## Veriopt Theories

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1 Canonicalization Phase	
$\begin{array}{c} \textbf{heory} \ \ Common \\ \textbf{imports} \\ Optimization DSL. Canonicalization \\ HOL-Eisbach. Eisbach \\ \textbf{pegin} \end{array}$	
Fun $size :: IRExpr \Rightarrow nat$ where $size (UnaryExpr op e) = (size e) + 1 \mid$ $size (BinaryExpr BinAdd x y) = (size x) + ((size y) * 2) \mid$ $size (BinaryExpr op x y) = (size x) + (size y) \mid$ $size (ConditionalExpr cond t f) = (size cond) + (size t) + (size f) + 2 \mid$ $size (ConstantExpr c) = 1 \mid$ $size (ParameterExpr ind s) = 2 \mid$ $size (LeafExpr nid s) = 2 \mid$ $size (ConstantVar c) = 2 \mid$ $size (VariableExpr x s) = 2$	
method unfold-optimization =  (unfold rewrite-preservation.simps, unfold rewrite-termination.simps, unfold intval.simps, rule conjE, simp, simp del: le-expr-def)   (unfold rewrite-preservation.simps, unfold rewrite-termination.simps, rule conjE, simp, simp del: le-expr-def) end	

## 1.1 Conditional Expression

 $\begin{array}{c} \textbf{theory} \ \textit{ConditionalPhase} \\ \textbf{imports} \end{array}$ 

```
Common
    Proofs. Stamp Eval Thms
begin
phase Conditional
 terminating size
begin
lemma negates: is-IntVal32 e \lor is-IntVal64 e \Longrightarrow val-to-bool (val[e]) \equiv \neg (val-to-bool
  by (smt\ (verit,\ best)\ Value.disc(1)\ Value.disc(10)\ Value.disc(4)\ Value.disc(5)
Value.disc(6)\ Value.disc(9)\ intval-logic-negation.elims\ val-to-bool.simps(1)\ val-to-bool.simps(2)
zero-neq-one)
optimization negate-condition: ((\neg e) ? x : y) \mapsto (e ? y : x)
   apply unfold-optimization apply simp using negates
  \textbf{using } \textit{Conditional ExprE } \textit{Unary ExprE } \textit{intval-logic-negation. elims } \textit{unary-eval. simps} (4)
val-to-bool.simps(1) val-to-bool.simps(2) zero-neq-one
   apply (smt (verit) ConditionalExpr)
   unfolding size.simps by simp
optimization const-true: (true ? x : y) \mapsto x
  apply unfold-optimization
  apply force
  unfolding size.simps by simp
optimization const-false: (false ? x : y) \mapsto y
  apply unfold-optimization
  apply force
  unfolding size.simps by simp
optimization equal-branches: (e ? x : x) \mapsto x
  apply unfold-optimization
  apply force
 unfolding size.simps by auto
definition wff-stamps :: bool where
 wff-stamps = (\forall m \ p \ expr \ val \ . ([m,p] \vdash expr \mapsto val) \longrightarrow valid-value \ val \ (stamp-expr
expr))
definition wf-stamp :: IRExpr \Rightarrow bool where
  wf-stamp e = (\forall m \ p \ v. ([m, p] \vdash e \mapsto v) \longrightarrow valid-value v \ (stamp-expr e))
optimization condition-bounds-x: ((x < y) ? x : y) \mapsto x
   when (stamp-under\ (stamp-expr\ x)\ (stamp-expr\ y)\ \land\ wf-stamp\ x\ \land\ wf-stamp\ y)
  apply unfold-optimization
  using stamp-under-semantics
 using wf-stamp-def
```

```
apply (smt (verit, best) ConditionalExprE le-expr-def stamp-under.simps)
 unfolding size.simps by simp
optimization condition-bounds-y: ((x < y) ? x : y) \mapsto y
   when (stamp-under\ (stamp-expr\ y)\ (stamp-expr\ x) \land wf-stamp\ x \land wf-stamp\ y)
  apply unfold-optimization
 \mathbf{using}\ stamp\text{-}under\text{-}semantics\text{-}inversed
 using wf-stamp-def
 apply (smt (verit, best) ConditionalExprE le-expr-def stamp-under.simps)
 unfolding size.simps by simp
optimization b[intval]: ((x eq y) ? x : y) \mapsto y
  apply unfold-optimization
    apply (smt (z3) bool-to-val.simps(2) intval-equals.elims val-to-bool.simps(1)
val-to-bool.simps(3))
   unfolding intval.simps
  apply (smt (z3) BinaryExprE ConditionalExprE Value.inject(1) Value.inject(2)
bin-eval.simps(10)\ bool-to-val.simps(2)\ evalDet\ intval-equals.simps(1)\ intval-equals.simps(10)
intval-equals.simps(12) intval-equals.simps(15) intval-equals.simps(2)
intval-equals.simps(5) intval-equals.simps(8) intval-equals.simps(9) le-expr-def val-to-bool.cases
val-to-bool. elims(2))
 unfolding size.simps by auto
end
end
```