

# Veriopt Theories

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## Contents

<b>1 Optimization DSLs</b>	<b>1</b>
1.1 Canonicalization DSL	4

## 1 Optimization DSLs

```
theory Markup
imports Semantics.IRTreeEval Snippets.Snipping
begin
```

```
datatype 'a Rewrite =
  Transform 'a 'a (-  $\mapsto$  - 10) |
  Conditional 'a 'a bool (-  $\mapsto$  - when - 70) |
  Sequential 'a Rewrite 'a Rewrite |
  Transitive 'a Rewrite
```

```
datatype 'a ExtraNotation =
  ConditionalNotation 'a 'a 'a (- ? - : -) |
  EqualsNotation 'a 'a (- eq -) |
  ConstantNotation 'a (const - 120) |
  TrueNotation (true) |
  FalseNotation (false) |
  ExclusiveOr 'a 'a (-  $\oplus$  -) |
  LogicNegationNotation 'a (!-) |
  ShortCircuitOr 'a 'a (- || -)
```

```
definition word :: ('a::len) word  $\Rightarrow$  'a word where
  word x = x
```

```
ML-file <markup.ML>
```

```
ML <
structure IRExpTranslator : DSL-TRANSLATION =
struct
  fun markup DSL-Tokens.Add = @{term BinaryExpr} $ @{term BinAdd}
    | markup DSL-Tokens.Sub = @{term BinaryExpr} $ @{term BinSub}
```

```

| markup DSL-Tokens.Mul = @{term BinaryExpr} $ @{term BinMul}
| markup DSL-Tokens.And = @{term BinaryExpr} $ @{term BinAnd}
| markup DSL-Tokens.Or = @{term BinaryExpr} $ @{term BinOr}
| markup DSL-Tokens.Xor = @{term BinaryExpr} $ @{term BinXor}
| markup DSL-Tokens.ShortCircuitOr = @{term BinaryExpr} $ @{term Bin-
ShortCircuitOr}
| markup DSL-Tokens.Abs = @{term UnaryExpr} $ @{term UnaryAbs}
| markup DSL-Tokens.Less = @{term BinaryExpr} $ @{term BinIntegerLessThan}
| markup DSL-Tokens.Equals = @{term BinaryExpr} $ @{term BinIntegerEquals}
| markup DSL-Tokens.Not = @{term UnaryExpr} $ @{term UnaryNot}
| markup DSL-Tokens.Negate = @{term UnaryExpr} $ @{term UnaryNeg}
| markup DSL-Tokens.LogicNegate = @{term UnaryExpr} $ @{term UnaryLog-
icNegation}
| markup DSL-Tokens.LeftShift = @{term BinaryExpr} $ @{term BinLeftShift}
| markup DSL-Tokens.RightShift = @{term BinaryExpr} $ @{term BinRight-
Shift}
| markup DSL-Tokens.UnsignedRightShift = @{term BinaryExpr} $ @{term Bin-
URightShift}
| markup DSL-Tokens.Conditional = @{term ConditionalExpr}
| markup DSL-Tokens.Constant = @{term ConstantExpr}
| markup DSL-Tokens.TrueConstant = @{term ConstantExpr (IntVal 32 1)}
| markup DSL-Tokens.FalseConstant = @{term ConstantExpr (IntVal 32 0)}
end

```

structure IntValTranslator : DSL-TRANSLATION =  
struct

```

fun markup DSL-Tokens.Add = @{term intval-add}
| markup DSL-Tokens.Sub = @{term intval-sub}
| markup DSL-Tokens.Mul = @{term intval-mul}
| markup DSL-Tokens.And = @{term intval-and}
| markup DSL-Tokens.Or = @{term intval-or}
| markup DSL-Tokens.ShortCircuitOr = @{term intval-short-circuit-or}
| markup DSL-Tokens.Xor = @{term intval-xor}
| markup DSL-Tokens.Abs = @{term intval-abs}
| markup DSL-Tokens.Less = @{term intval-less-than}
| markup DSL-Tokens.Equals = @{term intval-equals}
| markup DSL-Tokens.Not = @{term intval-not}
| markup DSL-Tokens.Negate = @{term intval-negate}
| markup DSL-Tokens.LogicNegate = @{term intval-logic-negation}
| markup DSL-Tokens.LeftShift = @{term intval-left-shift}
| markup DSL-Tokens.RightShift = @{term intval-right-shift}
| markup DSL-Tokens.UnsignedRightShift = @{term intval-uright-shift}
| markup DSL-Tokens.Conditional = @{term intval-conditional}
| markup DSL-Tokens.Constant = @{term IntVal 32}
| markup DSL-Tokens.TrueConstant = @{term IntVal 32 1}
| markup DSL-Tokens.FalseConstant = @{term IntVal 32 0}
end

