Unspecified Veriopt Theory

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Contents

theory SemanticsSnippets

```
imports
    Optimizations. \ Canonicalization Proofs
begin
notation (latex)
  kind (-\langle - \rangle)
syntax (spaced-type-def output)
  -constrain :: logic => type => logic (- :: - [4, 0] 3)
                       is-BinaryArithmeticNode :: IRNode <math>\Rightarrow bool
inputs-of :: IRNode \Rightarrow nat\ list
inputs-of (ConstantNode \ const) = []
inputs-of\ (ParameterNode\ index) = []
inputs-of\ (ValuePhiNode\ nid\ values\ merge) = merge\cdot values
inputs-of (AddNode\ x\ y) = [x,\ y]
inputs-of\ (IfNode\ condition\ trueSuccessor\ falseSuccessor) = [condition]
 typedef \ IRGraph = \{g :: ID \rightarrow IRNode \ . \ finite \ (dom \ g)\}
fun ids-fake :: (ID \rightarrow IRNode) \Rightarrow ID set where
  ids-fake g = \{ nid \in dom \ g \ . \ g \ nid \neq (Some \ NoNode) \}
fun kind-fake :: (ID \rightarrow IRNode) \Rightarrow (ID \Rightarrow IRNode) where
  kind\text{-}fake\ g = (\lambda nid.\ (case\ g\ nid\ of\ None \Rightarrow NoNode\ |\ Some\ v \Rightarrow v))
```

```
ids-fake :: (nat \Rightarrow IRNode \ option) \Rightarrow nat \ set
ids-fake g = \{nid \in dom \ g \mid g \ nid \neq Some \ NoNode\}
kind\text{-}fake :: (nat \Rightarrow IRNode \ option) \Rightarrow nat \Rightarrow IRNode
kind-fake g = (\lambda nid. case g \ nid \ of \ None <math>\Rightarrow NoNode \ | \ Some \ v \Rightarrow v)
inputs :: IRGraph \Rightarrow nat \Rightarrow nat set
inputs \ g \ nid = set \ (inputs-of \ g \langle nid \rangle)
succ :: IRGraph \Rightarrow nat \Rightarrow nat set
succ\ g\ nid = set\ (successors-of\ g\langle\!\langle nid\rangle\!\rangle)
input\text{-}edges :: IRGraph \Rightarrow (nat \times nat) set
input\text{-}edges\ g = (\bigcup_{i \in ids\ g} \{(i, j) \mid j \in inputs\ g\ i\})
usages :: IRGraph \Rightarrow nat \Rightarrow nat set
usages\ g\ nid = \{j \in ids\ g \mid (j,\ nid) \in input\text{-}edges\ g\}
successor\text{-}edges :: IRGraph \Rightarrow (nat \times nat) set
successor\text{-}edges\ g = (\bigcup_{i \in ids\ g} \{(i,j) \mid j \in succ\ g\ i\})
predecessors :: IRGraph \Rightarrow nat \Rightarrow nat set
predecessors \ g \ nid = \{j \in \mathit{ids} \ g \mid (j, \ nid) \in \mathit{successor-edges} \ g\}
wf-start g =
(0 \in ids \ g \land is\text{-}StartNode \ g\langle\langle 0\rangle\rangle)
\textit{wf-closed}\ g =
(\forall n \in ids \ g.
     inputs g n \subseteq ids g \land
     succ \ g \ n \subseteq ids \ g \land g\langle\langle n \rangle\rangle \neq NoNode
```

```
wf-phis g =
(\forall n \in ids \ g.
     is-PhiNode g\langle n \rangle \longrightarrow
    |ir\text{-}values\ g\langle\langle n\rangle\rangle| =
     |ir\text{-}ends\ g\langle\langle ir\text{-}merge\ g\langle\langle n\rangle\rangle\rangle\rangle|
wf-ends g =
(\forall n \in ids \ g.
     is-AbstractEndNode g\langle n \rangle \longrightarrow
     0 < |usages\ g\ n|)
wf-graph :: IRGraph \Rightarrow bool
\textit{wf-graph } g = (\textit{wf-start } g \land \textit{wf-closed } g \land \textit{wf-phis } g \land \textit{wf-ends } g)
type-synonym Signature = string
type-synonym Program = Signature 
ightharpoonup IRGraph
print-antiquotations
type-synonym Heap = objref \Rightarrow string \Rightarrow Value
type-synonym Free=nat
type-synonym DynamicHeap = Heap \times Free
h-load-field :: objref \Rightarrow string \Rightarrow DynamicHeap \Rightarrow Value
h-load-field rf(h, n) = h r f
\textit{h-store-field} :: \textit{objref} \Rightarrow \textit{string} \Rightarrow \textit{Value} \Rightarrow \textit{DynamicHeap} \Rightarrow \textit{DynamicHeap}
h-store-field r f v (h, n) = (h(r := (h r)(f := v)), n)
h\text{-}new\text{-}inst::DynamicHeap \Rightarrow (DynamicHeap \times Value)
h-new-inst (h, n) = ((h, n + 1), ObjRef (Some n))
```

