

5. Transformers

Generative Algorithms for Sound and Music



Universitat
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MTG
Music Technology
Group



**NEW,
SHINY AI MODEL**

**ANY AI
MUSIC ENGINEER**

**60+ YEARS
OF SOLID
TECHNIQUES**

Transformer Battle



Organize 4 teams

- Guinea pigs
- Dogs
- Cats
- Hamsters

Rules of engagement

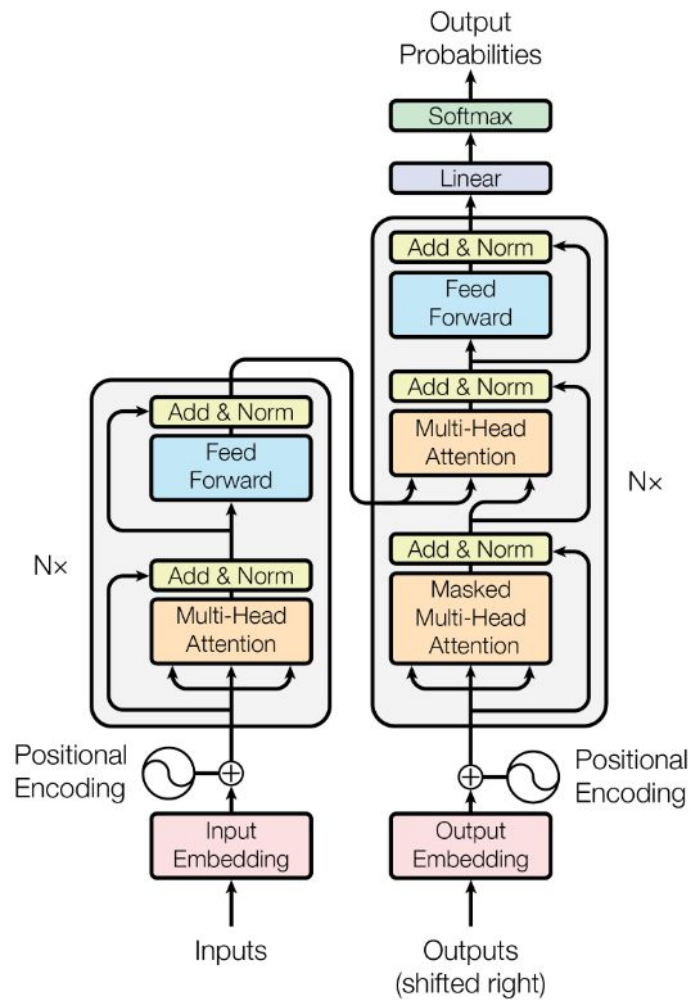
- Good explanation = +2
- Tough question = +4
- Wrong answer / explanation = -1
- If you can't answer, another group will jump in

Tough question





Real-time scores



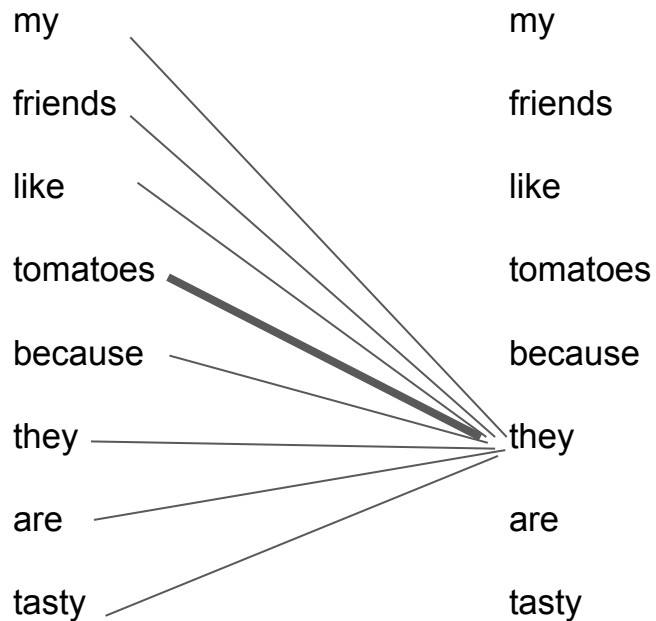
A reference problem

My friends like tomatoes because they are tasty

A reference problem

My friends like tomatoes because **they** are tasty

Self-attention: Intuition



What matrices do we have in self-attention?

Query, key, value matrices

Query (Q)

I	1.3	0.8
like	0.7	3.5
cats	1.9	0.1

Key (K)

I	0.6	2.4
like	0.8	1.7
cats	2.5	0.3

Value (V)

I	0.4	1.0
like	1.2	2.8
cats	1.7	0.2

How do we derive Q, K, V?

How do we derive Q, K, V?

- Multiply input matrix by 3 weight matrices
- Learn weights during training

$$IW_Q = Q$$

$$IW_K = K$$

$$IW_V = V$$

Why not use fixed K
instead of learnable
per head?

Self-attention: Formalisation

Self-attention: Formalisation

$$Z(Q, K, V) = \text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) V$$

Self-attention: Step 1

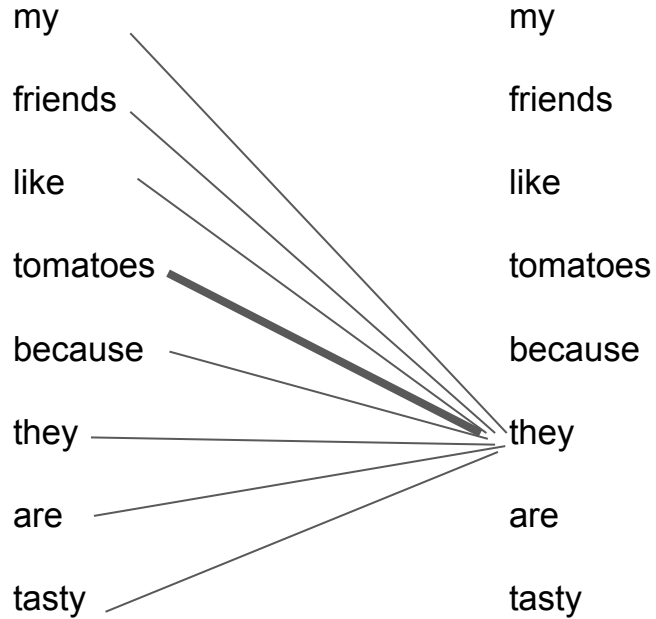
$$Z(Q, K, V) = \text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) V$$

Self-attention: Step 1

$$QK^T = \begin{matrix} & \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} & \begin{bmatrix} 1.3 & 0.8 \\ 0.7 & 3.5 \\ 1.9 & 0.1 \end{bmatrix} & \begin{matrix} q_1 \\ q_2 \\ q_3 \end{matrix} \end{matrix} \begin{matrix} \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} & \begin{matrix} k_1 \\ k_2 \\ k_3 \end{matrix} \\ \begin{matrix} \text{I} & \text{like} & \text{cats} \end{matrix} & \begin{bmatrix} 0.6 & 0.8 & 2.5 \\ 2.4 & 1.7 & 0.3 \end{bmatrix} \end{matrix} = \begin{bmatrix} q_1 k_1 & q_1 k_2 & q_1 k_3 \\ q_2 k_1 & q_2 k_2 & q_2 k_3 \\ q_3 k_1 & q_3 k_2 & q_3 k_3 \end{bmatrix} = \begin{matrix} & \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} & \begin{bmatrix} 2.7 & 2.4 & 3.49 \\ 8.82 & 6.51 & 2.8 \\ 1.38 & 1.69 & 4.78 \end{bmatrix} \end{matrix}$$

Q K^T

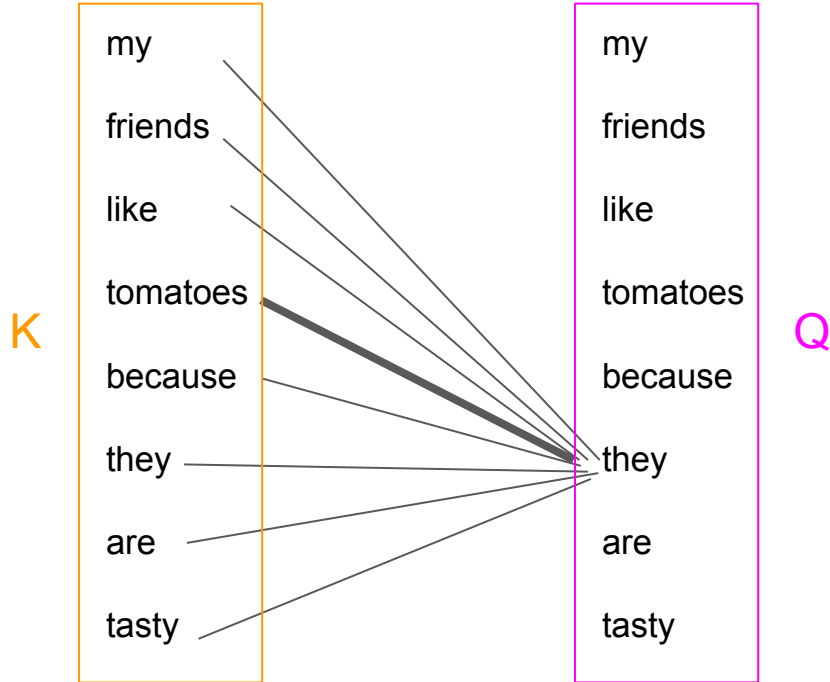
Which ones are Q and K really?



Self-attention: Step 2

$$Z(Q, K, V) = \text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) V$$

What are Q and K really?



Why Q and K are
separate matrices?

What happens if $Q = K$?

