Veriopt Theories

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Contents

1 Canonicalization Phase

theory *Common*
imports
OptimizationDSL.Canonicalization
HOL−Eisbach.Eisbach
begin

fun *size* :: *IRExpr* ⇒ *nat* **where**
size (*UnaryExpr op e*) = (*size e*) + *1* |
size (*BinaryExpr BinAdd x y*) = (*size x*) + ((*size y*) ∗ *2*) |
size (*BinaryExpr op x y*) = (*size x*) + (*size y*) |
size (*ConditionalExpr cond t f*) = (*size cond*) + (*size t*) + (*size f*) + *2* |
size (*ConstantExpr c*) = *1* |
size (*ParameterExpr ind s*) = *2* |
size (*LeafExpr nid s*) = *2* |
size (*ConstantVar c*) = *2* |
size (*VariableExpr x s*) = *2*

lemma *size-pos*[*simp*]: *0* < *size y*
apply (*induction y*; *auto?*)
subgoal premises *prems* **for** *op a b*
using *prems* **by** (*induction op*; *auto*)
done

lemma *size-non-add*: *op* ≠ *BinAdd* ⟹ *size* (*BinaryExpr op a b*) = *size a* + *size b*
by (*induction op*; *auto*)

lemma *size-non-const*:
¬ *is-ConstantExpr y* ⟹ *1* < *size y*
using *size-pos* **apply** (*induction y*; *auto*)

subgoal premises *prems* **for** *op a b*
apply (*cases op = BinAdd*)
using *size-non-add size-pos* **apply** *auto*
by (*simp add*: *Suc-lessI one-is-add*)+
done

method *unfold-optimization* =
(*unfold rewrite-preservation.simps*, *unfold rewrite-termination.simps*,
unfold intval.simps,
rule conjE, *simp*, *simp del*: *le-expr-def*)
| (*unfold rewrite-preservation.simps*, *unfold rewrite-termination.simps*,
rule conjE, *simp*, *simp del*: *le-expr-def*)

end

1.1 Conditional Expression

theory *ConditionalPhase*
imports
Common
Proofs.StampEvalThms
begin

phase *Conditional*
terminating *size*
begin

lemma *negates*: *is-IntVal32 e* ∨ *is-IntVal64 e* ⟹ *val-to-bool* (*val*[*e*]) ≡ ¬(*val-to-bool* (*val*[¬*e*]))
by (*smt* (*verit*, *best*) *Value.disc*(*1*) *Value.disc*(*10*) *Value.disc*(*4*) *Value.disc*(*5*) *Value.disc*(*6*) *Value.disc*(*9*) *intval-logic-negation.elims val-to-bool.simps*(*1*) *val-to-bool.simps*(*2*) *zero-neq-one*)

optimization *negate-condition*: ((¬*e*) *?* *x* : *y*) ⟼ (*e* *?* *y* : *x*)
apply *unfold-optimization* **apply** *simp* **using** *negates*
using *ConditionalExprE UnaryExprE intval-logic-negation.elims unary-eval.simps*(*4*) *val-to-bool.simps*(*1*) *val-to-bool.simps*(*2*) *zero-neq-one*
apply (*smt* (*verit*) *ConditionalExpr*)
unfolding *size.simps* **by** *simp*

optimization *const-true*: (*true* *?* *x* : *y*) ⟼ *x*
apply *unfold-optimization*
apply *force*
unfolding *size.simps* **by** *simp*

optimization *const-false*: (*false* *?* *x* : *y*) ⟼ *y*
apply *unfold-optimization*
apply *force*
unfolding *size.simps* **by** *simp*

optimization *equal-branches*: $(e\ ?\ x : x) \longmapsto x$
apply *unfold-optimization*
apply *force*
unfolding *size.simps* **by** *auto*

definition *wff-stamps* :: *bool* **where**
wff-stamps = $(\forall\ m\ p\ expr\ val\ .\ ([m,p] \vdash expr \mapsto val) \longrightarrow valid\text{-}value\ val\ (stamp\text{-}expr\ expr))$

definition *wf-stamp* :: *IRExpr* $\Rightarrow$ *bool* **where**
wf-stamp $e = (\forall\ m\ p\ v.\ ([m,\ p] \vdash e \mapsto v) \longrightarrow valid\text{-}value\ v\ (stamp\text{-}expr\ e))$

optimization *condition-bounds-x*: $((u < v)\ ?\ x : y) \longmapsto x$
when $(stamp\text{-}under\ (stamp\text{-}expr\ u)\ (stamp\text{-}expr\ v) \wedge wf\text{-}stamp\ u \wedge wf\text{-}stamp\ v)$
apply *unfold-optimization*
using *stamp-under-semantics*
using *wf-stamp-def*
apply (*smt* (*verit*, *best*) *ConditionalExprE le-expr-def stamp-under.simps*)
unfolding *size.simps* **by** *simp*

optimization *condition-bounds-y*: $((x < y)\ ?\ x : y) \longmapsto y$
when $(stamp\text{-}under\ (stamp\text{-}expr\ y)\ (stamp\text{-}expr\ x) \wedge wf\text{-}stamp\ x \wedge wf\text{-}stamp\ y)$
apply *unfold-optimization*
using *stamp-under-semantics-inversed*
using *wf-stamp-def*
apply (*smt* (*verit*, *best*) *ConditionalExprE le-expr-def stamp-under.simps*)
unfolding *size.simps* **by** *simp*

optimization *b*[*intval*]: $((x\ eq\ y)\ ?\ x : y) \longmapsto y$
apply *unfold-optimization*
apply (*smt* (*z3*) *bool-to-val.simps*(*2*) *intval-equals.elims val-to-bool.simps*(*1*) *val-to-bool.simps*(*3*))
unfolding *intval.simps*
apply (*smt* (*z3*) *BinaryExprE ConditionalExprE Value.inject*(*1*) *Value.inject*(*2*) *bin-eval.simps*(*10*) *bool-to-val.simps*(*2*) *evalDet intval-equals.simps*(*1*) *intval-equals.simps*(*10*) *intval-equals.simps*(*12*) *intval-equals.simps*(*15*) *intval-equals.simps*(*16*) *intval-equals.simps*(*2*) *intval-equals.simps*(*5*) *intval-equals.simps*(*8*) *intval-equals.simps*(*9*) *le-expr-def val-to-bool.cases val-to-bool.elims*(*2*))
unfolding *size.simps* **by** *auto*

end

end