Veriopt Theories

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```
markup\ DSL-Tokens.Less = @\{term\ BinaryExpr\} \$ @\{term\ BinIntegerLessThan\}
  markup\ DSL\text{-}Tokens.Equals = @\{term\ BinaryExpr\} \$ @\{term\ BinIntegerEquals\}
  markup\ DSL\text{-}Tokens.Not = @\{term\ UnaryExpr\} \$ @\{term\ UnaryLogicNegation\}
   markup\ DSL\text{-}Tokens.Negate = @\{term\ UnaryExpr\} \$ @\{term\ UnaryNeg\}
  | markup\ DSL\text{-}Tokens.LeftShift = @\{term\ BinaryExpr\} \$ @\{term\ BinLeftShift\}
 | markup\ DSL-Tokens. RightShift = @\{term\ BinaryExpr\}  $ @\{term\ BinRightShift\} 
  URightShift
   markup\ DSL\text{-}Tokens.Conditional = @\{term\ ConditionalExpr\}
   markup\ DSL-Tokens.Constant = @\{term\ ConstantExpr\}
   markup\ DSL\text{-}Tokens.TrueConstant = @\{term\ ConstantExpr\ (IntVal32\ 1)\}
   markup\ DSL\text{-}Tokens.FalseConstant = @\{term\ ConstantExpr\ (IntVal32\ 0)\}
end
structure\ IntValTranslator: DSL-TRANSLATION =
fun \ markup \ DSL-Tokens.Add = @\{term \ intval-add\}
   markup\ DSL\text{-}Tokens.Sub = @\{term\ intval\text{-}sub\}
   markup\ DSL-Tokens.Mul = @\{term\ intval-mul\}
   markup\ DSL-Tokens.And = @\{term\ intval-and\}
   markup\ DSL\text{-}Tokens.Or = @\{term\ intval\text{-}or\}
   markup\ DSL\text{-}Tokens.Xor = @\{term\ intval\text{-}xor\}
   markup\ DSL\text{-}Tokens.Abs = @\{term\ intval\text{-}abs\}
   markup\ DSL\text{-}Tokens.Less = @\{term\ intval\text{-}less\text{-}than\}
   markup\ DSL\text{-}Tokens.Equals = @\{term\ intval\text{-}equals\}
   markup\ DSL\text{-}Tokens.Not = @\{term\ intval\text{-}logic\text{-}negation\}
   markup\ DSL\text{-}Tokens.Negate = @\{term\ intval\text{-}negate\}
   markup\ DSL-Tokens.LeftShift = @\{term\ intval-left-shift\}
   markup\ DSL\text{-}Tokens.RightShift = @\{term\ intval\text{-}right\text{-}shift\}
   markup\ DSL\text{-}Tokens.UnsignedRightShift = @\{term\ intval\text{-}uright\text{-}shift\}
   markup\ DSL\text{-}Tokens.Conditional = @\{term\ intval\text{-}conditional\}
   markup\ DSL-Tokens.Constant = @\{term\ IntVal32\}
   markup\ DSL-Tokens. TrueConstant = @\{term\ IntVal32\ 1\}
   markup\ DSL-Tokens.FalseConstant = @\{term\ IntVal32\ 0\}
end
structure\ IRExprMarkup = DSL-Markup(IRExprTranslator);
structure\ IntValMarkup = DSL-Markup(IntValTranslator);
   ir expression translation
   syntax - expandExpr :: term \Rightarrow term (exp[-])
                                    @\{syntax\text{-}const
   parse-translation \leftarrow [(
                                                        -expandExpr
                                                                             IREx-
   prMarkup.markup-expr [])] \rightarrow
```

```
ir\ expression\ example
```

```
value exp[(e_1 < e_2) ? e_1 : e_2]
```

 $Conditional Expr\ (Binary Expr\ Bin Integer Less Than\ e_1\ e_2)\ e_1\ e_2$

$value\ expression\ example$

```
value val[(e_1 < e_2) ? e_1 : e_2] intval\text{-}conditional (intval\text{-}less\text{-}than } e_1 e_2) e_1 e_2
```

```
value exp[((e_1 - e_2) + (const (IntVal32 \ \theta)) + e_2) \mapsto e_1 \ when \ True]

value val[((e_1 - e_2) + (const \ \theta) + e_2) \mapsto e_1 \ when \ True]
```

\mathbf{end}

theory Phase imports Main begin

ML-file map.ML
ML-file phase.ML

end

1.1 Canonicalization DSL