Self-attention: Step 3

$$Z(Q, K, V) = \text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) V$$

Self-attention: Step 3

- Normalize similarity scores
- Apply *softmax*
- Each word vector (row) adds up to 1 (probability)

$$\text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) = \begin{matrix} & \text{I} & \text{like} & \text{cats} \\ \text{I} & 0.7 & 0.2 & 0.1 \\ \text{like} & 0.2 & 0.6 & 0.2 \\ \text{cats} & 0.4 & 0.1 & 0.5 \end{matrix}$$

*values in the matrix completely made up

Self-attention: Step 3

$$\text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right)$$

Self-attention: Step 3

$$\text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right)$$

Attention score

Relevance of different parts of the sequence to each other

Self-attention: Step 4

$$Z(Q, K, V) = \text{softmax} \left(\frac{QK^T}{\sqrt{d_k}} \right) V$$

Self-attention: Step 4

$$Z = \begin{matrix} & \text{I} & \text{like} & \text{cats} \\ \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} & \begin{bmatrix} 0.7 & 0.2 & 0.1 \\ 0.2 & 0.6 & 0.2 \\ 0.4 & 0.1 & 0.5 \end{bmatrix} \end{matrix} \quad \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} \begin{bmatrix} 0.4 & 1.0 \\ 1.2 & 2.8 \\ 1.7 & 0.2 \end{bmatrix} \begin{matrix} \mathbf{v}_1 \\ \mathbf{v}_2 \\ \mathbf{v}_3 \end{matrix} = \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} \begin{bmatrix} 0.69 & 1.28 \\ 1.14 & 1.92 \\ 1.13 & 0.78 \end{bmatrix} = \begin{bmatrix} \vec{z}_1 \\ \vec{z}_2 \\ \vec{z}_3 \end{bmatrix}$$

$\text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)$ V

Self-attention for word “I”

$$Z = \begin{matrix} & \text{I} & \text{like} & \text{cats} \\ \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} & \begin{bmatrix} 0.7 & 0.2 & 0.1 \\ 0.2 & 0.6 & 0.2 \\ 0.4 & 0.1 & 0.5 \end{bmatrix} \end{matrix} \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} \begin{bmatrix} 0.4 & 1.0 \\ 1.2 & 2.8 \\ 1.7 & 0.2 \end{bmatrix} \begin{matrix} \vec{v}_1 \\ \vec{v}_2 \\ \vec{v}_3 \end{matrix} = \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} \begin{bmatrix} 0.69 & 1.28 \\ 1.14 & 1.92 \\ 1.13 & 0.78 \end{bmatrix} = \begin{bmatrix} \vec{z}_1 \\ \vec{z}_2 \\ \vec{z}_3 \end{bmatrix}$$

$\text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right) \quad V$

$$\vec{z}_1 = 0.7\vec{v}_1 + 0.2\vec{v}_2 + 0.1\vec{v}_3 = 0.7 \begin{bmatrix} 0.4 & 1.0 \end{bmatrix} + 0.2 \begin{bmatrix} 1.2 & 2.8 \end{bmatrix} + 0.1 \begin{bmatrix} 1.7 & 0.2 \end{bmatrix}$$

I like cats I like cats

Sum of the value vectors weighted by the scores

A reference problem: Solved

My friends like tomatoes because they are tasty

$$\vec{z}_{they} = 0.0\vec{v}_1 + 0.0\vec{v}_2 + 0.0\vec{v}_3 + 0.9\vec{v}_4 + 0.0\vec{v}_5 + 0.1\vec{v}_6 + 0.0\vec{v}_7 + 0.0\vec{v}_8$$

my friends like tomatoes because they are tasty

Why not use K for V?

Analogy: Search engine

Q = ?

K = ?

V = ?

Attention scores = ?

Result = ? x ?

What's multi-head attention?

What's multi-head attention?

- Run multiple instances of the self-attention mechanism in parallel
- Compute as many Q, K, V, Z matrices as the number of heads

$$Z = \text{concatenate}(Z_1, Z_2, Z_3, \dots, Z_n)W_0$$

What does
concatenation **really**
mean mathematically?

$$Z = \text{concatenate}(Z_1, Z_2, Z_3, \dots, Z_n)W_0$$

WHY MULTIPLE HEADS?



Why do we multiply
concatenated Z by
 W_0 ?

$$Z = \text{concatenate}(Z_1, Z_2, Z_3, \dots, Z_n)W_0$$

Positional encoding: Strategy

$$I' = \underbrace{\begin{bmatrix} 0.2 & 1.2 \\ 0.5 & 4.1 \\ 2.1 & 0.4 \end{bmatrix}}_I + \underbrace{\begin{bmatrix} 0.5 & 1.0 \\ 2.5 & 1.3 \\ 1.1 & 0.3 \end{bmatrix}}_P = \begin{bmatrix} 0.7 & 2.2 \\ 3.0 & 5.4 \\ 3.2 & 0.7 \end{bmatrix}$$

Why transformer
doesn't know about
order?

How do we compute P ?

How do we compute P?

$$P(pos, 2i) = \sin \left(\frac{pos}{10000^{2i/dimension_{model}}} \right)$$

$$P(pos, 2i + 1) = \cos \left(\frac{pos}{10000^{2i/dimension_{model}}} \right)$$

Why sinusoidal?

How's the position
encoded, for real?

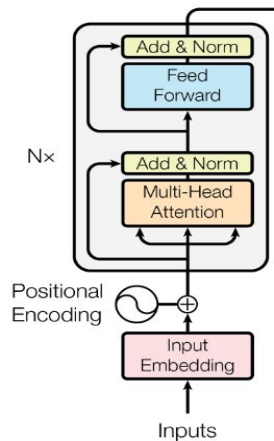
How do we compute P?

$$P(pos, 2i) = \sin\left(\frac{pos}{10000^{2i/dimension_{model}}}\right)$$

$$P(pos, 2i + 1) = \cos\left(\frac{pos}{10000^{2i/dimension_{model}}}\right)$$

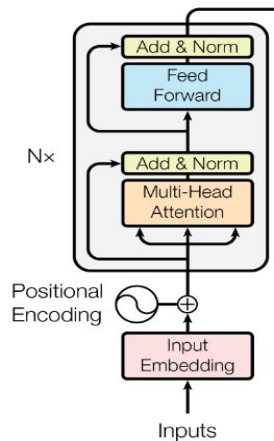
$$P = \begin{matrix} \text{Spaghetti} \\ \text{monster} \\ \text{is} \\ \text{great} \end{matrix} \begin{bmatrix} \sin\left(\frac{0}{10000^{2.0/3}}\right) & \cos\left(\frac{0}{10000^{2.1/2}}\right) & \sin\left(\frac{0}{10000^{2.2/3}}\right) \\ \sin\left(\frac{1}{10000^{2.0/3}}\right) & \cos\left(\frac{1}{10000^{2.1/2}}\right) & \sin\left(\frac{1}{10000^{2.2/3}}\right) \\ \sin\left(\frac{2}{10000^{2.0/3}}\right) & \cos\left(\frac{2}{10000^{2.1/2}}\right) & \sin\left(\frac{2}{10000^{2.2/3}}\right) \\ \sin\left(\frac{3}{10000^{2.0/3}}\right) & \cos\left(\frac{3}{10000^{2.1/2}}\right) & \sin\left(\frac{3}{10000^{2.2/3}}\right) \end{bmatrix}$$

Other components missing from encoder?



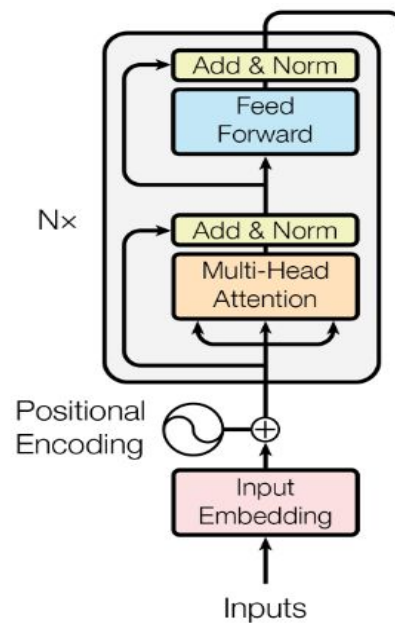
Other components missing from encoder?

- Feed-forward
- Add & Norm

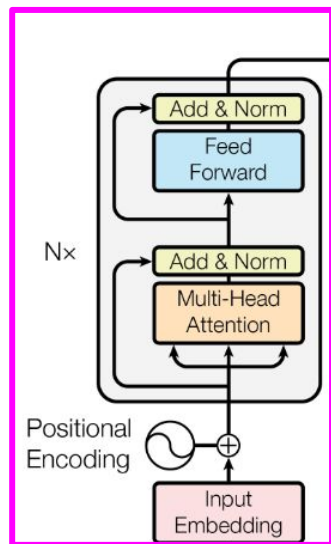


Why feedforward?

How do Add and Norm
work for real?

