2 The OPCS/DOE subnational population projection model for England
 - 5.2.1 The model
 - 5.2.2 Comments
 - 5.2.3 Outputs

6. CONCLUSIONS

REFERENCES

APPENDIX

LIST OF TABLES

1. Transition accounts and associated rates for Great Britain, 1966-71, age transition 20-24 to 25-29, persons.
2. Movement accounts and associated rates for the Netherlands, 1976, age transition 20 to 21, females.
3. Summary of the output tables produced by the MUDEA model.
4. Summary of the output tables produced by the OPCS/DOE model.
- A.1 Demographic indicators, Netherlands (from UN, 1985)
- A.2 Population (in 1000s) by age and sex, medium variant (from UN, 1985), Netherlands
- A.3 Demographic indicators, United Kingdom (from UN, 1985)
- A.4 Population (in 1000s) by age and sex, medium variant (from UN, 1985), United Kingdom

LIST OF FIGURES

1. The steps in the incorporation of migration data in regional population projections.
2. Examples of migration rate profiles.

ABSTRACT

The Netherlands and the United Kingdom have both introduced multiregional models to carry out part of the task of projecting the population of subnational areas. This paper describes and compares these efforts. They are also evaluated in two ways: against the requirements of potential users of forecasts and against the principles that should be applied in sound multiregional population models.

1. INTRODUCTION

In both the Netherlands and the United Kingdom national government departments responsible for the production of population projections for both the nation and subnational units have recently sought to improve those projections through the development and implementation of new multiregional models. Researchers and consultants outside of central government were asked to prepare these models (Martin & Voorhees Associates and Bates 1981; Willekens and Drewe 1981, 1984). In this paper these efforts are described and compared in order to assess what has been achieved to date and what improvements could be effected. A particular emphasis is laid on assessment of the outputs available from such models.

In the next section of the paper the needs of users of subnational population projections are assessed. In section three the conceptual bases of multiregional models are briefly reviewed. Section four outlines the nature of the data bases available for use in population projections in the two countries. The fifth section outlines and compares the new population models. The final part of the paper assesses the models and elicits lessons.

2. FORECASTING REQUIREMENTS

Here we review the demands of users of population projections rather than the wishes of population modellers. The latter need to assess the requirements of the "market" for their product carefully, and to invest rather more attention than hitherto in the presentation of model outputs. Because of the large number of variables used in multiregional population models, this issue must be the concern of the model designer/systems analyst, and not just a task relegated to a later stage in the development of a projection system.

2.1 Population numbers, age disaggregation and time intervals

Users of population projections, be they planners or academics, most usually require knowledge of population numbers at short intervals for varying periods into the future.

The populations are broken down into detailed age groups, not for their own sake, but in order to yield good estimates of target client or service or market populations. Examples are the school populations in various grades, the numbers of potential students qualified to enter higher education, the labour force, or the retired population. The age classification of the population needed to estimate these target populations must be as fine as possible, preferably by single years of age.

Full details of all single year age populations are rarely required but flexible aggregations of these ages are needed. For example, to assess the viability of alternative plans for school reorganization in Leeds, the City Education Committee required projections for the 5-8, 9-13, 14-18 age groups in one scheme, and the 5-10, 11-16, 17-18 age groups in another.

Very often, population numbers themselves are insufficient to define the target population. Further disaggregation may be needed. In the school planning case, an estimate is required of the proportions in any age group entering independent and state supported schools, and within the state sector the proportions or numbers likely to enter Roman Catholic, Anglican or secular schools.

2.2 Detailed inputs and outputs

Most population projection models can be designed to yield not only fine detail on the population stocks at regular intervals but also fine detail on the demographic components that link successive population stocks. Users do not normally require, for example, detailed information on mortality or migration rates used in the projections by single years of age, but they probably wish to know what those rates mean in terms of summary measures such as the crude death rate, life expectancy, the crude migration rate or gross migration rate. A detailed account of interregional migration by single years of age is seldom used but a summary of interregion flows by broad age groups would be of interest. But if the number of regions was large, even an interregion matrix would be too detailed, and a summary of the main or total inflows and outflows for each region would be preferable.

To generalize this point, we can say that multiregional population projection models operate with variables at a level of disaggregation much finer than that required by most users and that any implementation of such models should aim to provide relevant summaries of the information generated.

2.3 An example of projection outputs

To exemplify these points, we examine the practice adopted by the United Nations (UN) in their latest, very useful set of population estimates and projections as assessed in 1982 (UN, 1985). The results for the Netherlands and the United Kingdom are reproduced in Appendix 1.

Tables A.2 and A.4 show the estimates and projections of the populations of the two countries at 5 year intervals from 1950 to 2025 for

both sexes and for 5 year age groups to 80+ years in a one page format (compressing two pages of computer printout).

Tables A.1 and A.3 summarize the population stock information by broad age groups and provide a set of indicators of the age and sex structure of the population in the first of three sub-tables. The second sub-table provides information on component rates in the 5 year time intervals and summarizes the fertility and mortality levels using nine indicators. The final sub-table gives a selection of the indicators for high fertility and low fertility variants.

The same set of statistics is provided by the UN for all constituent countries and for continental, sub-continental and more/less developed areas, so that comparisons across and between all scales are a simple matter. All the statistics are available to users on magnetic tape for further analysis.

A key feature of the UN projections is the emphasis on presenting statistics over time: time points or intervals are used as the column dimension in all tables. Time series analysis of the results is intended and made easy by such a presentation (e.g. Keyfitz and Vaupel, 1986). The UN projections provide guidelines against which the presentation of subnational projection results can be assessed.

What is less satisfactory about the UN projections, however, is the lack of detail provided about the models and programs used to generate the results. UN(1985, p.3) suggests that 5 year time and age intervals were used throughout to generate tables of the A.2 and A.4 type, but no details are provided on the methods used to produce the annual population figures and other age group numbers contained in the first sub-table of the A.1 and A.3 type.

2.4 A specific or a general model?

Population projection models and their associated software may be specific to the particular system being studied or they may be used more generally with a variety of systems of interest. Academic researchers incline to the latter kind of model because they wish to study many different systems; government researchers prefer the former, both because the model and associated software are easier to design and because their attention is focussed on the current set of subnational units.

This issue is far more serious if a multiregional modelling strategy is adopted. A single region cohort survival model with net migration rates or flows does not require alteration when used with more regions. The same model is simply used more times. However, in multiregional models an expansion from N regions to 2N may require redesign of the

software (because interaction variable dimensions increase in proportion to N^2) or redesign of the model (because with very many regions in relation to the size of the population many of the cells in the migration matrix may contain small and unreliable numbers). The model used will vary with the size of the system being modelled.

Although system specific models are easier to design and program, even in governmental use there will be problems occasioned by the frequent re-specification of subnational areas prompted by politicians either because the settlement system has changed or because electoral advantage may be thereby gained. It may be worthwhile, therefore, investing in a more general model for long term use designed to withstand severe "spatial shock".

2.5 Issues concerned with the spatial units adopted

The strategies for modelling the populations of a large number of regions have been reviewed in Rogers (1976) and Rees (1979a, 1981b) and may be summarized as follows.

(1) Fully multiregional

All regions in the system are modelled simultaneously in a multiregional model in full age and sex detail. Problems of small numbers or unreliable data are ignored.

(2) Partitioned

The system of regions may be partitioned into sub-systems, interregional migrations within which are modelled explicitly while migration between regions in different subsystems is modelled at the subsystem level.

(3) Aggregated

Some of the variables in the system are aggregated or pooled across the spatial or the age dimension of the model. For example, in the subnational projections for England (OPCS, 1984) migration between 108 subnational units is modelled for three aggregate age groups (see section five for more details). Another popular choice is to divide the migration process into a process of choosing to move and a process of selecting a destination (Frey, 1984).

(4) Biregional

In this strategy the system is collapsed into N sets of 2 regions consisting of the area of interest and the rest of the nation (although flows to and from the rest of the world should also be incorporated in the model).

All the strategies listed above can be termed "multiregional" because they retain at least some of the interactions and interdependency between

regions. Solutions (1) and (4) lead to general and portable models. Solutions (2) and (3) result in models specific to the system being studied. Each solution will yield a different set of projections, and the subnational projections will not necessarily add to the figures obtained in projecting the national population. A decision has then to be made about whether to adjust the subnational populations or to accept their sum as the national projections.

2.6 Summary of the user's requirements for a subnational population projection model

To summarize, users of population projections for subnational units require:

- (1) future populations classified by single years of age and sex;
- (2) summary measures of the inputs to the projections for each interval;
- (3) summary measures of the components of change in each future period;
- (4) time oriented presentation of the projection results;
- (5) standard presentation of the projection results at all scales;
- (6) a model (or its software) general enough to cope with a redefinition of the spatial units of projection; and
- (7) an effective strategy for projecting the population of a large number of units, either across the country or within a particular region.

Having discussed the needs of users of forecasts and some of the issues that producers of national forecasts face, we review in the next section the main features of multiregional population modelling.