eval:const eval:add eval:param eval:phi eval:invoke eval:invoke eval:load

step:seq step:if step:end step:newinst step:load step:store

top:lift top:invoke top:return top:unwind

$$g\langle\!\langle x\rangle\!\rangle = ConstantNode\ c-1$$

$$\underline{g\langle\!\langle y\rangle\!\rangle} = ConstantNode\ c-2 \qquad val = intval-add\ c-1\ c-2$$

$$\overline{CanonicalizeAdd\ g\ (AddNode\ x\ y)\ (ConstantNode\ val)}$$

$$\underline{g\langle\!\langle x\rangle\!\rangle} = ConstantNode\ c-1 \qquad \neg\ is\text{-}ConstantNode\ g\langle\!\langle y\rangle\!\rangle \qquad c-1 = IntVal32\ 0}$$

$$\overline{CanonicalizeAdd\ g\ (AddNode\ x\ y)\ (RefNode\ y)}$$

$$\underline{\neg\ is\text{-}ConstantNode\ g\langle\!\langle x\rangle\!\rangle \qquad g\langle\!\langle y\rangle\!\rangle = ConstantNode\ c-2 \qquad c-2 = IntVal32\ 0}$$

$$\overline{CanonicalizeAdd\ g\ (AddNode\ x\ y)\ (RefNode\ x)}$$

 $[CanonicalizeAdd\ g\ before\ after;\ wf-graph\ g \land wf-stamps\ g;\ [g,\ m,\ p] \vdash before \mapsto IntVal32\ res;\ [g,\ m,\ p] \vdash after \mapsto IntVal32\ res'] \Longrightarrow res = res'$

$$\frac{g,\ p \vdash (nid,\ m,\ h) \rightarrow (nid',\ m,\ h)}{g\ m\ p\ h \vdash nid \leadsto nid'}$$

$$\frac{g,\ p \vdash (nid,\ m,\ h) \rightarrow (nid'',\ m,\ h) \qquad g\ m\ p\ h \vdash nid'' \leadsto nid'}{g\ m\ p\ h \vdash nid \leadsto nid'}$$

$$\frac{g \langle\!\langle cond \rangle\!\rangle = ConstantNode\ condv \qquad val\text{-}to\text{-}bool\ condv}{CanonicalizeIf\ g\ (IfNode\ cond\ tb\ fb)\ (RefNode\ tb)}$$

$$\frac{g \langle\!\langle cond \rangle\!\rangle = ConstantNode\ condv \qquad \neg\ val\text{-}to\text{-}bool\ condv}{CanonicalizeIf\ g\ (IfNode\ cond\ tb\ fb)\ (RefNode\ fb)}$$

$$\frac{\neg\ is\text{-}ConstantNode\ g \langle\!\langle cond \rangle\!\rangle \qquad tb\ =\ fb}{CanonicalizeIf\ g\ (IfNode\ cond\ tb\ fb)\ (RefNode\ tb)}$$

definition replace-node-fake :: $ID \Rightarrow IRNode \Rightarrow IRGraph \Rightarrow IRGraph$ where replace-node-fake nid node g = replace-node nid (node, default-stamp) g lemma CanonicalizeIfProof-fake: fixes m:: MapState and h:: RefFieldHeap assumes $kind\ g\ nid = before$ assumes $CanonicalizeIf\ g\ before\ after$ assumes g' = replace-node-fake nid after g assumes $g,\ p \vdash (nid,\ m,\ h) \rightarrow (nid',\ m,\ h)$ shows $nid \mid g \sim g'$ by $(metis\ CanonicalizeIfProof\ assms(1)\ assms(2)\ assms(3)\ assms(4)\ replace$ -node-fake-def)

```
 \begin{array}{c} \textbf{notation } (latex \ \textbf{output}) \\ filtered-inputs \ (inputs^{-\langle\!\langle -\rangle\!\rangle}_{-}) \\ \textbf{notation } (latex \ \textbf{output}) \\ filtered-successors \ (succ^{-\langle\!\langle -\rangle\!\rangle}_{-}) \\ \textbf{notation } (latex \ \textbf{output}) \\ filtered-usages \ (usages^{-\langle\!\langle -\rangle\!\rangle}_{-}) \\ \\ inputs^{g\langle\!\langle nid\rangle\!\rangle}_{f} \\ \\ \textbf{notation } (latex \ \textbf{output}) \\ Pure.dummy-pattern \ (-) \\ \\ \textbf{end} \\ \end{array}
```