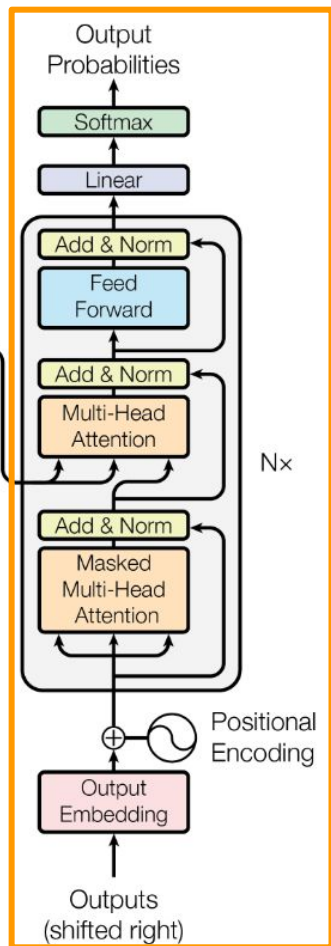


Encoder



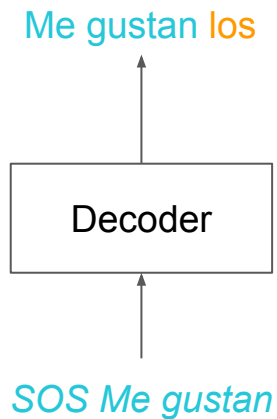
Inputs

Decoder

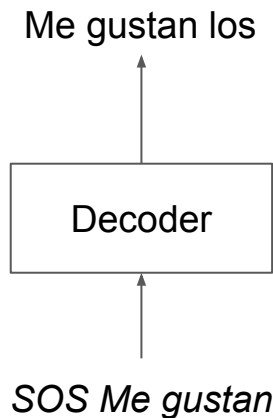


Outputs
(shifted right)

Training / inference discrepancy



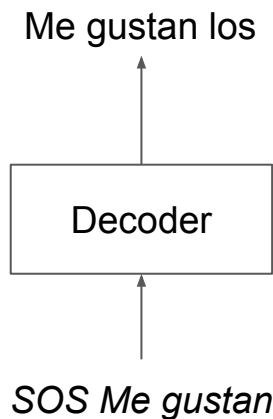
Training / inference discrepancy



What decoder knows during inference

SOS me gustan

Training / inference discrepancy



What decoder knows during inference

SOS me gustan

What decoder knows during training

SOS me gustan los gatos

Masked multi-head attention

$$Z_i(Q_i, K_i, V_i) = \text{softmax} \left(\frac{Q_i K_i^T}{\sqrt{d_k}} \right) V_i$$

Masked multi-head attention

$$\frac{Q_i K_i^T}{\sqrt{d_k}} =$$

	SOS	me	gustan	los	gatos
SOS	1.3	0.8	1.3	2.8	2.3
me	2.4	2.8	2.3	6.8	1.9
gustan	1.6	7.4	1.6	0.3	0.5
los	2.1	1.2	9.3	5.2	0.2
gatos	4.3	3.8	6.3	1.8	2.3

Masked multi-head attention

$$\frac{Q_i K_i^T}{\sqrt{d_k}} =$$

	SOS	me	gustan	los	gatos
SOS	1.3	0.8	1.3	2.8	2.3
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Masked multi-head attention

$$\frac{Q_i K_i^T}{\sqrt{d_k}} =$$

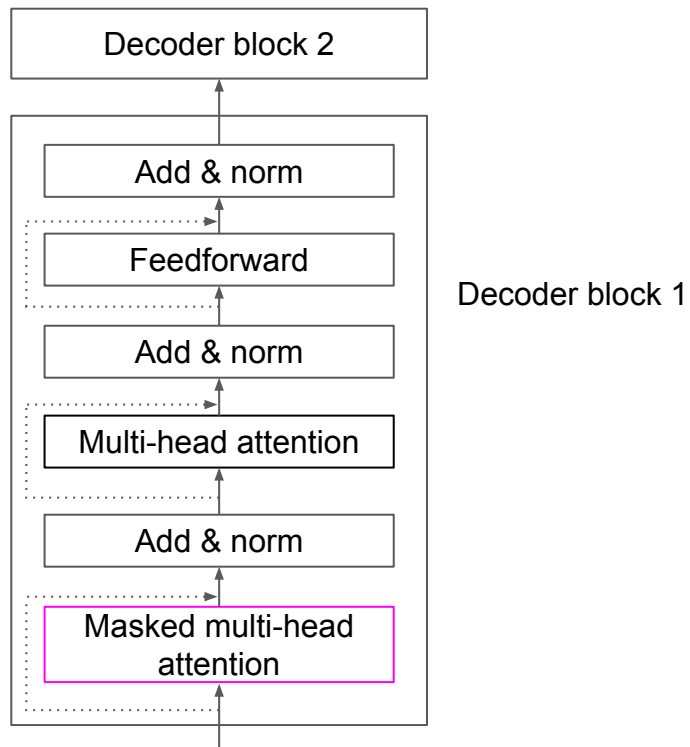
	SOS	me	gustan	los	gatos
SOS	1.3	0.8	1.3	2.8	2.3
me	2.4	2.8	2.3	6.8	1.9
gustan	1.6	7.4	1.6	0.3	0.5
los	2.1	1.2	9.3	5.2	0.2
gatos	4.3	3.8	6.3	1.8	2.3

Masked multi-head attention

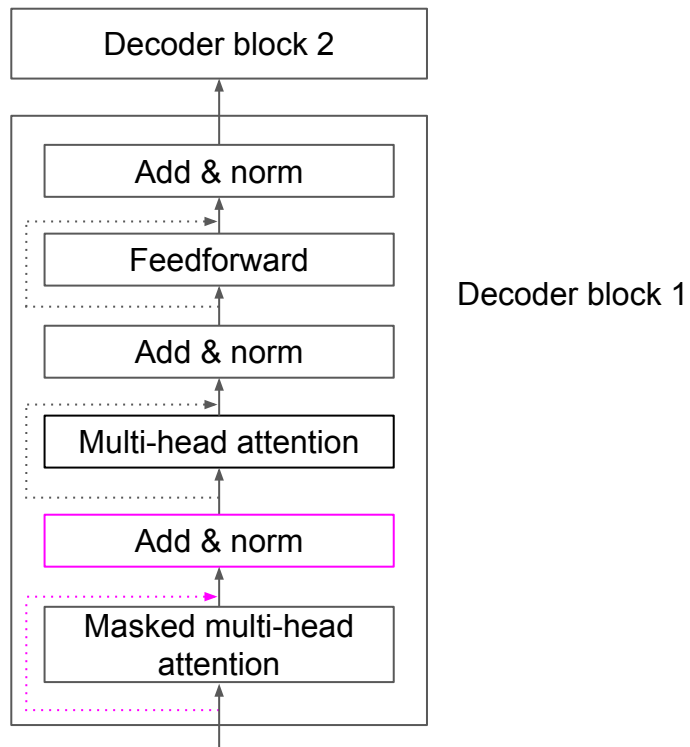
$$\frac{Q_i K_i^T}{\sqrt{d_k}} = \begin{array}{c} \text{SOS} \\ \text{me} \\ \text{gustan} \\ \text{los} \\ \text{gatos} \end{array} \begin{array}{ccccc} \text{SOS} & \text{me} & \text{gustan} & \text{los} & \text{gatos} \\ \left[\begin{array}{ccccc} 1.3 & -\infty & -\infty & -\infty & -\infty \\ 2.4 & 2.8 & -\infty & -\infty & -\infty \\ 1.6 & 7.4 & 1.6 & -\infty & -\infty \\ 2.1 & 1.2 & 9.3 & 5.2 & -\infty \\ 4.3 & 3.8 & 6.3 & 1.8 & 2.3 \end{array} \right] \end{array}$$

What does *softmax* spit
when it encounters the
-infinity mask?