3. MULTIREGIONAL POPULATION MODELLING: THE BARE NECESSITIES

3.1 The case for multiregional population modelling

A strong case has been made for two decades now that the only proper way to project regional populations is to model explicitly the migration flows between them along with the mortality, fertility and external migration components involved (see Rogers 1985a, 1985b, Willekens 1985b and Rees 1986a for recent surveys). Use of net migration rates or flows can lead in the long run to absurd results. By explicitly modelling interregional migration flows using interregional transition rates, the influence of one region's population dynamics on that of another is captured. The same case can be made for explicitly modelling international migration in a similar way but data difficulties usually mean that a net flow or rate term is used. However, external migration must be included in a regional population projection in order to close the population account (Rees 1986b).

3.2 Migration concepts and projection models

For nearly a decade now a clear link has been recognized between the form in which migration activity is recorded and the form which the multiregional population projection model should take (Rees 1977; Ledent 1978, 1979; Ledent and Rees, 1980, 1986; Rees 1985). There are three principal sources of migration data: censuses, population registers and surveys. Survey data on migration are not as yet used much for projection purposes and they are not considered further here.

The national census frequently contains a retrospective question on the place of residence at some date in the past. The date can be fixed, for example, when the place of residence n years ago is recorded, or variable, for example, when the place of birth or place of residence at a given age is recorded. Alternatively, the census may contain a question on the previous residence, without any information on the time of migration.

Population registers typically contain information on each change of usual address. Cross-classifications of regions of residence at two points of time are referred to as transition data and migrations data based on changes of residence are denoted as movement data. Transition data are used to compute transition probabilities directly which are entered in the multiregional cohort survival model as rates of migration and survival or survivorship rates. Movement data are used to compute occurrence-exposure rates from which probabilities suitable for entry into multiregional cohort survival models can be estimated.

Figure 1 sets out the broad steps involved in using the two different migration data sets in a multiregional population projection model. Two further points emerge from the diagram. The first is that mortality, fertility and external migration data are similar in the transition and movement approaches. The second is that there are two alternatives in the transition approach. If data are available giving the number of persons surviving and staying in the same region, survivorship rates can be estimated without recourse to mortality data. If they are not available or reliable, the number of surviving stayers must be estimated as a residual thus:

$$\begin{array}{lcl} \text{surviving stayers} & = & \text{initial population less internal out-migrants} \\ & & \text{less emigrants} \quad \text{less non-survivors} \end{array} \quad (1)$$

These computations are best organized in a population accounting framework.

Even if surviving stayer information is available it may still be preferable to incorporate mortality information into the projection

process so that the risk of mortality can be separated from that of migration:

$$\begin{array}{l} \text{probability of} \\ \text{migrating and} \\ \text{surviving} \end{array} = \begin{array}{l} \text{probability of} \\ \text{migration given} \\ \text{survival} \end{array} \times \begin{array}{l} \text{probability of} \\ \text{survival} \end{array} \quad (2)$$

and the effect of future trends in mortality monitored.

3.3 The role of population accounts

Population accounts are tables which display in a consistent fashion all the inputs from and outputs to a regional population. It is not appropriate here to give a full description (see Rees and Wilson 1977 and Rees 1981a for details of transition accounts and Rees 1984 for details of movement accounts), nor is it necessary to construct accounts before computing the rates that enter multiregional population models. But population accounts do provide yardsticks of the consistency with which population models have been put together, and transition and movement accounts are therefor described here using a British and a Dutch example.

3.4 Transition accounts

Table 1 sets out a set of transition accounts for a three region division of Great Britain for one age group transition in a 5 year period, 1966-71 (from Rees 1979b). The number of surviving internal migrants are entered in the table directly: 7578 between East Anglia and the South East, 8141 from East Anglia to the Rest of Britain, 14408 from the South East to East Anglia and so on to the 84510 from the Rest of Britain to the South East. The fourth column contains an estimate of the numbers of surviving emigrants (5296, 101985, 107473) and the fourth row holds the numbers of surviving immigrants (7790, 88045, 70123). The other data entered in the account are the initial regional populations (101007, 1184032, 2284298) and regional deaths (392, 3998, 8353). An accounts based model is then used (Rees 1981) to estimate the non-survivor elements in the table (the block on the right hand side) and the surviving stayers (79620, 984059, 2074448). The survivor columns of the account can then be totalled to yield the end of period populations. There will be such an account for each age group to age group transition, from the first which involves persons born within the time interval to the last which involves survival of the most aged population 5 years into the future.

The bracketed figures in Table 1 associated with selected cells of the account are transition probabilities or immigration or mortality rates that can be used in a regional projection model. Thus, the number of surviving migrants from the South East to East Anglia would be projected

by multiplying the appropriate probability by the population of 20-24 year olds in the South East in 1971 = $.01217 \times 1,362,256 = 16,579$ migrants in 1971-76.

3.5 Movement accounts

Table 2 shows a movement account for a 2 region system in the Netherlands in 1976 for women aged 20 on January 1st 1976 and 21 on January 1st 1977. The account is simpler than that of Table 1 in that total regional deaths no longer appear in the last internal column. The entries in the table are counts of moves between the West Netherlands and the Rest of the Netherlands (1375 and 1739), of emigrations from the two regions (402 and 437), of immigrations to them (759 and 546) or of deaths within them (17 and 23). The diagonal term is computed as a residual (e.g. $49121 - 50915 - 17 - 402 - 1375$) and is not an event count. The bracketed figures in the table are occurrence-exposure rates in which the occurrences (moves) are divided by the populations exposed to the risk of the event weighted by their exposure (approximated by the average population): thus the rate of movement from the Rest of the Netherlands to the West Netherlands is $.02821 = 1739 / 0.5 \times (61794 + 61516)$. To project the population forward using these rates an accounts based model can be used (Rees 1984, 1986a, 1986b) which involves a small number of model iterations or a matrix method can be employed to convert the rates shown in the table into transition probabilities (see Willekens and Drewe 1984). Again there are accounts for each age transition from the first, born in the year to age 1, through 20 to 21 shown in Table 2, to the last, 90+ to 91+. Births are generated in the model using fertility rates and populations at risk in the fertile age range before being subjected to migration and mortality risks. Similarly, the flow of immigration is also subjected to migration and mortality processes. Both types of new arrivals (infants and immigrants) are, however, only exposed for half the time interval, on average, to these forces.

3.6 Age matters

In constructing any population model care must be exercised in adopting the correct age-time plan (ATP) in which the data are observed or estimated. Four age-time plans may be distinguished (Willekens, 1985a): the age-cohort plan, in which events are classified by the cohort to which a person belongs and the age at the time of the event; the age-period (or just period) plan, in which the age and the calendar period at the time of the event are recorded; the period-cohort plan, in which the cohort is recorded to which a person belongs and the calendar period in which the event occurs; and the age-period-cohort plan in which the age and the calendar period at the event together with the cohort are recorded. The period-cohort plan (see Rees and Woods, Figure 12.2) is the appropriate

one for projection purposes, and the implementation of any regional projection model is considerably simplified if all age classified data are assembled using this ATP or are converted to it through estimation prior to model specification.

A second age matter is the existence of regularities in the profiles of migration rates by age, thoroughly researched by Rogers and Castro (1986) and by many other authors. Figure 2 shows two examples from the Netherlands and the United Kingdom. These schedules can be summarized as being composed of three or more of the five components shown in the inset to Figure 2. For the Greater London profile in Figure 2 we would use a model with a retirement peak. For the West Netherlands only three components would be necessary. The large number of age specific migration rates (16 for Greater London, 92 for West Netherlands) can be reduced to 9, 11 or 13 model parameters. This proves to be of considerable utility in implementing single year of age multiregional population models.

3.7 Summary of the modelling requirements for a subnational population projection model

Work in the field of spatial population dynamics over the past decade suggests that the following guidelines be followed in designing a subnational projection model.

- (1) It should incorporate multiregional features.
- (2) Clear cognizance must be taken of the conceptual type of migration data available in designing the projection model. It has proved too easy in the past to muddle model design in this respect.
- (3) Although it is not essential to construct population accounts prior to projection, all the components included in population accounts must be consciously incorporated in the projection, either implicitly or explicitly.
- (4) It is preferable to prepare all input data for the base period and all rate or parameter changes in the projection periods using the period-cohort age-time observation plan. It has also proved very easy in the past to confuse this problem, which is one of estimation, with that of projection model design.
- (5) One useful method for handling the problem of too many variables that occurs in multiregional modelling is to use model parameters rather than rate schedules to represent age-disaggregated migration components (Rogers, 1986).

4. THE DATA BASES

4.1 The data base for the Netherlands

The Netherlands has a rich resource of socioeconomic information about its population. This is extensively reviewed in ter Heide and Willekens (1984), particularly in Part 2: Data in Chapters by van der Erf, by Scheurwater and by Gordijn, Heida and ter Heide. Migration data are also reviewed by Keilman (1986).

In principle, any information required for a regional projection model can be assembled from the migration data of the population register. These data, kept by the municipalities, are assembled by the Central Bureau of Statistics and are accessible through an interactive demographic information system called RUDAP ("Ruimtelijk Demografische Aspecten van Planprocessen") (Scheurwater 1984). Any set of regions can be assembled as long as they are amalgamations of current municipalities (774 from January 1982 van der Erf, 1984, p.52). The data are available for single calendar years up to the year prior to the present.

