## Integral Applications

Area between two curves, integrating on the x-axis

$$A = \int_{a}^{b} [f(x) - g(x)] dx$$

Area between two curves, integrating on the y-axis

$$A = \int_{c}^{d} [u(y) - v(y)] dy$$

Disk Method along the x-axis

$$V = \int_a^b \pi [f(x)]^2 dx$$

Disk Method along the y-axis

$$V = \int_{c}^{d} \pi [g(y)]^2 dy$$

Washer Method

$$V = \int_{a}^{b} \pi [(f(x))^{2} - (g(x))^{2}] dx$$

Method of Cylindrical Shells

$$V = \int_{a}^{b} (2\pi x f(x)) dx$$

Arc Length of a Function of  $\mathbf{x}$ 

Arc Length = 
$$\int_a^b \sqrt{1 + [f'(x)]^2} dx$$

Arc Length of a Function of y

Arc Length = 
$$\int_{c}^{d} \sqrt{1 + [g'(y)]^2} \, dy$$

Surface Area of a Function of x

Surface Area = 
$$\int_a^b \left(2\pi f(x)\sqrt{1+(f'(x))^2}\right) dx$$