```
theory Canonicalization
imports

Markup
Phase
keywords
phase :: thy-decl and
terminating :: quasi-command and
print-phases :: diag and
optimization :: thy-goal-defn
begin

ML <
datatype 'a Rewrite =
Transform of 'a * 'a |
Conditional of 'a * 'a * term |
```

```
Sequential of 'a Rewrite * 'a Rewrite |
 Transitive of 'a Rewrite
type\ rewrite = \{name: string, rewrite: term\ Rewrite\}
structure\ RewriteRule: Rule =
struct
type T = rewrite;
fun\ pretty-rewrite\ ctxt\ (Transform\ (from,\ to)) =
     Pretty.block
      Syntax.pretty-term ctxt from,
      Pretty.str \mapsto,
      Syntax.pretty-term ctxt to
 | pretty-rewrite ctxt (Conditional (from, to, cond)) =
     Pretty.block
      Syntax.pretty-term ctxt from,
      Pretty.str \mapsto,
      Syntax.pretty-term ctxt to,
      Pretty.str when,
      Syntax.pretty-term ctxt cond
 | pretty-rewrite - - = Pretty.str not implemented
fun pretty ctxt t =
 Pretty.block [
   Pretty.str ((\#name\ t)\ \widehat{}:),
   pretty-rewrite ctxt (#rewrite t)
end
structure\ RewritePhase = DSL-Phase(RewriteRule);
val - =
 Outer-Syntax.command command-keyword (phase) enter an optimization phase
  (Parse.binding -- | Parse.\$\$\$ terminating -- Parse.const -- | Parse.begin
    >> (Toplevel.begin-main-target true o RewritePhase.setup));
fun \ print-phases \ ctxt =
 let
   val thy = Proof\text{-}Context.theory\text{-}of ctxt;
   fun\ print\ phase = RewritePhase.pretty\ phase\ ctxt
   map print (RewritePhase.phases thy)
 end
fun print-optimizations thy =
 print-phases thy |> Pretty.writeln-chunks
```

```
val - =
  Outer-Syntax. \ command \ \textbf{\textit{command-keyword}} \ \langle \textit{print-phases} \rangle
   print debug information for optimizations
   (Scan.succeed
     (\ Toplevel.keep\ (print-optimizations\ o\ Toplevel.context-of)));
ML-file rewrites.ML
fun rewrite-preservation :: IRExpr\ Rewrite \Rightarrow bool\ \mathbf{where}
  rewrite-preservation (Transform x y) = (y \le x)
 rewrite-preservation (Conditional x y cond) = (cond \longrightarrow (y \le x))
 rewrite-preservation (Sequential xy) = (rewrite-preservation x \land rewrite-preservation
  rewrite-preservation (Transitive x) = rewrite-preservation x
fun rewrite-termination :: IRExpr Rewrite \Rightarrow (IRExpr \Rightarrow nat) \Rightarrow bool where
  rewrite-termination (Transform x y) trm = (trm x > trm y)
 rewrite-termination (Conditional x y cond) trm = (cond \longrightarrow (trm \ x > trm \ y))
 rewrite-termination (Sequential x y) trm = (rewrite-termination \ x \ trm \land rewrite-termination
y trm) \mid
  rewrite-termination (Transitive x) trm = rewrite-termination x trm
fun intval :: Value Rewrite <math>\Rightarrow bool where
  intval\ (Transform\ x\ y) = (x \neq UndefVal \land y \neq UndefVal \longrightarrow x = y) \mid
  intval\ (Conditional\ x\ y\ cond) = (cond \longrightarrow (x = y))
  intval (Sequential x y) = (intval x \wedge intval y)
  intval (Transitive x) = intval x
\mathbf{ML} \leftarrow
structure\ System: Rewrite System=
struct
val\ preservation = @\{const\ rewrite-preservation\};
val\ termination = @\{const\ rewrite-termination\};
val\ intval = @\{const\ intval\};
end
structure\ DSL = DSL-Rewrites(System);
val - =
  Outer	ext{-}Syntax.local	ext{-}theory	ext{-}to	ext{-}proof 	extbf{command-keyword} \land optimization 
angle
   define an optimization and open proof obligation
   (Parse-Spec.thm-name: -- Parse.term
       >> DSL.rewrite-cmd);
```

end