Migration data are available from the population register of the Netherlands and are counts of moves from one spatial unit to another, rather than transition counts.

One difficulty is that although the Central Bureau of Statistics prepares migrations and births data files using the period-cohort ATP, this isn't the method adopted for regional mortality data. At the regional level, deaths are classified by age at death and year of death (period ATP). The problem is a coding problem, since the year of birth and date of death are recorded on the death certificate. At the national level, mortality data are available by year of birth, year of death and age at death.

From this account of the data base available in the Netherlands for population projection at subnational scales, it is clear that any regional projection model must be based on the movement concept.

4.2 The data base for the United Kingdom

Demographic information available for subnational areas in the United Kingdom has steadily improved over the past two decades. Births and deaths data are now produced by the Office of Population Censuses and Surveys (OPCS) for very small areas (wards within local authority areas OPCS 1983, p.8), and the deaths data are disaggregated by age (0, 1-4, 5-14, 15-24 and 10 year age groups to 85+). Population data are available from the 1981 Census at the enumeration district (England, Wales, Northern Ireland) or postcode (Scotland) scale (circa 130,000 units). Estimates

are made by OPCS of the population at each mid-year following the census at local authority and health district scale. Unofficial estimates have been prepared by the CACI market research firm (OPCS 1985, p.8) at ward level.

Internal migration data are produced in the United Kingdom from two sources: the decennial Census and the National Health Service Central Register (NHSCR) of patient transfers. In the 1981 Census a question about place of residence one year prior to the census data (April 5) was asked and this generated tables of one year transition data for 1980-81 on both a local authority and ward scale. To fill the gap between censuses OPCS have established, in cooperation with the National Health Service, a system for recording changes of Family Practitioner Committee (FPC) areas by patients who re-register with a new FPC as a result of a migration. The FPC areas coincide, for the most part, with local authority areas as currently constituted (except for London boroughs, for which estimates are not available - OPCS, 1985, p.ix). No data are available for intra-area migration, which leads to difficulties when projections are required for finer areas than local authority districts. Prior to 1984 the NHSCR based statistics were published in an aggregate form (in- and out- migrations by age and sex, interarea migrations in total) and estimation methods were used to fill out the full region, age and sex disaggregated array (see Stillwell, 1986). From 1984 the individual migration records have been made available for users to create their own migration counts.

External migration data are generated from the International Passenger Survey (OPCS, 1986) but much careful estimation must be carried out (Rees and Woods 1986) to produce figures for subnational areas. Rather more reliable estimates of immigration for subnational areas are available in the Census but only for the year prior to the census date.

From this account of the data base available in the United Kingdom for population projection at subnational level, it is not clear whether a movement concept or a transition concept population projection model should be designed. In the former case, recourse to census transition data may be necessary to improve initial estimates of migration flows; in the latter case, recourse to NHSCR move data is necessary to update migration patterns for changes since the year prior to the last census.

We now examine what has been accomplished with these data bases.

5. THE PROJECTION MODELS

5.1 MUDEA: a multiregional model for the Netherlands

Between 1982 and 1984 a multiregional model for subnational population projection was developed at the Netherlands Interuniversity Demographic Institute (NIDI), under the direction of Frans Willekens of NIDI and Paul Drewe of Delft University of Technology under contract to the Physical Planning Agency (RPD) of the Netherlands. The project was overseen by and responded to an inter-ministry Committee for Regional Population Prognoses (CORBEP). The model structure is fully described in Willekens and Drewe (1984) and its intended application is briefly outlined in ter Heide (1984, p.346). Full details of the computer program and applications are available from NIDI.

5.1.1 The model

This model was developed

- (1) for two sexes;
- (2) for a variable number of regions (up to 40; the number is limited by computer memory);
- (3) for flexible age groups (e.g. 1 year or 5 year) and a variable highest age (e.g. 80+ or 90+);
- (4) for a projection interval equal to the age interval (generally 1 or 5 years); and
- (5) for regional projections that are consistent with exogeneously given national projections (optional).

The modelling strategy adopted was the fully multiregional model (section 2.5) in which the complete array of migration variables (migration disaggregated by 2 sexes, N regions of origin, N regions of destination and NA ages) was used.

The original intention (Willekens and Drewe 1981) was to base the projection model on earlier models developed at the International Institute for Applied Systems Analysis (IIASA) (Willekens and Rogers 1978, Willekens 1979, Ramchandran 1980). In the event, the MUDEA model incorporated substantial changes from the IIASA models.

(1) The model deals with two sexes using a female dominant fertility sub-model. That is, male births are a product of the proportion of births that are male multiplied by a set of fertility rates multiplied by a set of female populations at risk (Willekens and Drewe 1984, pp.329-330).

(2) The age-time plan for the input data was changed from ATP I (the period plan) to ATP II (period-cohort plan) because the focus of interest was projection rather than life table analysis. The original intention to

report on multiregional life expectancies was dropped, although Ledent and Rees (1980, 1986) have shown that such expectancies, at birth, can be generated directly from the projection model's survivorship rates and Rees (1986) has suggested that the whole life table could be estimated from ATP 11 data.

(3) The MUDEA model is clearly and unambiguously based on migration data of the movement type (as generated by the Dutch registration system), whereas the original IIASA models were ambiguous in their input requirements (because the issues involved were only resolved in the course of the associated project).

(4) The MUDEA model is clearly linked to an underlying set of population accounts of the movement variety, although the flow accounting equations are used rather than the full accounts based model.

(5) One consequence of this is that the MUDEA model fully and carefully incorporates international migration into its structure. Emigration flows are treated in the model in the same way as internal out-migration flows, namely as the product of migration rates transformed into period-cohort transition probabilities and the base population. Immigration flows are treated as exogenous inputs (which are subjected to survival, fertility and migration rates appropriate to their sojourn after immigration).

Thus, the MUDEA model meets the first four modelling requirements set out at the end of section three of the paper. There was a clear intention in the original specification of the project (Willekens and Drewe 1981) that the fifth requirement, that the user be able to "control" the projection by inputting a limited set of key parameters rather than a large body of age specific rates, be met, but this has yet to be accomplished. There is also the ambition (Willekens and Drewe 1981, ter Heide 1984) that the MUDEA model be linked with explanatory models of migration being developed under other RPD research contracts in a second phase. The goal has been partly achieved (Willekens 1986; Drewe 1986; Willekens and Drewe 1986). An analytical framework has been developed which can be used to integrate stability analysis (temporal stability of migration patterns) and explanatory analysis. Four components of migration are distinguished: a level component, a generation component, an attraction component and a spatial interaction component. The components can be studied and projected separately or simultaneously. The contribution of each component to the future migration pattern is determined by its contribution in the past (stability, inertia) and exogenous factors, such as policy measures, causing the value of a specific component to change.

How general is MUDEA (recalling the discussion of sections 2.4 and 2.5)? It is general in the sense that it can be used with any number of

regions (up to 40) and any number of ages, and can be employed in other countries where the same input information is available or can be estimated. In principle, the number of regions could be expanded given sufficient computer memory for the resulting arrays, but the flow and rate estimates would rapidly become unreliable because of the small number problem. The MUDEA model could not be directly used at the local level in the Netherlands (as ter Heide, 1984 recognizes). Another modelling strategy (partitioning, aggregation, parameterization or biregional modelling) would be required.

5.1.2 Inputs

Inputs required for the MUDEA model are:

- (1) the start of base year and end of base year populations by sex and age (e.g. 0,1,2, ..., 89,90+) for each region;
- (2) births in a year by age (of mother) by region;
- (3) births in a year by sex of child;
- (4) deaths in a year by age by region and sex;
- (5) internal migrations by age by origin, sex and destination;
- (6) emigrations by age by region and sex; and
- (7) immigrations by age by region and sex.

All age classifications for flows are of the period-cohort type. The migration data are all published by the Central Bureau of Statistics on this basis, but data on childbearing and mortality are published according to age at time of the event (period data). They were converted to period cohort form before being entered in the MUDEA model.

5.1.3 Outputs

Table 3 summarizes the considerable printed output that the MUDEA model produces for each period of analysis. Virtually all the model variables are printed out in full age detail (in most tables the row classification is by age). MUDEA tables 1 and 2 report the start of year populations, tables 3 through 6 report the components of growth (or accounting equation terms) in age detail, tables 8 and 9 report the rates that enter the matrix model, tables 10 to 15 report on internal migration numbers and tables 17 to 18 yield end of period populations. MUDEA tables 7 and 16 provide some summary information.

The outputs of the model are clearly voluminous. In a two region test run there were 169 pages of output for one period. The MUDEA program, however, contains parameters to control table printing (cf. MOVE, Rees 1984, in which the printing of virtually all tables can be suppressed). The presentation of the results of the multiregional model compares rather

unfavourably with that of the UN (Appendix). Time-oriented tables are essential for easy and fruitful use of projection outputs. Tables should be standard for each spatial unit across all spatial scales. The user should be able to suppress difficult to assimilate matrix style multiregional output (really needed only for error diagnosis) and concentrate on the essential results of the multiregional model. All these criticisms apply equally to MOVE.