```

structure WordTranslator : DSL-TRANSLATION =

```

struct
fun markup DSL-Tokens.Add = @{term plus}
| markup DSL-Tokens.Sub = @{term minus}
| markup DSL-Tokens.Mul = @{term times}
| markup DSL-Tokens.And = @{term Bit-Operations.semiring-bit-operations-class.and}
| markup DSL-Tokens.Or = @{term or}
| markup DSL-Tokens.Xor = @{term xor}
| markup DSL-Tokens.Abs = @{term abs}
| markup DSL-Tokens.Less = @{term less}
| markup DSL-Tokens.Equals = @{term HOL.eq}
| markup DSL-Tokens.Not = @{term not}
| markup DSL-Tokens.Negate = @{term uminus}
| markup DSL-Tokens.LogicNegate = @{term logic-negate}
| markup DSL-Tokens.LeftShift = @{term shiftl}
| markup DSL-Tokens.RightShift = @{term signed-shiftr}
| markup DSL-Tokens.UnsignedRightShift = @{term shiftr}
| markup DSL-Tokens.Constant = @{term word}
| markup DSL-Tokens.TrueConstant = @{term 1}
| markup DSL-Tokens.FalseConstant = @{term 0}
end

```

```

structure IRExprMarkup = DSL-Markup(IRExprTranslator);
structure IntValMarkup = DSL-Markup(IntValTranslator);
structure WordMarkup = DSL-Markup(WordTranslator);
>

```

*ir expression translation*

```

syntax -expandExpr :: term ⇒ term (exp[-])
parse-translation < [( @{syntax-const -expandExpr} , IRExprMarkup.markup-expr []) >

```

*value expression translation*

```

syntax -expandIntVal :: term ⇒ term (val[-])
parse-translation < [( @{syntax-const -expandIntVal} , IntValMarkup.markup-expr []) >

```

*word expression translation*

```

syntax -expandWord :: term ⇒ term (bin[-])
parse-translation < [( @{syntax-const -expandWord} , WordMarkup.markup-expr []) >

```

*ir expression example*

**value** *exp*[( $e_1 < e_2$ ) ?  $e_1 : e_2$ ]

*ConditionalExpr* (*BinaryExpr* *BinIntegerLessThan*  $e_1$   $e_2$ )  $e_1$   $e_2$

*value expression example*

**value** *val*[( $e_1 < e_2$ ) ?  $e_1 : e_2$ ]

*intval-conditional* (*intval-less-than*  $e_1$   $e_2$ )  $e_1$   $e_2$

**value** *exp*[( $(e_1 - e_2) + (\text{const } (\text{IntVal } 32\ 0)) + e_2$ )  $\mapsto e_1$  when *True*]

*word expression example*

**value** *bin*[ $x \ \& \ y \mid z$ ]

*intval-conditional* (*intval-less-than*  $e_1$   $e_2$ )  $e_1$   $e_2$

**value** *bin*[ $\neg x$ ]

**value** *val*[ $\neg x$ ]

**value** *exp*[ $\neg x$ ]

**value** *bin*[ $!x$ ]

**value** *val*[ $!x$ ]

**value** *exp*[ $!x$ ]

**value** *bin*[ $\neg x$ ]

**value** *val*[ $\neg x$ ]

**value** *exp*[ $\neg x$ ]

**value** *bin*[ $\sim x$ ]

**value** *val*[ $\sim x$ ]

**value** *exp*[ $\sim x$ ]

**value**  $\sim x$

**end**

**theory** *Phase*

**imports** *Main*

**begin**

**ML-file** *map.ML*

**ML-file** *phase.ML*

**end**

## 1.1 Canonicalization DSL

**theory** *Canonicalization*

**imports**

*Markup*

*Phase*

*HOL-Eisbach.Eisbach*

**keywords**

*phase* :: *thy-decl* **and**

*terminating* :: *quasi-command* **and**

*print-phases* :: *diag* **and**

*export-phases* :: *thy-decl* **and**

*optimization* :: *thy-goal-defn*

**begin**

**print-methods**

**ML** <

*datatype* 'a *Rewrite* =

*Transform* of 'a \* 'a |

*Conditional* of 'a \* 'a \* *term* |

*Sequential* of 'a *Rewrite* \* 'a *Rewrite* |

*Transitive* of 'a *Rewrite*

*type* *rewrite* = {  
  *name*: *binding*,  
  *rewrite*: *term Rewrite*,  
  *proofs*: *thm list*,  
  *code*: *thm list*,  
  *source*: *term*  
}

