- A process that suspects it is deadlocked, initiates a (Lai-Yang) snapshot to compute the wait-for graph.
- Each node u takes a local snapshot of:
  - requests it sent or received that weren't yet granted or dismissed;
  - and grant and dismiss messages in edges.
- Then it computes:
  - Out, : the nodes it sent a request to (not granted)
  - In<sub>...</sub>: the nodes it received a request from (not dismissed)
  - Requests, : the number of grants u requires to become unblocked.

Initially notified u = false and  $free_u = false$  at all nodes u.

The initiator starts a deadlock detection run by executing Notify.

Notify<sub>u</sub>: 
$$notified_u \leftarrow true$$
  
for all  $w \in Out_u$  send NOTIFY to  $w$   
if  $requests_u = 0$  then  $Grant_u$   
for all  $w \in Out_u$  await DONE from  $w$ 

Grant<sub>u</sub>: 
$$free_u \leftarrow true$$
  
for all  $w \in In_u$  send GRANT to  $w$   
for all  $w \in In_u$  await ACK from  $w$ 

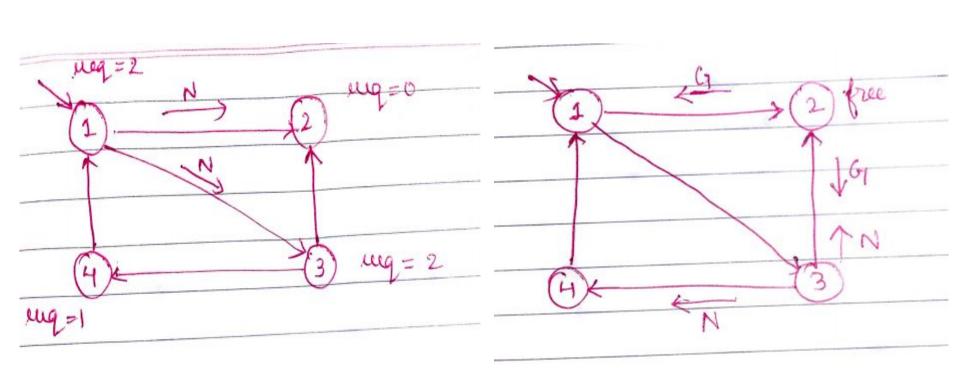
While a node is awaiting DONE or ACK messages, it can also process incoming NOTIFY and GRANT messages.

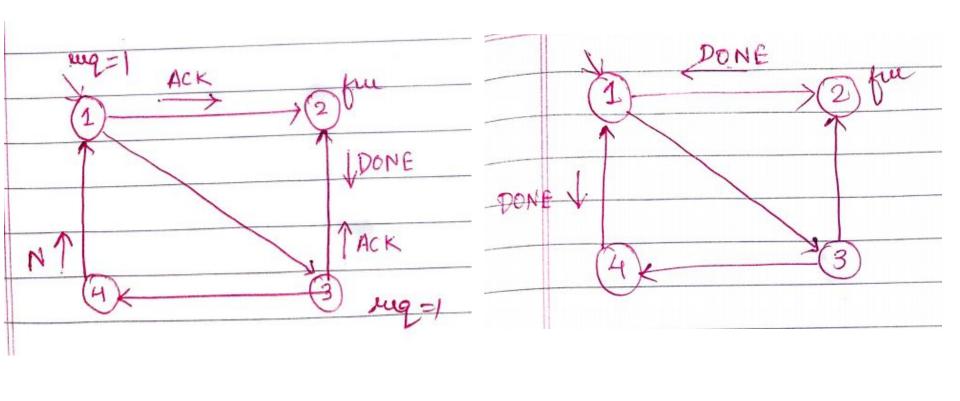
Let u receive NOTIFY. If  $notified_u = false$ , then u executes  $Notify_u$ . u sends back DONE.