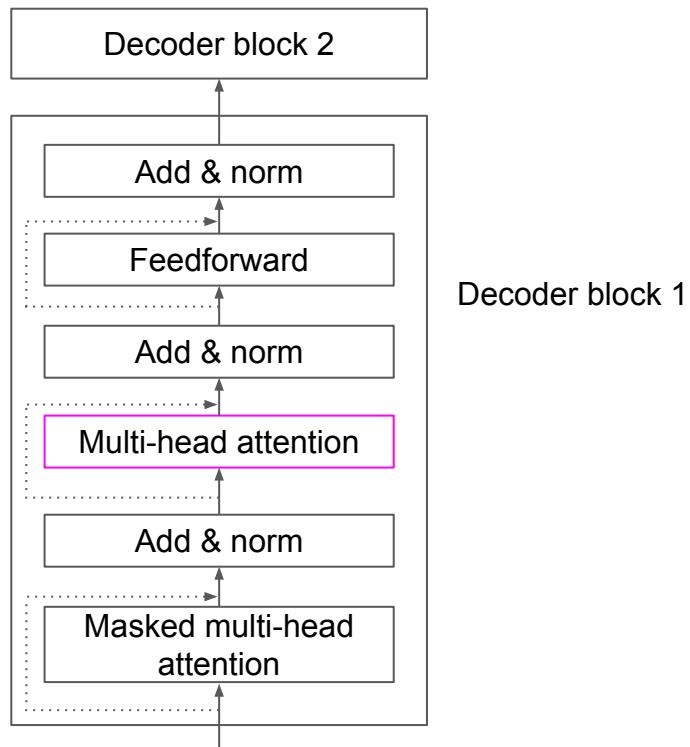
Decoder block



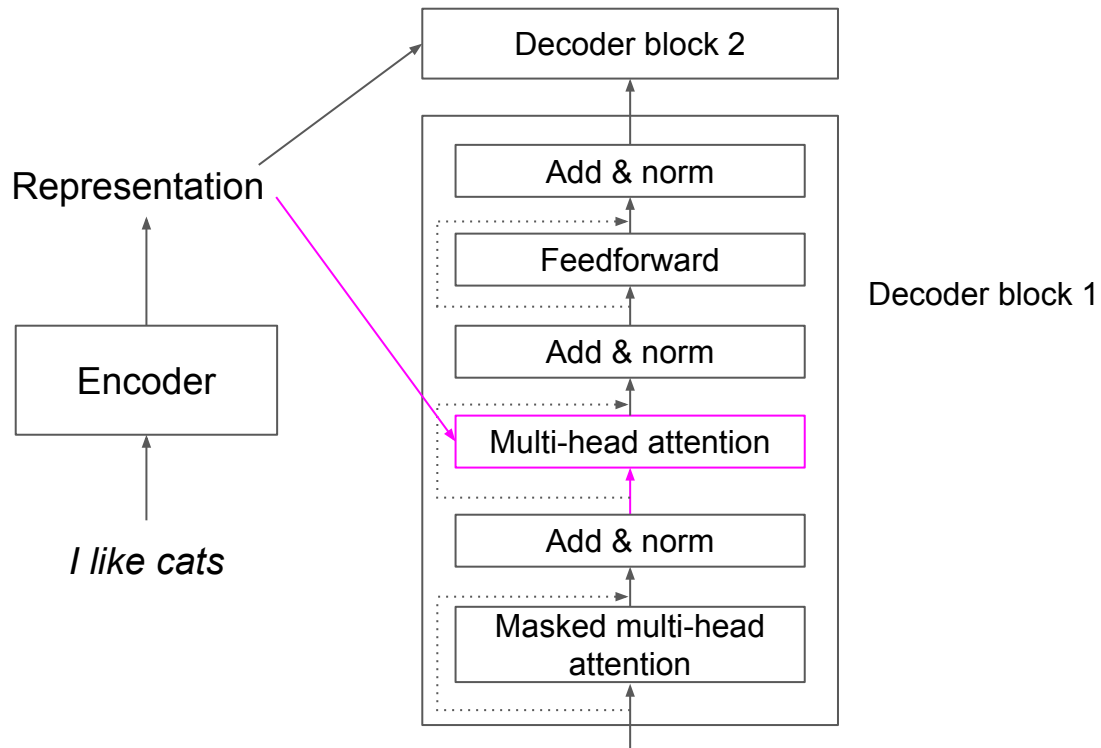
Decoder block



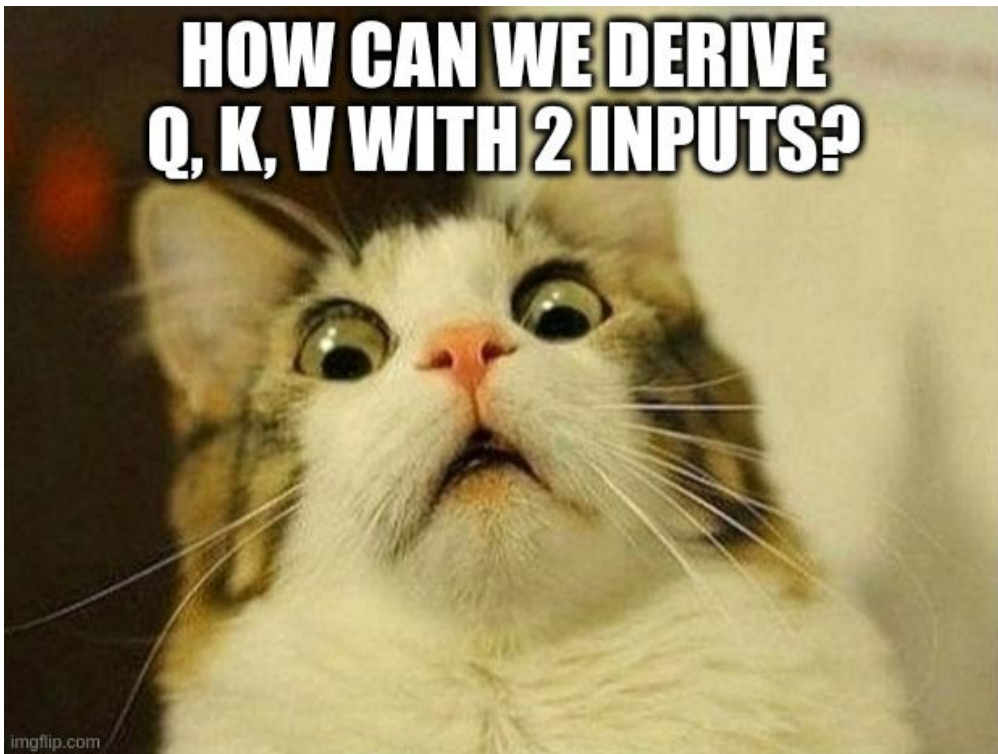
Decoder block



Decoder block



**HOW CAN WE DERIVE
Q, K, V WITH 2 INPUTS?**



Deriving Q, K, V

- Query matrix (Q) from masked attention input
- Key (K) and value (V) matrices from encoder representation

$$MW_Q = Q$$

$$RW_K = K$$

$$RW_V = V$$

Deriving Q, K, V

- Q holds representation of target sentence
- K, V hold representation of source sentence

Why do we derive Q
from target, and K, V
from source?

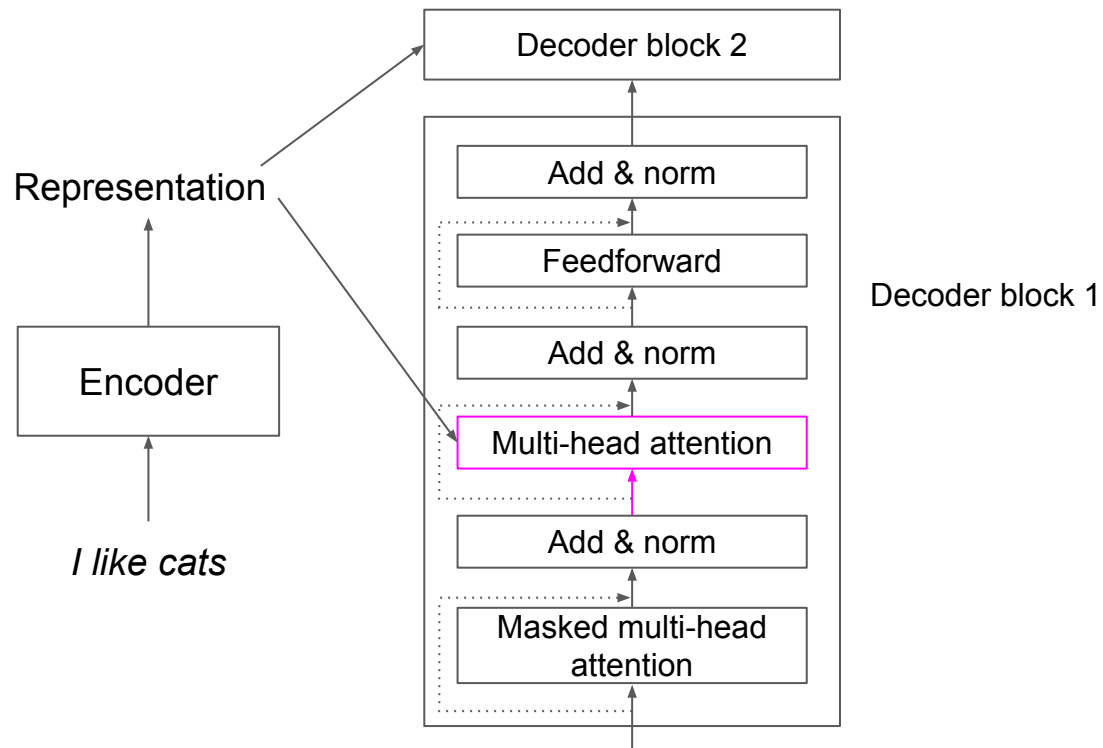
Deriving attention matrix

$$Z = \begin{matrix} & \text{I} & \text{like} & \text{cats} \\ \text{SOS} & \begin{bmatrix} 0.7 & 0.2 & 0.1 \end{bmatrix} \\ \text{me} & \begin{bmatrix} 0.6 & 0.3 & 0.1 \end{bmatrix} \\ \text{gustan} & \begin{bmatrix} 0.1 & 0.8 & 0.1 \end{bmatrix} \\ \text{los} & \begin{bmatrix} 0.1 & 0.3 & 0.6 \end{bmatrix} \\ \text{gatos} & \begin{bmatrix} 0.1 & 0.1 & 0.8 \end{bmatrix} \end{matrix} \quad \begin{matrix} \text{I} \\ \text{like} \\ \text{cats} \end{matrix} \begin{bmatrix} 0.4 & 1.0 \\ 1.2 & 2.8 \\ 1.7 & 0.2 \end{bmatrix} \begin{matrix} v_1 \\ v_2 \\ v_3 \end{matrix} = \begin{matrix} \text{SOS} \\ \text{me} \\ \text{gustan} \\ \text{los} \\ \text{gatos} \end{matrix} \begin{bmatrix} \vec{z}_1 \\ \vec{z}_2 \\ \vec{z}_3 \\ \vec{z}_4 \\ \vec{z}_5 \end{bmatrix}$$

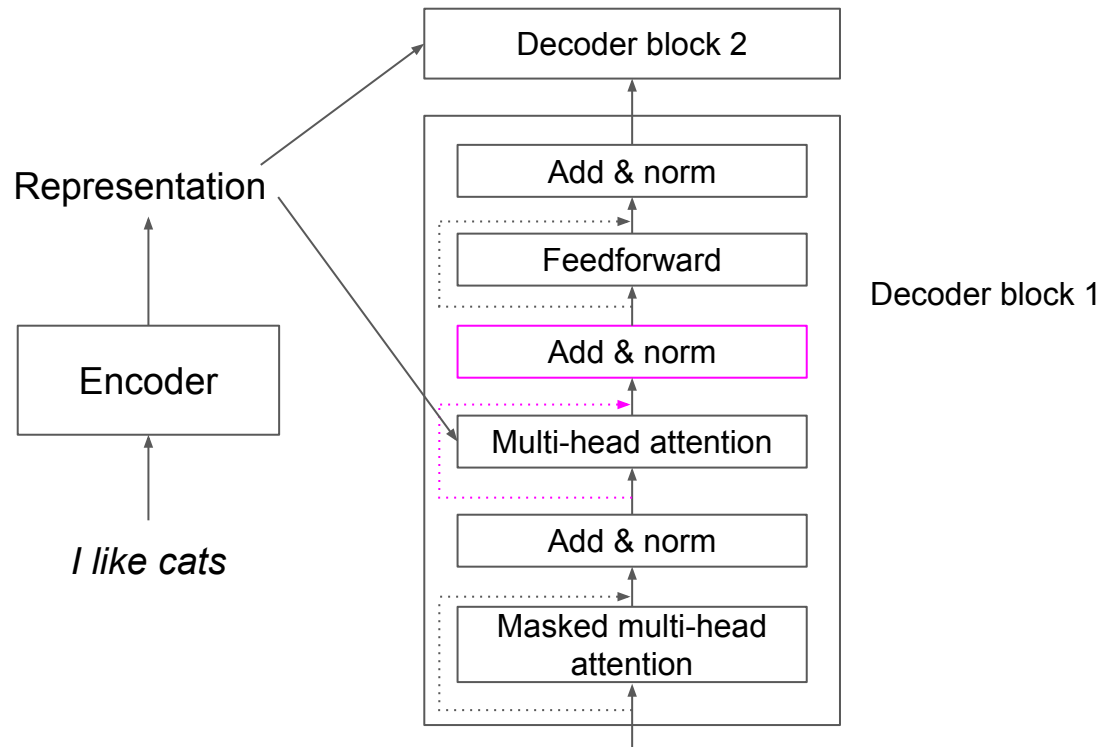
$$\vec{z}_3 = 0.1\vec{v}_1 + 0.8\vec{v}_2 + 0.1\vec{v}_3$$