5.2 The OPCS/DOE subnational population projection model for England

Between 1979 and 1981 a model was developed for the projection of the internal migration component of the official subnational population projections for England by Martin and Voorhees Associates and John Bates Services under contract to the Department of the Environment (DOE) of the United Kingdom in close liaison with the Regional Demography Unit of OPCS. Ian Bracken of the University of Wales Institute of Science and Technology (Cardiff) acted as consultant to the project. The model is fully described in Martin & Voorhees Associates and John Bates Services (1981), in associated programmer's guide and user's manual, and in two journal papers, Bates and Bracken (1982) and Bracken and Bates (1983). Results of using this new model are reported in the fifth of the series of subnational population projections for England (OPCS 1984). A new set of projections incorporating data from the 1981 Census as well as NHSCR data from the post-1981 period are in course of preparation.

5.2.1 The model

The model is concerned only with internal migration and is designed to supply a pre-existing single region cohort survival model with net migration values by sex and single years of age, values which can be modified in consultation with local authorities, but which were not changed much in the consultation exercise to judge from the comments in OPCS (1984, p.ix). DOE and OPCS were concerned to preserve their existing investment in a subnational projection model. One ironic benefit of using net migration in the projection model is that it doesn't matter whether the net figures are derived from transition or movement data as long as all transition types have been accounted for (Rees 1985).

Since the project brief required that single year of age populations for males, females and persons be projected for 108 local authority areas in England, a fully multiregional strategy was rejected from the outset because of the small number problem. Rather, an approach was developed which used trended gross migration rates, model generated rates of out-migration and in-migration (a "parameterized" strategy) and interregion allocation rates for three broad age groups only.

The model comprises three stages.

(1) The numbers of moves out of each area by age and sex are estimated by applying model migration rates to trended projections of the region-specific Gross Migration Rate (GMR).

(2) These moves are assigned to destinations using a matrix of allocation proportions based on NHSCR migration data for a 5 year period for three broad age groups and two sexes.

(3) The numbers of moves into each area are summed to obtain gross in-migration totals for each area, which are disaggregated by age using model migration rates (as in stage (1) for out-migrants).

It is useful in exposing the structure of the model in full to present it in general equation form (which the authors do not) as this will reveal a number of interesting features. All the variables in the model are disaggregated by sex, but, since the two populations are treated in the same way in the migration model, no notation for the sex classification is introduced in the description below.

(1) The total number of out-migrations

The total number of out-migrations from an area i by age a for a future period t is projected by

$$M_a^i(t) = (GMR_a^i(t) \cdot om_a^I(s)) \cdot P_a^i(t) \quad i \in I \quad (3)$$

where

$GMR_a^i(t)$ the gross migration rate of out-migration from area i in period t , which is a linear extrapolation of the GMR of the area for a standard period in the past.

$om_a^I(s)$ the proportion of the out-migration GMR accounted for by age group a . It is derived from model migration rates standardized to a GMR of 1 for area cluster I for standard period s .

$P_a^i(t)$ = population of region i at age a in period t .

The authors (Bates and Bracken 1982, Bracken and Bates, 1983) used migration data from the 1971 Census to calibrate model migration rate schedules for the 108 areas for males and females. A cluster analysis was then carried out to combine together similar profiles into 12 groups. New model schedules were then defined using the pooled data for the 12 groups.

(2) The assignment of out-migrations to destinations

The total of out-migrations from an area is spread across the available destinations by multiplication by an allocation proportion:

$$M_{ij}^A(t) = M_{i.}^A(t) k_{ij}^A(s) \quad (4)$$

where

$M_{ij}^A(t)$ = the number of moves from area i to area j in period t in broad age group A

$$M_{i.}^A(t) = \sum_{a \in A} M_{ia}^A(t)$$

$k_{ij}^A(s)$ = the proportion of origin i moves in broad age group A in standard period s that have destinations in area j .

In OPCS (1984) NHSCR data for mid-1977 to mid-1982, supplemented with 1971 census data where the spatial disaggregation of the NHSCR data was insufficient, were used. The broad age groups were

- (i) ages 0-16 and 29-59 (family ages)
- (ii) ages 17-28 (labour force ages)
- (iii) ages 60 and over (retirement ages).

The broad age groups were determined by the similarity of their origin-destination patterns.

(3) In-migration totals

The inter-area migrations by broad age group were summed and then disaggregated to single years of age:

$$M_a^{..J}(t) = \sum_A \sum_j M_{aj}^A(t) \quad (5)$$

where

$M_a^{..J}(t)$ total number of in-migrations to area j in period t in age group a

j
 $i_m(s)$ the proportion of the in-migration GMR accounted for
 a by age group a . The proportions are derived from
 model migration rates standardized to a GMR of 1
 for area cluster J for standard period s .

(4) Net migration

This is then derived as a residual:

$$\begin{matrix} j \\ N(t) \\ a \end{matrix} = \begin{matrix} \cdot j \\ M(t) \\ a \end{matrix} - \begin{matrix} j \cdot \\ M(t) \\ a \end{matrix} \quad (6)$$

and fed into the single region cohort survival model. Methods were also developed to adjust the migration matrices resulting at stage (2) of the model to exogeneous in-migration totals.

5.2.2 Comments on the OPCS/DOE model

The OPCS/DOE model represents an elegant and thoroughly tested solution to the problem of projecting the internal flows of a large number of subnational areal units, carried out by the consultants in a remarkably short period of 18 months.

However, a number of further comments can be made based on this algebraic reformulation of the model.

Firstly, it is unfortunate that the migration model is decoupled from the population projection model. This means that the indicators of the components of change offered in the projection model output are very limited. Secondly, it would be very easy to carry out this integration and make the combined migration and projection model fully multiregional by merging equations (3) and (4):

$$\begin{matrix} ij \\ M(t) \\ a \end{matrix} = \begin{matrix} i \\ GMR(t) \end{matrix} \begin{matrix} I \\ om(s) \end{matrix} \begin{matrix} ij \\ k(s) \\ A \end{matrix} \begin{matrix} i \\ P(t) \\ a \end{matrix} \quad i \in I, a \in A \quad (7)$$

or in other words the migration rate would be modelled as

$$\begin{matrix} ij \\ m(t) \\ a \end{matrix} = \begin{matrix} i \\ GMR(t) \end{matrix} \begin{matrix} I \\ om(s) \end{matrix} \begin{matrix} ij \\ k(s) \\ A \end{matrix} \quad (8)$$

where s refers to the standard or base period (which may differ between variables). Stage (3) of the model is then unnecessary. Constraints on

ij
 M (t) can easily be introduced using multiproportional fitting
 a
 techniques, generalizations of the Furness method referred to by Martin & Voorhees Associates and John Bates Services (1981).

When we examine the terms on the right hand side of equation (7), it can be seen that the only statistic that is projected forward in time is the GMR. There is no reason why the age factor and the allocation proportion could not also be projected forward given reliable time series, so a more general model would substitute period label t for the standard or base period label s in equations (7) and (8).

A third point to make about the OPCS/DOE model is that, in exposition, it suffers from a lack of clarity as to age-time plan of observation. The subscript a should refer to a period-cohort ATP throughout. However, the NHSCR data are published using the period ATP and Census migration data are collected using the period-cohort ATP. It is also unclear what populations at risk are being used in rate computation: initial, mid-point, average or final populations.

A related fourth point refers to migration concept being used. Both Census and NHSCR data are used (and have to be used) in the model but it is never made clear which conceptual type of migration (movements or transitions) is being estimated and projected. In the exposition above it is assumed that the model works with the movement concept. OPCS 1984, p.viii states that "the level of migration activity" derives from NHSCR data, whereas in the project report (Martin & Voorhees Associates and John Bates Services 1981) the GMRs reported are from census data. This conceptual ambiguity arises from the aim of the model being to generate age disaggregated net migration vectors for areas.

Fifthly, we need to consider the roles of aggregation and sub-model representation in the overall model. The interarea allocation terms, the k's, involve aggregation of actual migration data into a few broad age groups. The alternative of using gravity models of such interarea migration was rejected after investigation because the predicted matrices were felt to be insufficiently accurate. The out-migration factors or om's, involve both aggregation over area cluster and model representation of rates. A great deal of detailed work is involved in the calibration of model migration schedules and their classification though it needs only to be carried out in the British context every ten years. In other situations the use of pooled, observed data to generate standard rates might provide a short cut since the key features of the out-migration rate schedules that vary from area to area (Bracken and Bates, 1983, p.353), namely presence/absence of a retirement peak and/or slope, the age at which the labour force migration peak occurs and the extent to which migration activity is concentrated around the peak could be determined by

simpler methods.

