## Veriopt Theories

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An IRGraph can be treated as an instantiation of various type classes such as the equal type class.

Here we define the instantiations for all type classes of which IRGraph belongs.

## 1.1 Equal Instance

The following is an incorrect definition of equality which is used to allow code generation of the Canonicalization phase. Without this we have to use the values command to generate all possible results of the canonicalization phase.

Note that we should be able to find a correct equality definition in terms of the ids, kind, and stamp function. However, we are yet to find a satisfactory definition as yet.

**definition** IRGraph-equal ::  $IRGraph \Rightarrow IRGraph \Rightarrow bool$  where IRGraph-equal g1 g2 = True

 $\begin{array}{l} \textbf{instantiation} \ \mathit{IRGraph} :: \ \mathit{equal} \\ \textbf{begin} \end{array}$ 

```
definition equal-IRGraph :: IRGraph \Rightarrow IRGraph \Rightarrow bool where
  equal-IRGraph = IRGraph-equal
instance proof
  \mathbf{fix}\ g1\ g2\ ::\ IRGraph
 show equal-class.equal g1 g2 \longleftrightarrow (g1 = g2)
   apply standard
   unfolding equal-IRGraph-def IRGraph-equal-def
   unfolding as-list-def
   apply transfer
   sorry
qed
end
end
{\bf theory}\ Validation Snippets
 imports
   IRGraphSort
   Snippets. Snipping
   Graph.\ Comparison
    Conditional Elimination. Conditional Elimination\\
begin
notation (latex)
  kind (-\langle - \rangle)
    StepSemantics
    intval-mod\ (IntVal\ (b1.0::nat)\ (v1.0::64\ word))
    (IntVal\ (b2.0::nat)\ (v2.0::64\ word)) =
    (if v2.0 = (0::64 word) then UndefVal
    else new-int-bin b1.0 b2.0
          (word-of-int
            (int-signed-value b1.0 v1.0 smod
             int-signed-value b2.0 v2.0)))
    eval:rem
    Modulo\, Test Snippet
    static\text{-}test
                  moduloSnippet
                                       [(Int Val
                                                    32
                                                           (1)),
                                                                     (Intval
                                                                                32
    (-2147483648))] (IntVal 32 (1))
```

```
Conditional Initial Encoding
definition test1-initial :: IRGraph where
test1-initial = irgraph
(0, (StartNode (Some 3) 7), VoidStamp),
(1, (ParameterNode 0), default-stamp),
(2, (ParameterNode 1), default-stamp),
(3, (FrameState | None None None), IllegalStamp),
(4, (IntegerLessThanNode 2 1), VoidStamp),
(5, (BeginNode 8), VoidStamp),
(6, (BeginNode 13), VoidStamp),
(7, (IfNode 4 6 5), VoidStamp),
(8, (EndNode), VoidStamp),
(9, (MergeNode [8, 10] (Some 16) 18), VoidStamp),
(10, (EndNode), VoidStamp),
(11, (BeginNode 15), VoidStamp),
(12, (BeginNode 10), VoidStamp),
(13, (IfNode 4 11 12), VoidStamp),
(14, (ConstantNode (IntVal 32 (1))), IntegerStamp 32 (1) (1)),
(15, (ReturnNode (Some 14) None), VoidStamp),
(16, (FrameState [] None None None), IllegalStamp),
(17, (ConstantNode (IntVal 32 (2))), IntegerStamp 32 (2) (2)),
(18, (ReturnNode (Some 17) None), VoidStamp)
```

```
Conditional Optimized Encoding \\
definition test1-final :: IRGraph where
test1-final = irgraph [
(0, (StartNode (Some 3) 7), VoidStamp),
(1, (ParameterNode 0), default-stamp),
(2, (ParameterNode 1), default-stamp),
(3, (FrameState [] None None None), IllegalStamp),
(4, (IntegerLessThanNode 2 1), VoidStamp),
(5, (BeginNode 8), VoidStamp),
(6, (BeginNode 13), VoidStamp),
(7, (IfNode 4 6 5), VoidStamp),
(8, (EndNode), VoidStamp),
(9, (MergeNode [8, 10] (Some 16) 18), VoidStamp),
(10, (EndNode), VoidStamp),
(11, (BeginNode 15), VoidStamp),
(12, (BeginNode 10), VoidStamp),
(13, (IfNode 19 11 12), VoidStamp),
(14, (ConstantNode (IntVal 32 (1))), IntegerStamp 32 (1) (1)),
(15, (ReturnNode (Some 14) None), VoidStamp),
(16, (FrameState [] None None None), IllegalStamp),
(17, (ConstantNode (IntVal 32 (2))), IntegerStamp 32 (2) (2)),
(18, (ReturnNode (Some 17) None), VoidStamp),
(19, (ConstantNode (IntVal 1 (1))), VoidStamp)
```

 ${\bf value} \ runConditional Elimination \ test 1-initial$ 

## Conditional Test

**corollary** (runConditionalElimination test1-initial)  $\approx_s$  test1-final by eval

end