gustan I like cats

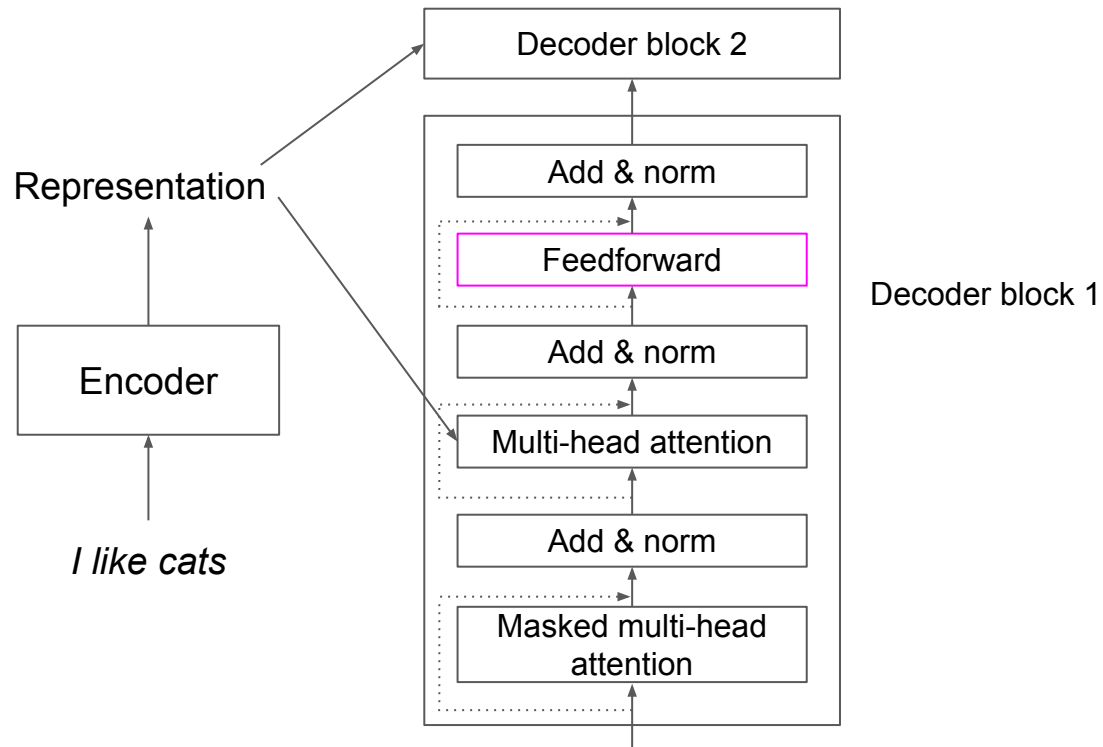
Decoder block



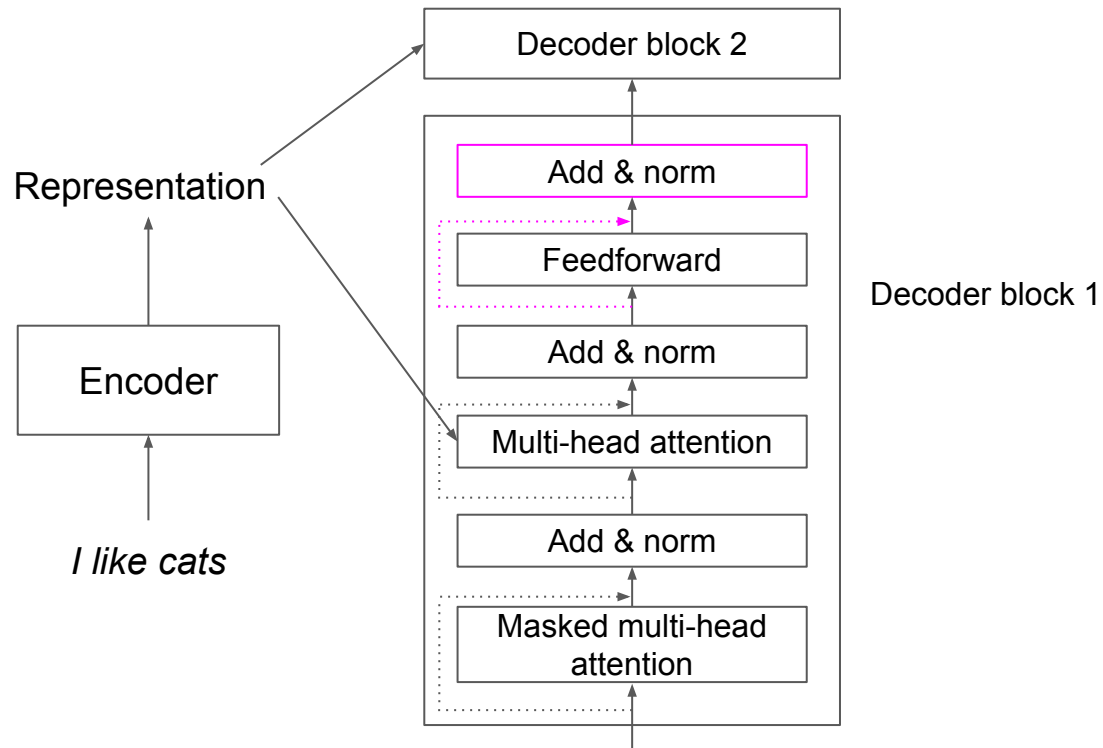
Decoder block



Decoder block

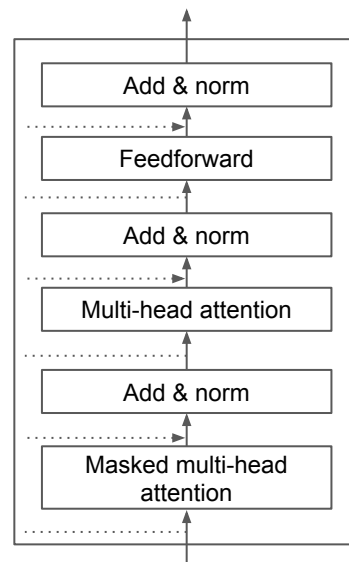


Decoder block

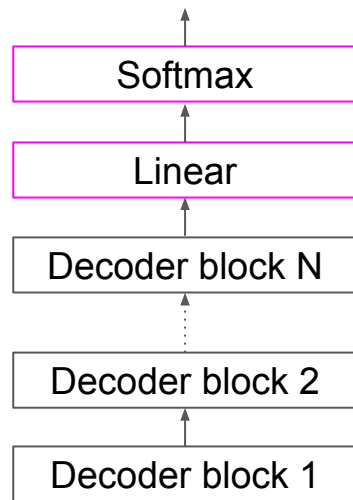


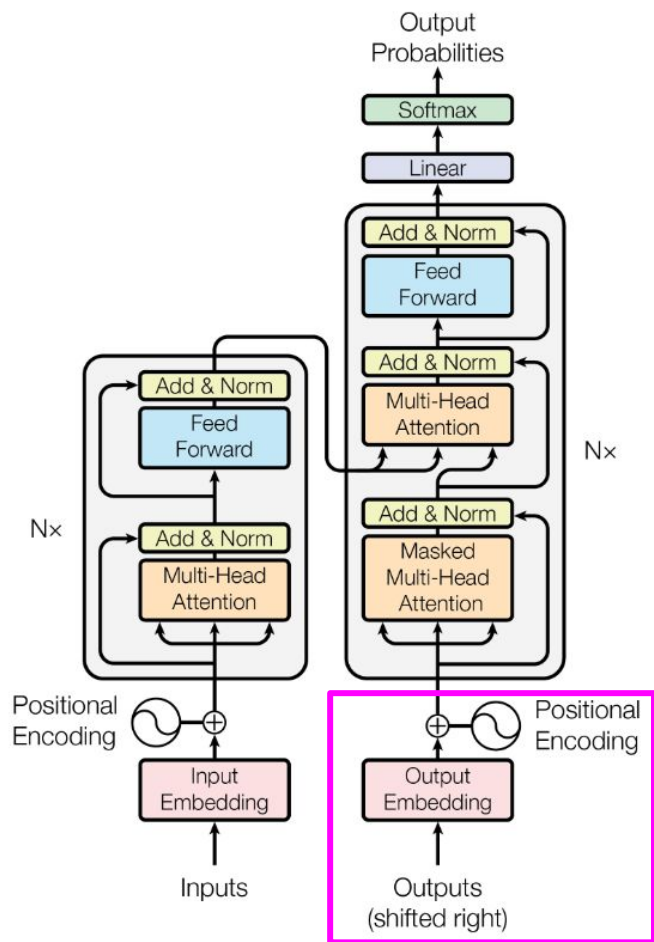
What's the deeper meaning?