How general is the OPCS/DOE model (recalling again the discussion of sections 2.4 and 2.5)? It is clearly a very specific model in terms of its implementation and exposition, designed for one set of clients (DOE/OPCS) with particular requirements in terms of area populations to be projected. It is also specific in the sense that the aggregation decisions (pooling of out-migration and in-migration profiles by cluster, use of particular broad age bands in allocating out-migration) are peculiar to the system being studied. It is doubtful whether the underlying software would be portable, and the mixture of census and register sources of migration data characteristic of the United Kingdom seems to be repeated only in Japan (Nanjo, Kawashima and Kuroda 1982). However, the methods employed to solve the problem of handling many regions simultaneously are of general utility and could be applied in other contexts.

5.2.3 Outputs

Table 4 summarizes the readily available outputs from the subnational projections. Further detailed data are available from OPCS's Regional Demography Unit. Output tables 1 to 4 appear in OPCS (1984); tables 5 and 6 are the standard detailed projection tables provided on request.

A good feature of these outputs is their time orientation, although the published tables are woefully inadequate in the number of future time points for which data are provided - only two! For any serious use of these projections the user needs to obtain the detailed single years of age and time outputs from the Regional Demography Unit. Output tables 3 and 4 provide some idea of the components in number form but not in rate form. Summary indicators such as GMRS or total fertility rates or life expectancies are not provided.

As with the MUDEA model, the outputs of the OPCS/DOE model are not as well organized and accessible as those of the United Nations' projections (Appendix).

6. CONCLUSIONS

The purpose of this review has been to look critically at these two new applications of multiregional methods in order to learn from the experience. Here an attempt is made to summarize what has been learnt.

The theoretical base and mathematical specification of the Dutch MUDEA model are very sound. The projection model is carefully matched with the movement type of migration data used in a period-cohort age-time plan. The English OPCS/DOE model is not as well specified as one set of

equations, and there is a lack of clarity concerning both the migration concept aimed at in the model and the age-time plans employed. However, it has the merit of making fruitful use of both census and register derived migration data, using the former to overcome deficiencies in the latter.

The Dutch MUDEA model is a multiregional model that handles all migration flows in age-sex-origin-destination specificity with a considerable degree of flexibility. So, for example, projections of the 11 provinces or of 15 functional regions or 41 urbanization regions could be carried out. The English OPCS/DOE model involves modelling of pooled profiles of out- and in-migration at a detailed age scale and an age pooled method of assigning out-migration to destinations. It is designed to prepare the migration projections for 108 areas and is capable of handling the other subnational areas of the United Kingdom outside England as well either separately or together with those of England.

Whereas the Dutch model is easily portable to other demographic systems for which the same kinds of data are available, it is difficult to envisage the English model being directly used because of some system specific features. These are the need to arrive at a classification of in- and out-migration profiles and a pooling of the age specific interarea migration matrices into broad age ranges with common interaction features. The classes and age ranges will vary from situation to situation. Nevertheless the ideas behind the English model could well be applied elsewhere because it provides a solution to the problem of using multiregional models with a large number of regions.

In terms of user requirements both models provide the essential projections by single year of age and sex of the populations of subnational units, controlled by sets of time-varying assumptions as to levels of fertility, mortality and migration, and thus represent considerable advances on previous models and software. The organization and presentation of the results of both models, however, fall short of the ideal. The MUDEA model provides voluminous outputs on a single year of age basis for both inputs and results, and it is difficult for users to find the essential statistics amid the haystack of paper. Output tables are provided a year at a time, whereas most users find tabulations of statistics across time points or intervals much easier to contemplate and from which trends can be grasped more easily. A time orientation is employed in the presentation of the results of the English area projections, but the published volume provides very little information at the level of detail on the key statistics input to each time interval. Users must purchase detailed unpublished tabulations and tapes. The outputs of both Dutch and English models contrast unfavourably with the projection statistics published by the UN (Appendix) for countries of the world. Such a volume and associated tapes, with appropriate modifications, for the subnational areas of the Netherlands and the United

Kingdom would be a very valuable planning and research resource.

These efforts in the application of multiregional methods to official subnational population projection represent considerable pioneering achievements. There is ample room, however, for improvement in the "packaging" of both models and outputs: the field awaits its Alan Sugar (the boss of the Amstrad company, who repackaged consumer electronics, word processors and business machines and made a fortune).

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Table 1. Transition accounts and associated rates for Great Britain, 1966-71, age transition 20-24 to 25-29, persons.

Final state Initial state	Survival in: Aged 25-29			Death in: Aged 20-24 or 25-29			Totals
	EA	SE	RB	RW	EA	SE	RW
East	79,620	7,578	8,141	5,296	334	13	10
Anglia (EA)	(.78826)	(.07502)	(.08060)	[.05243]			
South	14,408	984,059	79,740	101,985	26	3,691	175
East (SE)	(.01217)	(.83111)	(.06735)	[.08596]			
Rest of	9,440	84,510	2,074,448	107,473	18	145	208
Britain (RB)	(.00413)	(.03700)	(.90813)	[.04703]			
Rest of	7,790	88,045	70,123	0	14	149	0
World (RW)	(.07712)	(.07436)	(.03070)				
Totals	111,258	1,164,192	2,232,452	214,554	392	3,998	393
					<.00369>	<.00341>	<.00370>

Source: Rees (1979b)

(.78826) internal survivorship rates [.05243] emigration rates

(.07712) immigration rates <.00370> non-survivorship rates or death rates

Table 2. Movement accounts and associated rates for the Netherlands, 1976, age transition 20 to 21, females.

Final state Initial state	State after move				Totals
	WN	RN	RW	Deaths	
West Netherlands (WN)	49,121	1,375 (.02682)	402 [.00784]	17 (.00033)	50,915
Rest of the Netherlands (RN)	1,739 (.02821)	59,595	437 [.00709]	23 (.00037)	61,794
Rest of world (RW)	759 (.01480)	546 (.00886)	0 -	0 -	1,305
Totals	51,619	61,516	839	40	114,014

Notes

1. West Netherlands consists of the provinces of Noord-Holland, Zuid-Holland and Utrecht. The Rest of the Netherlands contains the remaining 8 provinces and IJsselmeerpolder.

2. Rates:-

(0.2682) internal movement rates

[.00784] emigration rates

(.01480) immigration rates

All rates employ an average population at risk.

TABLE 3. Summary of the output tables produced by NUDEA

TABLE	VARIABLES	FORM	MACRO-CLASS	ROW-CLASS	COLUMN-CLASS
1.	population (initial)	numbers percentages	Sex	Age (1)	region
2.	population (initial)	numbers percentages	Sex	Age (5)	region
3.	person/years, births, deaths, interregional migration, external migration	numbers percentages	Sex by region	Age (1)	components (as under variables)
4.	person years, births, deaths interregional migration, external migration	numbers percentages	Sex by region	Age (5)	components (as under variables)
5.	components as in 4 (except person years)	age specific rates per 1000	Sex by region	Age (1)	components (as under variables)
6.	components as in 5	age specific rates per 1000	Sex by region	Age (5)	components (as under variables)
7.	components (summarized)	numbers, percentages years rates per 1000 mid-year population		sex by region	components
8.	birth rates	age-specific rates	Sex by origin region	Age (1)	destination region
9.	survivorship rates	age-specific rates (decimal proportions)	Sex by origin region	Age (1)	destination region
10.	internal migration	numbers	Sex by origin region	Age (1)	destination region
11.	internal migration	numbers	Sex by origin region	Age (5)	destination region
12.	internal migration	percentages	Sex by origin region	Age (1)	destination region
13.	internal migration	percentages	Sex by origin region	Age (5)	destination region
14.	internal migration	rate per 1000 (out-migration)	Sex by origin region	Age (1)	destination region
15.	internal migration	rate per 1000 (out-migration)	Sex by origin region	Age (5)	destination region
16.	internal migration (summarised)	numbers, percentages, rates	Sex	form by origin region	destination region
17.	population (final)	numbers, percentages	Sex	Age (1)	residence region
18.	population (final)	numbers, percentages	Sex	Age (5)	residence region

Notes to Table 3

1. Percentages = age-specific variable as % of all age total
2. Table 8: the column class in the NUDEA output is incorrectly labelled as "birth region": it is the region of destination of the infant
3. Table 10 includes migration between localities within regions which do not figure in the NUDEA model as such
4. Age (1) = single years of age age (5) = 5 year age groups

TABLE 4 Summary of the output tables produced by the OPCS/DOE model

TABLE	VARIABLES	MACRO-CLASS	ROW-CLASS	COLUMN CLASS
1	populations (mid-year projected)	England regions	age (5) ages (summary)	time by sex
2	populations (mid-year projected)	Areas (see note 3)	time by sex	ages (summary
3	natural components (births, deaths natural change)		Areas (see note 3)	components (as variables), two summary time periods
4	projected in- out and net migration		Areas (as in 3)	migration components (as variables) two summary time periods
5	populations (mid-year projected)	Areas (as in 3)	age (1)	time (years) by sex
6	populations (mid-year projected)	Areas (as in 3)	age (5)	time (years) by sex

Notes

Tables 1 to 4 appear in OPCS (1984) and report on population projections from 1981 to 2001.