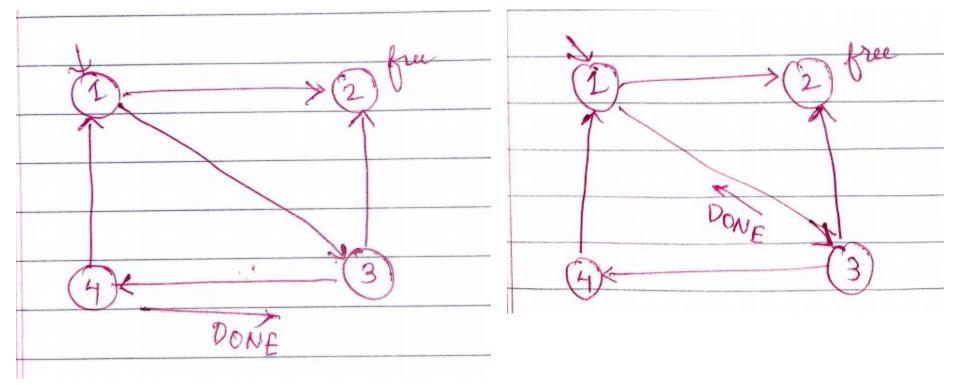
Let u receive GRANT. If  $requests_u > 0$ , then  $requests_u \leftarrow requests_u - 1$ ; if  $requests_u$  becomes 0, then u executes  $Grant_u$ . u sends back ACK.

When the initiator has received DONE from all nodes in its *Out* set, it checks the value of its *free* field.

If it is still false, the initiator concludes it is deadlocked.







The Bracha-Toueg algorithm is deadlock-free:

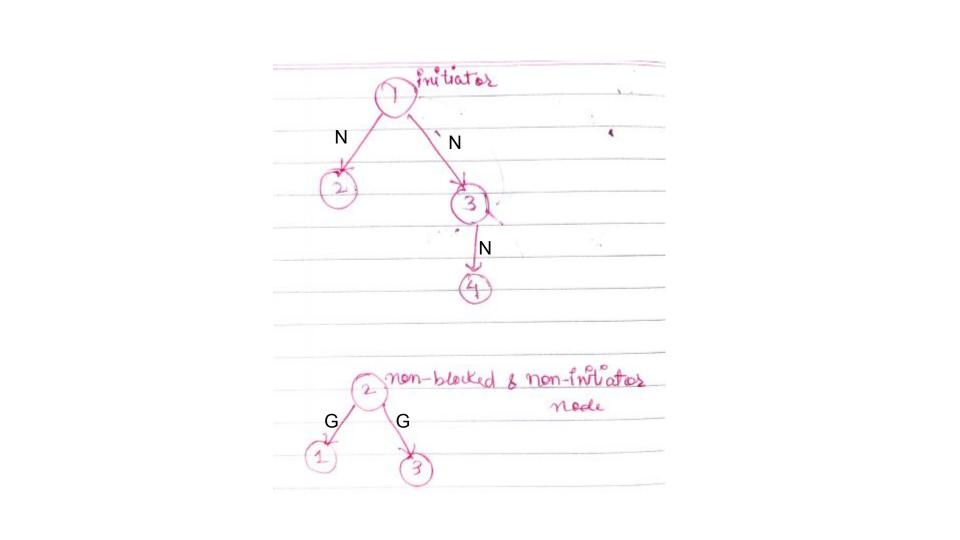
The initiator eventually receives DONE's from all nodes in its Out set.

At that moment the Bracha-Toueg algorithm has terminated.

Two types of trees are constructed, similar to the echo algorithm:

- 1. NOTIFY/DONE's construct a tree T rooted in the initiator.
- 2. GRANT/ACK's construct disjoint trees  $T_v$ , rooted in a node v where from the start  $requests_v = 0$ .

The NOTIFY/DONE's only complete when all GRANT/ACK's have completed.



## Time Complexity Analysis

- Message Complexity: 4 messages per node,
  <notify>,<grant>,<done>,<ack>.
- Time complexity: 2d hops, where d = diameter of the WFG.
  - One diameter to send <notify>/<grant> to the farthest node in the graph.
  - Another diameter to receive <done>/<ack> from the same.