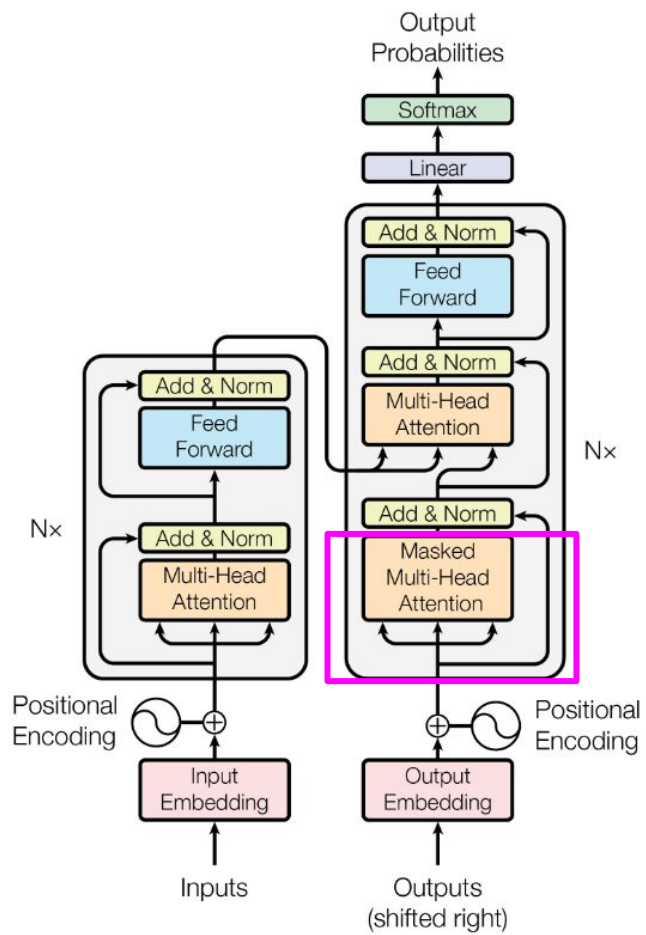
- Masked multi-head attention
- Multi-head attention
- Feedforward
- Add & Norm