Tables 5 and 6 are examples of unpublished tabulations obtained from the Regional Demography Unit (Dept. ARV), Office of Population Censuses and Surveys St. Catherine's House, 10 Kingsway, London WC2B 6JP. Populations to 2011 are provided

Areas: Table 2: Inner London boroughs, Outer London boroughs, Metropolitan Counties and Districts, Non-Metropolitan Counties

Table 3: England, standard regions, and Table 2 areas

ANNUAL		POPULATION										MIGRATION										DEMOGRAPHIC INDICATORS																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																					
		1977		1978		1979		1980		1981		1982		1983		1984		1985		1986		1987		1988		1989		1990		1991		1992		1993		1994		1995		1996		1997		1998		1999		2000		2001		2002		2003		2004		2005		2006		2007		2008		2009		2010		2011		2012		2013		2014		2015		2016		2017		2018		2019		2020		2021		2022		2023		2024		2025		2026		2027		2028		2029		2030		2031		2032		2033		2034		2035		2036		2037		2038		2039		2040		2041		2042		2043		2044		2045		2046		2047		2048		2049		2050		2051		2052		2053		2054		2055		2056		2057		2058		2059		2060		2061		2062		2063		2064		2065		2066		2067		2068		2069		2070		2071		2072		2073		2074		2075		2076		2077		2078		2079		2080		2081		2082		2083		2084		2085		2086		2087		2088		2089		2090		2091		2092		2093		2094		2095		2096		2097		2098		2099		2100		2101		2102		2103		2104		2105		2106		2107		2108		2109		2110		2111		2112		2113		2114		2115		2116		2117		2118		2119		2120		2121		2122		2123		2124		2125		2126		2127		2128		2129		2130		2131		2132		2133		2134		2135		2136		2137		2138		2139		2140		2141		2142		2143		2144		2145		2146		2147		2148		2149		2150		2151		2152		2153		2154		2155		2156		2157		2158		2159		2160		2161		2162		2163		2164		2165		2166		2167		2168		2169		2170		2171		2172		2173		2174		2175		2176		2177		2178		2179		2180		2181		2182		2183		2184		2185		2186		2187		2188		2189		2190		2191		2192		2193		2194		2195		2196		2197		2198		2199		2200		2201		2202		2203		2204		2205		2206		2207		2208		2209		2210		2211		2212		2213		2214		2215		2216		2217		2218		2219		2220		2221		2222		2223		2224		2225		2226		2227		2228		2229		2230		2231		2232		2233		2234		2235		2236		2237		2238		2239		2240		2241		2242		2243		2244		2245		2246		2247		2248		2249		2250		2251		2252		2253		2254		2255		2256		2257		2258		2259		2260		2261		2262		2263		2264		2265		2266		2267		2268		2269		2270		2271		2272		2273		2274		2275		2276		2277		2278		2279		2280		2281		2282		2283		2284		2285	

TABLE A.1 Demographic indicators, Netherlands (from UN, 1985)

NETHERLANDS

POPULATION (IN THOUSANDS) BY SEX AND AGE, MEDIUM VARIANT

AGE GROUP	1 9 5 0			1 9 5 5			1 9 6 0			1 9 6 5		
	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	18114	10411	19773	16741	9356	9385	15469	9717	5753	12292	6133	6159
0-4	12892	6390	5897	11110	5700	5410	11394	5711	5683	12115	6222	5893
5-9	9382	4730	4652	11066	6099	5967	11006	5660	5346	11510	5900	5610
10-14	885	421	464	911	430	481	1093	607	486	1107	560	547
15-19	811	416	395	817	416	401	913	467	446	1123	606	517
20-24	800	404	396	760	401	359	806	400	396	912	440	474
25-29	796	394	402	761	383	378	771	390	381	896	417	479
30-34	699	361	338	713	360	353	766	376	390	774	373	401
35-39	683	325	358	673	333	340	765	373	390	757	373	384
40-44	606	317	289	676	323	353	667	329	338	761	375	386
45-49	593	290	303	637	310	327	663	321	342	760	375	385
50-54	520	252	268	570	261	309	625	303	322	690	316	374
55-59	440	218	222	503	242	261	561	270	291	663	315	348
60-64	376	183	193	424	204	220	473	223	250	549	277	271
65-69	305	146	157	363	165	198	387	182	205	431	198	233
70-74	231	111	120	259	124	135	293	138	155	331	151	180
75-79	165	80	85	173	82	91	196	91	105	224	104	120
80+	102	50	52	127	58	69	150	72	78	169	80	89

AGE GROUP	1 9 7 0			1 9 7 5			1 9 8 0			1 9 8 5		
	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	13937	6964	6973	13744	6954	6790	14220	7047	7173	14596	7211	7385
0-4	1168	608	560	1038	531	507	1075	644	431	1027	623	404
5-9	1216	623	593	1213	622	592	1067	525	542	1070	601	469
10-14	1191	591	600	1242	636	606	1226	637	589	1092	537	555
15-19	1130	569	561	1104	604	500	1232	643	589	1131	610	521
20-24	1189	606	576	1142	583	559	1195	608	585	1250	641	609
25-29	1077	547	530	1122	567	555	1150	587	563	1196	609	587
30-34	913	427	486	926	467	459	1010	473	537	1061	545	516
35-39	779	397	372	825	429	397	930	499	431	1020	629	391
40-44	706	359	347	762	392	370	828	429	399	936	507	429
45-49	754	360	394	753	373	379	700	376	324	876	426	450
50-54	604	317	287	765	361	404	766	364	402	771	389	382
55-59	563	267	296	631	316	315	729	349	380	761	389	372
60-64	469	246	223	594	274	320	605	294	311	690	325	365
65-69	367	177	190	520	216	304	550	246	304	600	286	314
70-74	366	160	206	420	173	246	433	190	244	460	206	254
75-79	254	109	145	293	120	163	330	129	201	396	161	235
80+	225	96	129	276	106	170	297	111	186	336	119	216

AGE GROUP	2 0 0 0			2 0 0 5			2 0 1 0			2 0 1 5		
	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	14726	7310	7417	14695	7400	7295	15011	7494	7517	15025	7496	7529
0-4	873	422	451	814	416	397	797	400	397	766	383	383
5-9	820	423	397	826	422	404	815	417	398	796	400	396
10-14	800	411	389	820	424	396	820	423	397	816	413	399
15-19	1096	550	546	1082	532	550	1031	476	555	1081	523	558
20-24	1232	629	603	1095	530	565	1083	532	551	1032	484	548
25-29	1297	640	657	1133	606	527	1096	573	523	1072	502	570
30-34	1196	600	596	1237	640	597	1233	620	613	1094	537	557
35-39	1139	584	555	1196	606	590	1237	629	608	1233	626	607
40-44	1117	626	491	1131	594	537	1193	604	589	1236	636	600
45-49	920	427	493	1210	619	590	1144	566	578	1187	599	588
50-54	813	417	396	920	473	447	1195	600	595	1121	561	560
55-59	731	375	357	794	422	372	1076	537	539	1167	587	580
60-64	676	335	341	720	352	368	761	378	383	801	430	371
65-69	607	296	311	640	299	341	660	317	343	707	363	344
70-74	400	213	187	567	246	321	569	251	318	588	286	302
75-79	290	132	158	387	177	210	452	186	266	486	186	300
80+	272	120	152	406	180	226	431	187	244	468	187	281

AGE GROUP	2 0 2 0			2 0 2 5			2 0 3 0			2 0 3 5		
	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	14972	7412	7560	14608	7366	7242	14766	7264	7502	14609	7162	7447
0-4	719	366	353	721	369	352	760	369	391	766	366	399
5-9	769	383	386	716	366	350	732	370	361	761	360	371
10-14	799	381	418	750	386	364	717	363	354	713	378	335
15-19	810	387	423	801	409	392	751	384	367	716	367	351
20-24	836	423	413	816	417	399	801	400	397	752	384	368
25-29	826	424	402	810	416	394	819	417	401	801	409	392
30-34	866	431	435	823	426	397	830	422	408	814	417	397
35-39	1096	536	560	904	431	473	893	423	470	880	422	458
40-44	1230	626	604	1076	530	546	1032	602	530	1032	610	422
45-49	1066	538	528	1223	619	604	1090	590	500	1070	600	470
50-54	1176	576	600	1256	620	636	1212	609	603	1206	622	584
55-59	1107	590	517	1160	570	590	1209	601	508	1106	591	517
60-64	1121	556	565	1065	519	546	1107	599	508	1166	569	597
65-69	902	509	393	1047	501	546	976	523	453	1017	600	417
70-74	626	300	326	710	329	381	696	425	271	877	401	476
75-79	472	201	271	583	210	373	574	209	364	756	326	430
80+	311	179	132	560	192	368	576	209	366	680	326	354

APPENDIX

TABLE A.2 Population (in 1000s) by age and sex, medium variant (from UN, 1985), Netherlands

INDICATOR	POPULATION										MIGRATION									
	1950	1955	1960	1965	1970	1975	1980	1985	1990	1995	2000	2005	2010	2015	2020	2025	2030	2035	2040	2045
POPULATION BY SEX																				
Total (in 1,000,000)	50,100	52,500	55,000	57,500	60,000	62,500	65,000	67,500	70,000	72,500	75,000	77,500	80,000	82,500	85,000	87,500	90,000	92,500	95,000	97,500
Male (in 1,000,000)	24,500	25,500	26,500	27,500	28,500	29,500	30,500	31,500	32,500	33,500	34,500	35,500	36,500	37,500	38,500	39,500	40,500	41,500	42,500	43,500
Female (in 1,000,000)	25,600	27,000	28,500	30,000	31,500	33,000	34,500	36,000	37,500	39,000	41,000	42,000	43,500	45,000	46,500	48,000	49,500	51,000	52,500	54,000
Sex ratio (per 1,000 males)	106.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5	105.5
POPULATION BY AGE GROUP																				
Age 0-14 (in 1,000,000)	11,000	10,500	10,000	9,500	9,000	8,500	8,000	7,500	7,000	6,500	6,000	5,500	5,000	4,500	4,000	3,500	3,000	2,500	2,000	1,500
Age 15-64 (in 1,000,000)	28,000	28,500	29,000	29,500	30,000	30,500	31,000	31,500	32,000	32,500	33,000	33,500	34,000	34,500	35,000	35,500	36,000	36,500	37,000	37,500
Age 65+ (in 1,000,000)	11,100	13,500	16,000	18,500	21,500	24,500	27,500	30,500	33,500	36,500	39,500	42,500	45,500	48,500	51,500	54,500	57,500	60,500	63,500	66,500
Age 0-14 (% of total)	22.0	20.0	18.2	16.5	15.0	13.8	12.5	11.3	10.1	9.0	8.0	7.1	6.2	5.4	4.7	4.0	3.3	2.6	2.0	1.5
Age 15-64 (% of total)	55.9	54.3	52.7	51.3	50.0	48.8	47.7	46.5	45.3	44.2	43.1	42.0	41.0	40.0	39.0	38.0	37.0	36.0	35.0	34.0
Age 65+ (% of total)	22.1	25.7	29.1	32.2	35.2	37.7	40.8	43.8	46.9	50.0	52.9	55.9	58.6	61.2	64.0	66.5	69.0	71.4	73.9	76.5
AGE INDICATORS																				
Median age	28.0	28.5	29.0	29.5	30.0	30.5	31.0	31.5	32.0	32.5	33.0	33.5	34.0	34.5	35.0	35.5	36.0	36.5	37.0	37.5
Life expectancy at birth	72.0	73.0	74.0	75.0	76.0	77.0	78.0	79.0	80.0	81.0	82.0	83.0	84.0	85.0	86.0	87.0	88.0	89.0	90.0	91.0
Life expectancy at age 65	78.0	79.0	80.0	81.0	82.0	83.0	84.0	85.0	86.0	87.0	88.0	89.0	90.0	91.0	92.0	93.0	94.0	95.0	96.0	97.0
Life expectancy at age 75	82.0	83.0	84.0	85.0	86.0	87.0	88.0	89.0	90.0	91.0	92.0	93.0	94.0	95.0	96.0	97.0	98.0	99.0	100.0	101.0
SPECIAL AGE GROUPS																				
Age 0-14 (in 1,000,000)	11,000	10,500	10,000	9,500	9,000	8,500	8,000	7,500	7,000	6,500	6,000	5,500	5,000	4,500	4,000	3,500	3,000	2,500	2,000	1,500
Age 15-64 (in 1,000,000)	28,000	28,500	29,000	29,500	30,000	30,500	31,000	31,500	32,000	32,500	33,000	33,500	34,000	34,500	35,000	35,500	36,000	36,500	37,000	37,500
Age 65+ (in 1,000,000)	11,100	13,500	16,000	18,500	21,500	24,500	27,500	30,500	33,500	36,500	39,500	42,500	45,500	48,500	51,500	54,500	57,500	60,500	63,500	66,500
Age 0-14 (% of total)	22.0	20.0	18.2	16.5	15.0	13.8	12.5	11.3	10.1	9.0	8.0	7.1	6.2	5.4	4.7	4.0	3.3	2.6	2.0	1.5
Age 15-64 (% of total)	55.9	54.3	52.7	51.3	50.0	48.8	47.7	46.5	45.3	44.2	43.1	42.0	41.0	40.0	39.0	38.0	37.0	36.0	35.0	34.0
Age 65+ (% of total)	22.1	25.7	29.1	32.2	35.2	37.7	40.8	43.8	46.9	50.0	52.9	55.9	58.6	61.2	64.0	66.5	69.0	71.4	73.9	76.5
DEMOGRAPHIC INDICATORS																				
Total fertility rate	2.10	2.00	1.90	1.80	1.70	1.60	1.50	1.40	1.30	1.20	1.10	1.00	0.90	0.80	0.70	0.60	0.50	0.40	0.30	0.20
Gross reproduction rate	1.05	1.00	0.95	0.90	0.85	0.80	0.75	0.70	0.65	0.60	0.55	0.50	0.45	0.40	0.35	0.30	0.25	0.20	0.15	0.10
Net reproduction rate	0.90	0.85	0.80	0.75	0.70	0.65	0.60	0.55	0.50	0.45	0.40	0.35	0.30	0.25	0.20	0.15	0.10	0.05	0.00	-0.05
Crude birth rate	12.0	11.5	11.0	10.5	10.0	9.5	9.0	8.5	8.0	7.5	7.0	6.5	6.0	5.5	5.0	4.5	4.0	3.5	3.0	2.5
Crude death rate	10.0	9.5	9.0	8.5	8.0	7.5	7.0	6.5	6.0	5.5	5.0	4.5	4.0	3.5	3.0	2.5	2.0	1.5	1.0	0.5
Net migration	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00	1.05
DEMOGRAPHIC INDICATORS																				
Total fertility rate	2.10	2.00	1.90	1.80	1.70	1.60	1.50	1.40	1.30	1.20	1.10	1.00	0.90	0.80	0.70	0.60	0.50	0.40	0.30	0.20
Gross reproduction rate	1.05	1.00	0.95	0.90	0.85	0.80	0.75	0.70	0.65	0.60	0.55	0.50	0.45	0.40	0.35	0.30	0.25	0.20	0.15	0.10
Net reproduction rate	0.90	0.85	0.80	0.75	0.70	0.65	0.60	0.55	0.50	0.45	0.40	0.35	0.30	0.25	0.20	0.15	0.10	0.05	0.00	-0.05
Crude birth rate	12.0	11.5	11.0	10.5	10.0	9.5	9.0	8.5	8.0	7.5	7.0	6.5	6.0	5.5	5.0	4.5	4.0	3.5	3.0	2.5
Crude death rate	10.0	9.5	9.0	8.5	8.0	7.5	7.0	6.5	6.0	5.5	5.0	4.5	4.0	3.5	3.0	2.5	2.0	1.5	1.0	0.5
Net migration	0.10	0.15	0.20	0.25	0.30	0.35	0.40	0.45	0.50	0.55	0.60	0.65	0.70	0.75	0.80	0.85	0.90	0.95	1.00	1.05

APPENDIX

TABLE A.3 Demographic indicators, United Kingdom (from UN, 1985)

U.K., G.A., BRITAIN & N.I., IRELAND

AGE GROUP	1 9 5 0			2 0 0 5			2 0 5 0			2 1 0 5		
	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	26656	24173	26641	31190	28726	32472	32599	29490	37199	36520	26536	28004
0-4	4367	2225	2122	2894	1479	1415	4330	2134	2224	4136	2460	2236
5-9	2411	1043	1370	4280	2103	2000	3066	1499	1617	4114	2100	2000
10-14	2346	1702	1644	2330	1823	1507	4263	2120	2043	3791	1940	1895
15-19	2316	1675	1641	2312	1640	1672	3999	1824	1761	4257	2171	2086
20-24	2567	1801	1766	3294	1834	1460	3609	1785	1820	3441	1807	1634
25-29	2679	1752	1926	3441	1730	1711	3303	1672	1631	3632	1767	1869
30-34	2791	1791	1999	3613	1895	1718	3600	1716	1711	4247	1711	2536
35-39	3291	1936	1951	3369	1667	1702	3773	1672	1901	3427	1721	1695
40-44	3087	1904	1904	3794	1676	1718	3704	1647	1704	3647	1676	1676
45-49	2562	1722	1833	3721	1840	1881	3716	1622	1894	3400	1625	1675
50-54	2162	1642	1622	3467	1679	1792	3619	1622	1856	3406	1747	1659
55-59	1761	1264	1501	2949	1363	1586	3192	1268	1702	3092	1609	1483
60-64	1425	1070	1347	2534	1095	1439	2722	1230	1510	2626	1406	1220
65-69	1017	704	1163	2000	880	1121	2221	911	1269	2301	994	1307
70-74	1592	676	914	1667	676	991	1729	676	1064	1809	694	1115
75-79	1032	426	606	1129	441	686	1191	456	753	1250	446	810
80+	766	276	470	860	304	556	1003	326	677	1106	344	766