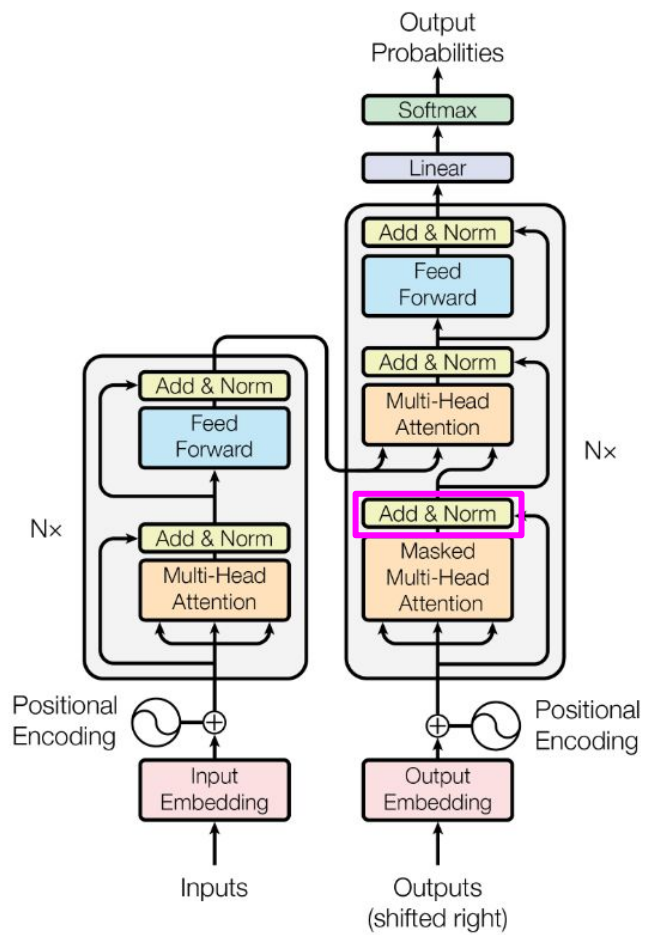


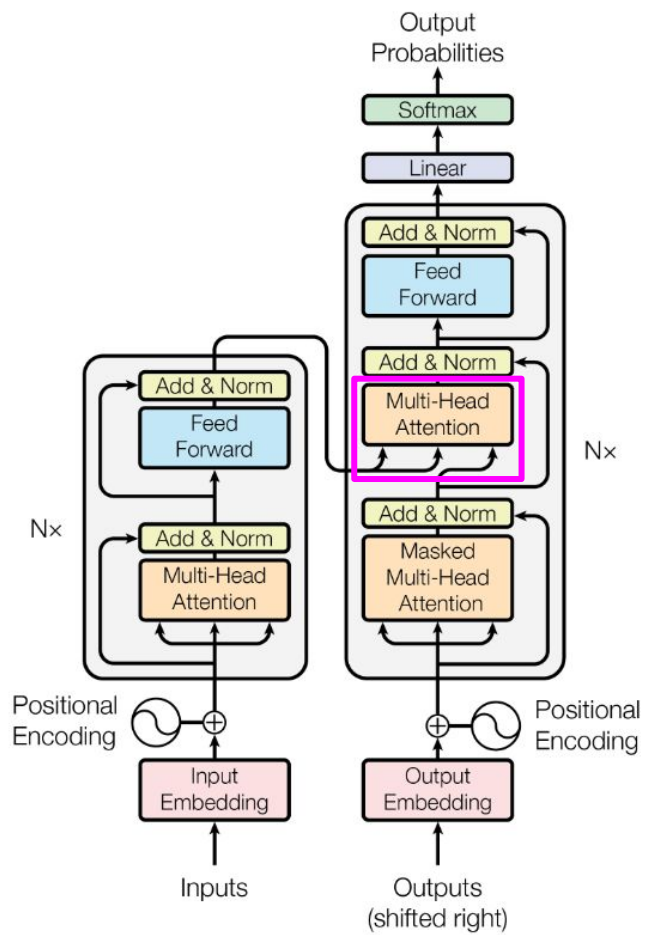
Linear & softmax layers

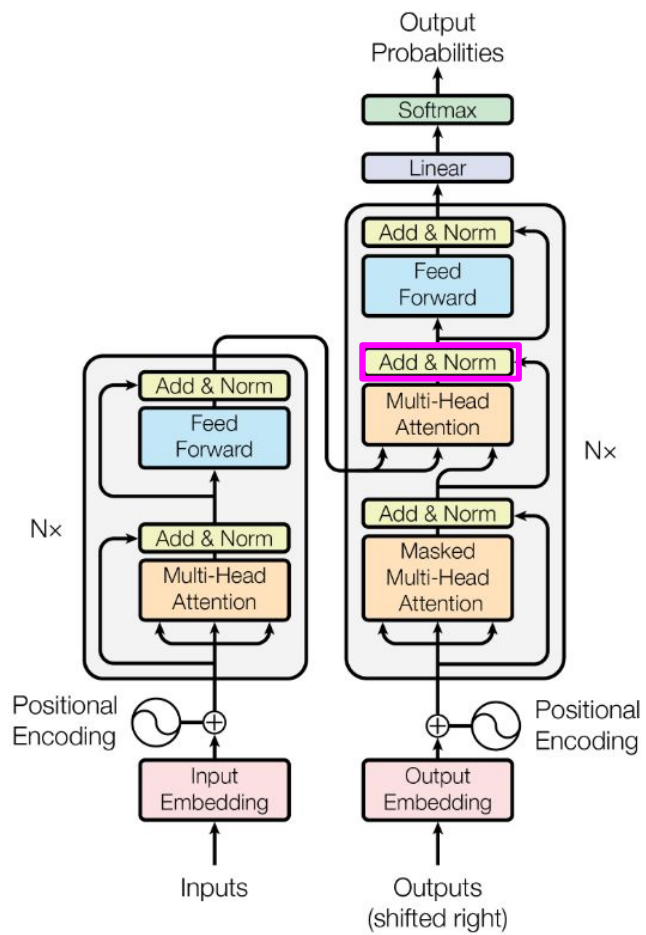


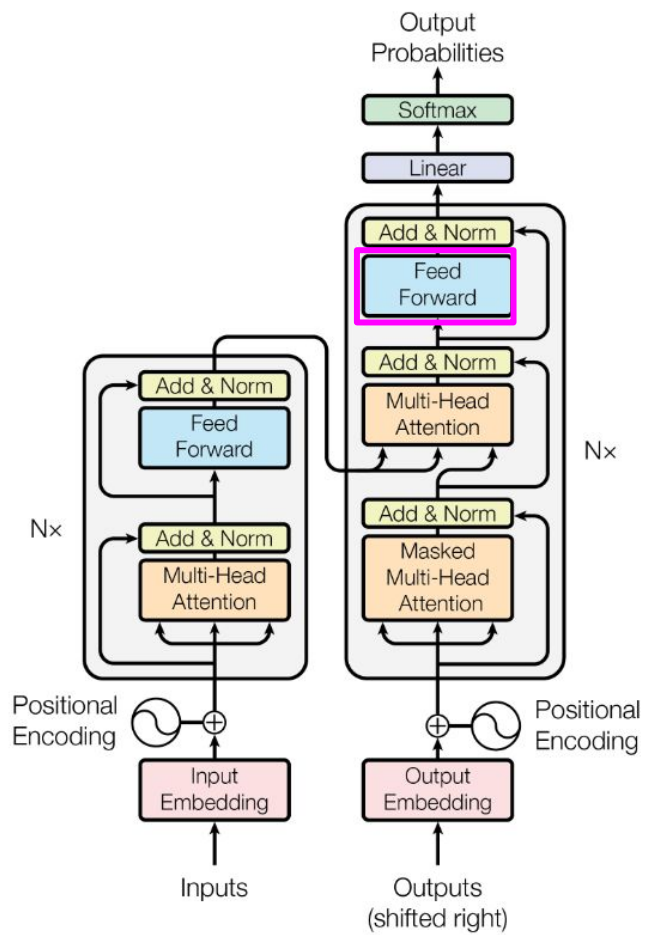


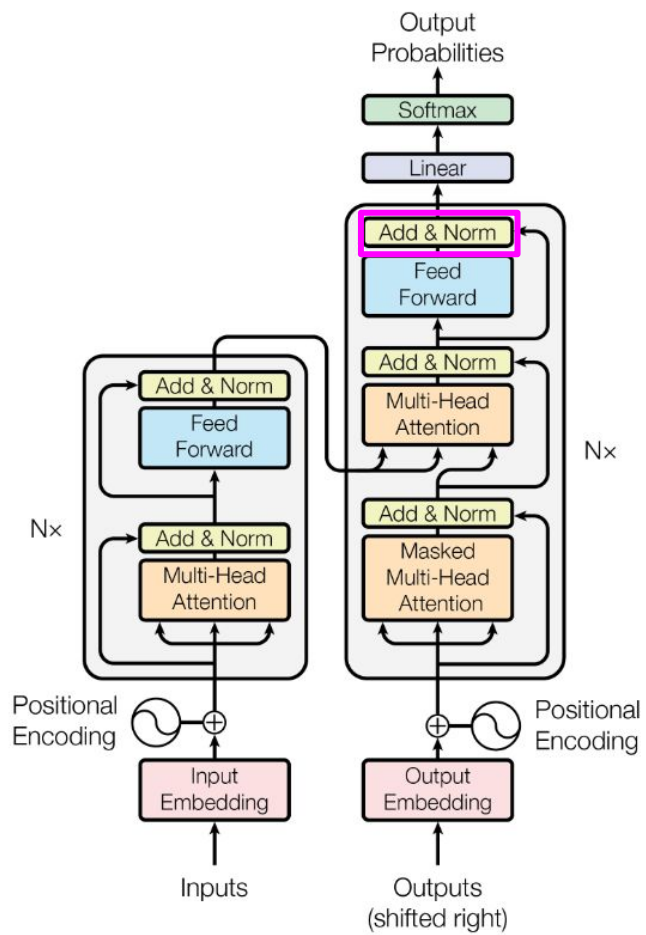


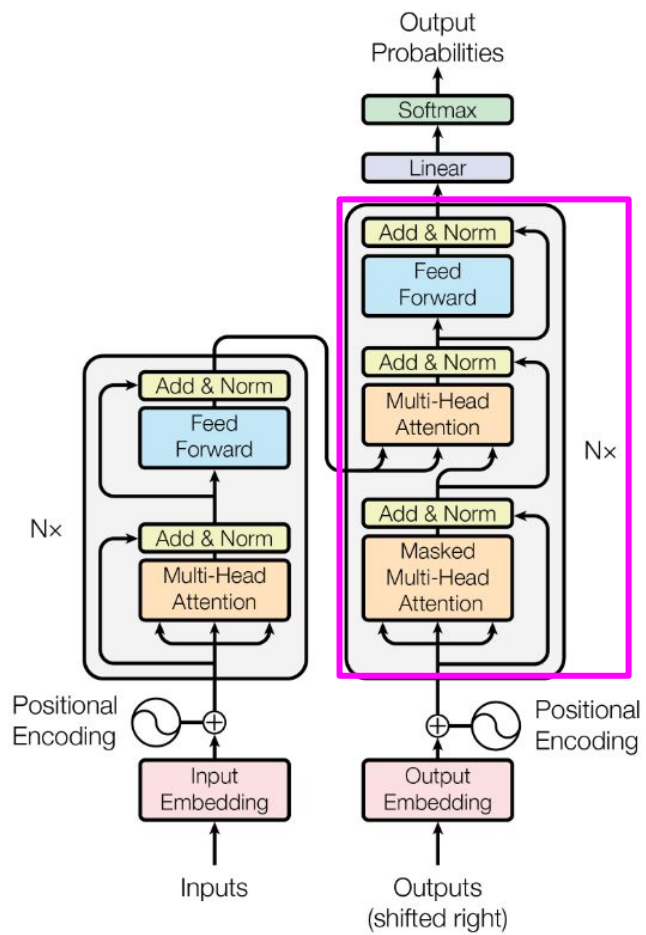


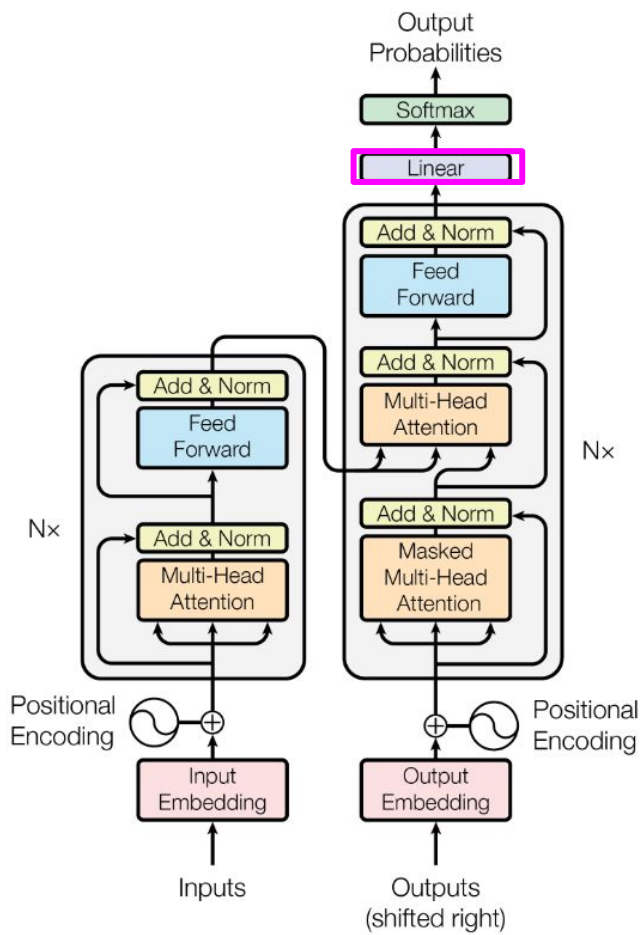


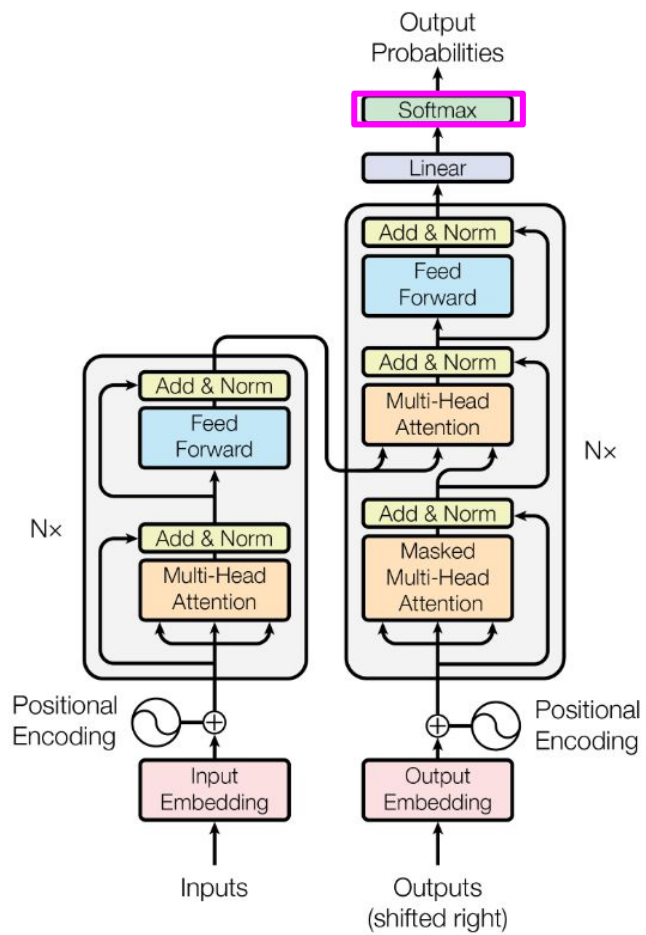


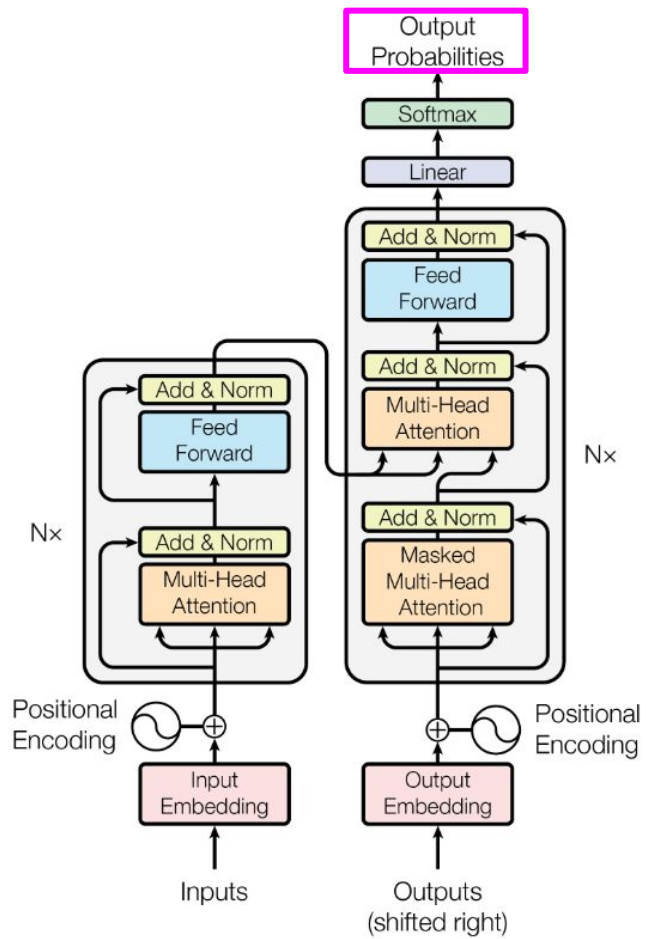












After all of this, why
encoder + decoder?