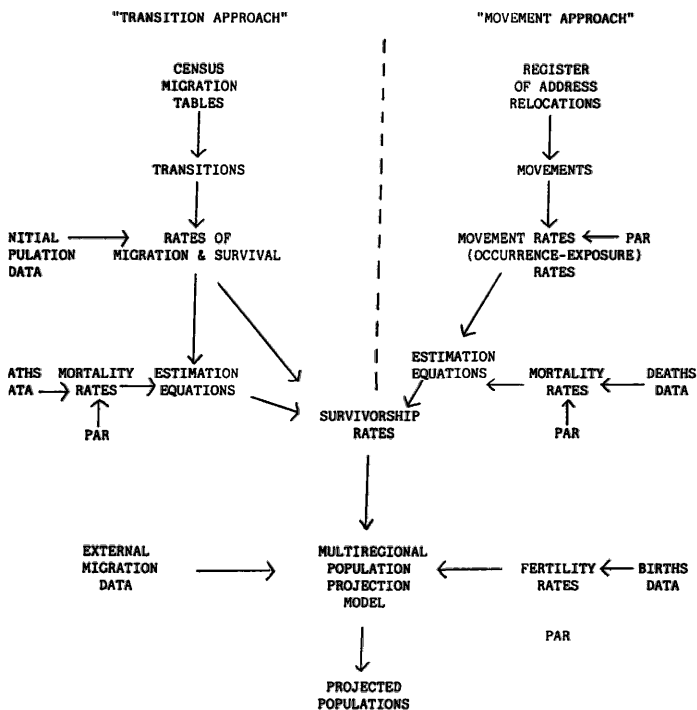
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	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	26656	24173	26641	31190	28726	32472	32599	29490	37199	36520	26536	28004
0-4	4367	2225	2122	2894	1479	1415	3600	1766	1832	3422	1767	1655
5-9	4699	2409	2290	4494	2309	2185	3903	2008	1895	3362	1827	1535
10-14	2366	1724	1642	2306	1642	1664	4662	2211	2172	3696	2004	1696
15-19	2602	1951	1651	2645	2375	2270	4616	2246	2162	4122	2109	2010
20-24	4779	2165	2100	3676	1922	1900	4442	2126	2016	4422	2266	2256
25-29	4791	2679	2112	3704	1927	1777	3603	1736	1869	4462	2096	2366
30-34	3294	1694	1600	3676	1760	1711	4102	2000	2062	3729	1662	1667
35-39	3197	1993	1902	3232	1653	1600	3606	1710	1666	4095	1631	2026
40-44	3009	1690	1919	3647	1692	1955	3600	1615	1573	3640	1607	1637
45-49	2509	1736	1770	3292	1637	1655	3000	1549	1527	3126	1676	1659
50-54	2266	1592	1676	2531	1722	1809	3177	1503	1612	3000	1609	1609
55-59	1826	1403	1423	2607	1406	1501	2621	1321	1401	2646	1367	1279
60-64	1372	1043	1300	2170	1000	1170	2700	1311	1387	2126	1009	1099
65-69	1162	816	1146	1621	766	855	2100	1100	1100	2161	1100	1061
70-74	1694	766	928	2212	879	1333	1641	766	1074	2266	776	1399
75-79	1276	460	816	1666	666	999	1666	566	1100	1766	676	1117
80+	1276	361	914	1626	379	955	1666	462	1067	1501	344	1033

AGE GROUP	1 9 5 0			2 0 0 5			2 0 5 0			2 1 0 5		
	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	26656	24173	26641	31190	28726	32472	32599	29490	37199	36520	26536	28004
0-4	4620	1653	1766	3646	1666	1780	3566	1617	1726	3266	1712	1552
5-9	4696	1677	1649	3566	1623	1741	3610	1647	1726	3504	1721	1781
10-14	2366	1724	1642	2306	1642	1664	3576	1631	1743	3600	1609	1673
15-19	2602	2054	1548	2645	1795	1650	3507	1712	1616	3640	1627	1774
20-24	4779	2165	2100	3676	1922	1900	4442	2126	2016	4422	2266	2256
25-29	4791	2679	2112	3704	1927	1777	3603	1736	1869	4462	2096	2366
30-34	3294	1694	1600	3676	1760	1711	4102	2000	2062	3729	1662	1667
35-39	3197	1993	1902	3232	1653	1600	3606	1710	1666	4095	1631	2026
40-44	3009	1690	1919	3647	1692	1955	3600	1615	1573	3640	1607	1637
45-49	2509	1736	1770	3292	1637	1655	3000	1549	1527	3126	1676	1659
50-54	2266	1592	1676	2531	1722	1809	3177	1503	1612	3000	1609	1609
55-59	1826	1403	1423	2607	1406	1501	2621	1321	1401	2646	1367	1279
60-64	1372	1043	1300	2170	1000	1170	2700	1311	1387	2126	1009	1099
65-69	1162	816	1146	1621	766	855	2100	1100	1100	2161	1100	1061
70-74	1694	766	928	2212	879	1333	1641	766	1074	2266	776	1399
75-79	1276	460	816	1666	666	999	1666	566	1100	1766	676	1117
80+	1276	361	914	1626	379	955	1666	462	1067	1501	344	1033

AGE GROUP	2 0 0 5			2 0 1 5			2 0 2 0			2 0 3 0		
	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES	BOTH SEXES	MALES	FEMALES
ALL AGES	26656	24173	26641	31190	28726	32472	32599	29490	37199	36520	26536	28004
0-4	3900	1696	1615	3409	1706	1703	3522	1606	1716	3596	1616	1720
5-9	3910	1699	1611	3476	1679	1799	3570	1725	1849	3667	1616	1781
10-14	3606	1791	1615	3300	1600	1700	3523	1673	1850	3660	1623	1717
15-19	3666	1676	1790	3597	1622	1775	3561	1723	1840	3327	1709	1622
20-24	3650	1666	1784	3677	1601	1776	3591	1626	1766	3370	1729	1640
25-29	3677	1721	1956	3706	1630	1776	3629	1696	1791	3623	1661	1711
30-34	3816	1696	1620	3609	1720	1879	3510	1662	1726	3566	1617	1749
35-39	3615	1661	1954	3671	1678	1693	3577	1716	1861	3621	1676	1723
40-44	3607	1699	1908	3706	1627	1879	3590	1696	1802	3393	1696	1696
45-49	3600	1712	1788	3600	1710	1890	3590	1699	1912	3627	1662	1765
50-54	3616	1696	1920	3616	1696	1920	3616	1696	1920	3616	1696	1920
55-59	3606	1696	1710	3729	1663	1866	3606	1696	1710	3606	1696	1710
60-64	3601	1696	1901	3600	1662	1738	3600	1696	1710	3601	1696	1710
65-69	3709	1717	1992	3616	1696	1920	3616	1696	1920	3616	1696	1920
70-74	3601	1696	1901	3600	1662	1738	3600	1696	1710	3601	1696	1710
75-79	3601	1696	1901	3600	1662	1738	3600	1696	1710	3601	1696	1710
80+	3601	1696	1901	3600	1662	1738	3600	1696	1710	3601	1696	1710

APPENDIX

TABLE A.4 Population (in 1000's) by age and sex, medium variant (From UN, 1985), United Kingdom



KEY

PAR . POPULATION AT RISK (MID-INTERVAL OR AVERAGE POPULATION)

FIGURE 1 The steps in the incorporation of migration data in regional population projections

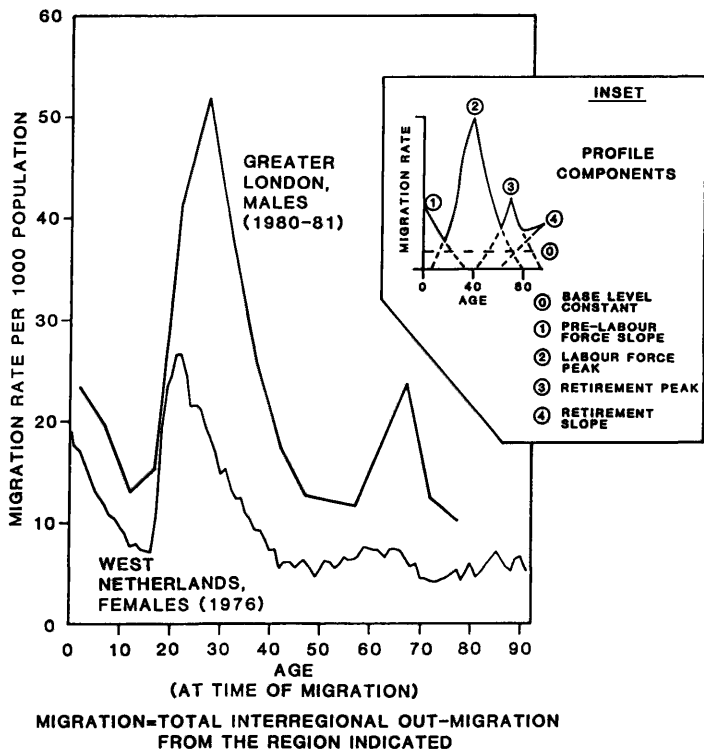


FIGURE 2. Examples of migration rate profiles

52

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