YOU'VE MADE IT



CONGRATS!

My experience with Transformers

- Most capable model

My experience with Transformers

- Most capable model
- Massive amount of music data needed

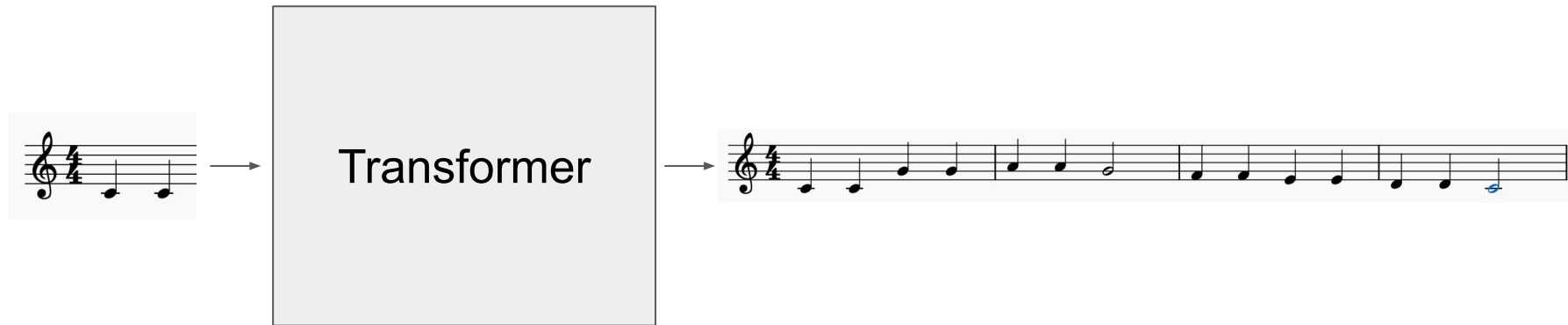
My experience with Transformers

- Most capable model
- Massive amount of music data needed
- Music theory bozo

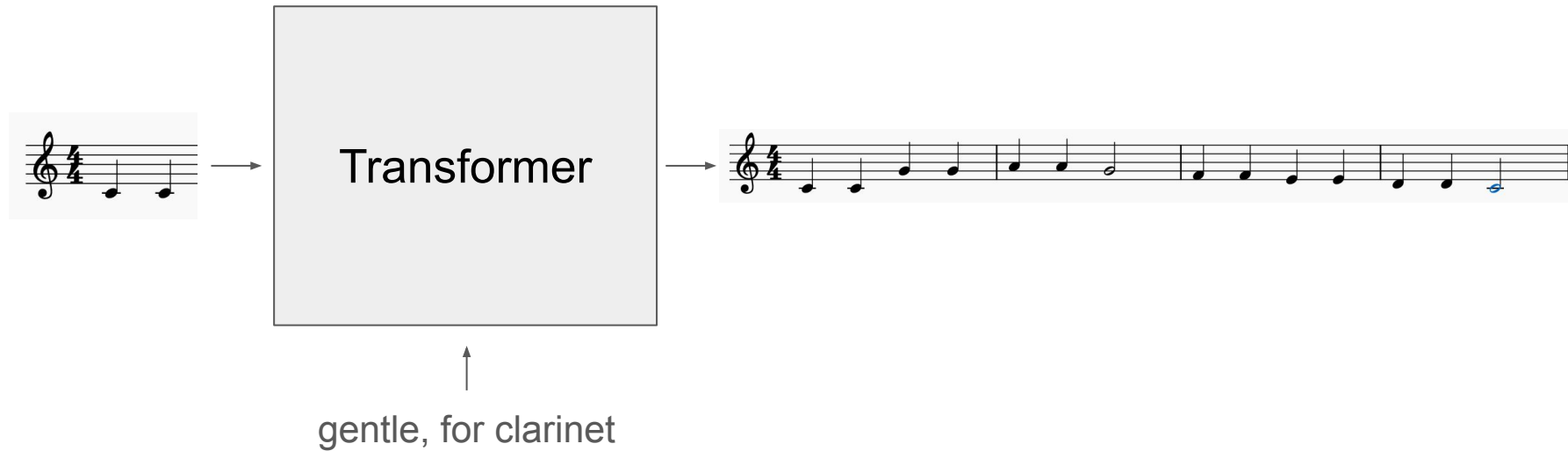
My experience with Transformers

- Most capable model
- Massive amount of music data needed
- Music theory bozo
- Music representation is everything

Lack of creative control



Lack of creative control



**AI ENGINEERS WHO THROW AI AND
BRUTE-FORCE AT MUSIC GENERATION TASKS**



**IGNORING ALL
MUSIC KNOWLEDGE**

My idea

- 2-level transformer
- Level 1: Generate high-level music representation
- Level 2: Fill the notes for level 1

My idea: Music representation



Music gestures: Examples

- Melodic
 - Running scale up
 - Running scale down
- Harmonic
 - Perfect cadence
- Structure
 - Repetition
 - Variation

BEING
AN ESSAY
ON
VARIOUS
SCHEMATA
CHARACTERISTIC OF
EIGHTEENTH-CENTURY
MUSIC
FOR COURTLY CHAMBERS,
CHAPELS, AND THEATERS,
INCLUDING TASTEFUL
PASSAGES OF MUSIC
DRAWN FROM
MOST EXCELLENT
CHAPEL MASTERS
IN THE EMPLOY OF
NOBLE AND NOTEWORTHY
PERSONAGES,
Said Music
All Collected for the
Reader's Delectation
on the
World Wide Web

MUSIC
in the
GALANT STYLE



ROBERT O. GJERDINGEN

Theme

MEYER

1 2 3 4 5 6 7

PRINNER

.....

CADENCE

5 6 7 8 9 10 11 12

9

IV V

MONTE

13 14 15 16 17 18 19

14

VI

CADENCE

20 21 22 23 24 25 26

18

MEYER

27 28 29 30 31 32 33

22

PRINNER

.....

CADENCE

34 35 36 37 38 39 40

My idea: Level 1 music representation

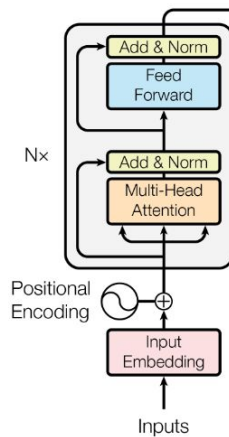
- High-level description of symbolic music

My idea: Level 1 music representation

- High-level description of symbolic music
- Easier to learn
- More coherent generation
- Controllable

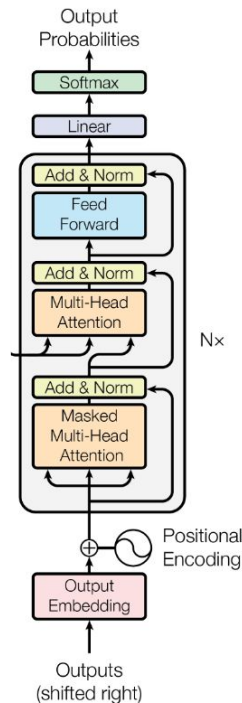
3 types of Transformer architectures

- Encoder only (BERT, MERT)



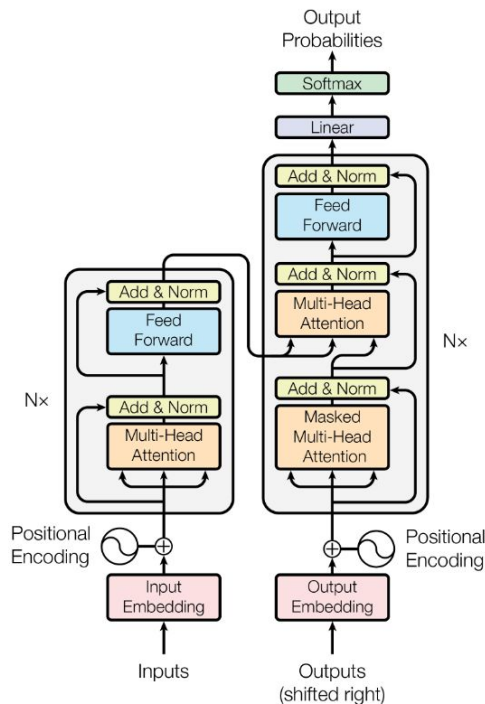
3 types of Transformer architectures

- Encoder only (BERT, MERT)
- Decoder only (GPT, MuPT)



3 types of Transformer architectures

- Encoder only (BERT, MERT)
- Decoder only (GPT, MuPT)
- Encoder - decoder



How can you condition
music generation on
text (*a la* Suno)?

How do we condition generation?

1. Single prompt (decoder)

[text tokens] <SEP> [music tokens]

How do we condition generation?

1. Single prompt (decoder)
2. Special tokens + segment embeddings (decoder)

<TEXT> blah blah </TEXT>
<MUSIC> ... </MUSIC>

How do we condition generation?

1. Single prompt (decoder)
2. Special tokens + segment embeddings (decoder)
3. Prefix conditioning with learned embeddings (decoder)

[prefix embeddings] + [music tokens]

How do we condition generation?

1. Single prompt (decoder)
2. Special tokens + segment embeddings (decoder)
3. Prefix conditioning with learned embeddings (decoder)
4. Encoder - decoder conditioning

How do we condition generation?

1. Single prompt (decoder)
2. Special tokens + segment embeddings (decoder)
3. Prefix conditioning with learned embeddings (decoder)
4. Encoder - decoder conditioning
5. Multi-stream encoder - decoder conditioning

Can transformers
create truly original
music? Can they get
us to transformational
creativity?

Tips for using Transformers

- Get as much (consistent) data as possible

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- Augment music data
- When using pre-trained models:
 - Fine-tune
 - Distillation

Bridging symbolic and audio

- Come up with a strategy / new architecture to repurpose the Transformer architecture for audio-based music gen.
- What challenges would you face?

ANY QUESTIONS / DOUBTS/ IDEAS?