*structure* *RewriteRule* : *Rule* =

*struct*

*type* *T* = *rewrite*;

(\*

*fun* *pretty-rewrite ctxt (Transform (from, to))* =

*Pretty.block* [

*Syntax.pretty-term ctxt from*,

*Pretty.str*  $\mapsto$  ,

*Syntax.pretty-term ctxt to*

  ]

| *pretty-rewrite ctxt (Conditional (from, to, cond))* =

*Pretty.block* [

*Syntax.pretty-term ctxt from*,

*Pretty.str*  $\mapsto$  ,

*Syntax.pretty-term ctxt to*,

*Pretty.str* *when* ,

*Syntax.pretty-term ctxt cond*

```

    ]
  | pretty-rewrite - - = Pretty.str not implemented*)

fun pretty-thm ctxt thm =
  (Proof-Context.pretty-fact ctxt (, [thm]))

fun pretty ctxt obligations t =
  let
    val is-skipped = Thm-Deps.has-skip-proof (#proofs t);

    val warning = (if is-skipped
      then [Pretty.str (proof skipped), Pretty.brk 0]
      else []);

    val obligations = (if obligations
      then [Pretty.big-list
        obligations:
        (map (pretty-thm ctxt) (#proofs t)),
        Pretty.brk 0]
      else []);

    fun pretty-bind binding =
      Pretty.markup
        (Position.markup (Binding.pos-of binding) Markup.position)
        [Pretty.str (Binding.name-of binding)];

    in
      Pretty.block ([
        pretty-bind (#name t), Pretty.str : ,
        Syntax.pretty-term ctxt (#source t), Pretty.fbrk
      ] @ obligations @ warning)
    end
  end

structure RewritePhase = DSL-Phase(RewriteRule);

val - =
  Outer-Syntax.command command-keyword <phase> enter an optimization phase
  (Parse.binding --| Parse.$$$ terminating -- Parse.const --| Parse.begin
   >> (Toplevel.begin-main-target true o RewritePhase.setup));

fun print-phases print-obligations ctxt =
  let
    val thy = Proof-Context.theory-of ctxt;
    fun print phase = RewritePhase.pretty print-obligations phase ctxt
  in
    map print (RewritePhase.phases thy)
  end
end

```

```

fun print-optimizations print-obligations thy =
  print-phases print-obligations thy |> Pretty.writeln-chunks

val - =
  Outer-Syntax.command command-keyword ⟨print-phases⟩
  print debug information for optimizations
  (Parse.opt-bang >>
    (fn b => Toplevel.keep ((print-optimizations b) o Toplevel.context-of)));

fun export-phases thy name =
  let
    val state = Toplevel.theory-tolevel thy;
    val ctxt = Toplevel.context-of state;
    val content = Pretty.string-of (Pretty.chunks (print-phases false ctxt));
    val cleaned = YXML.content-of content;

    val filename = Path.explode (name ^ ".rules");
    val directory = Path.explode optimizations;
    val path = Path.binding (
      Path.append directory filename,
      Position.none);
    val thy' = thy |> Generated-Files.add-files (path, content);

    val - = Export.export thy' path [YXML.parse cleaned];

    val - = writeln (Export.message thy' (Path.basic optimizations));
  in
    thy'
  end

val - =
  Outer-Syntax.command command-keyword ⟨export-phases⟩
  export information about encoded optimizations
  (Parse.text >>
    (fn name => Toplevel.theory (fn state => export-phases state name)))
,

```

**ML-file** rewrites.ML

```

fun rewrite-preservation :: IRExp Rewrite ⇒ bool where
  rewrite-preservation (Transform x y) = (y ≤ x) |
  rewrite-preservation (Conditional x y cond) = (cond ⟶ (y ≤ x)) |
  rewrite-preservation (Sequential x y) = (rewrite-preservation x ∧ rewrite-preservation
y) |
  rewrite-preservation (Transitive x) = rewrite-preservation x

```

```

fun rewrite-termination :: IRExp Rewrite ⇒ (IRExp ⇒ nat) ⇒ bool where
  rewrite-termination (Transform x y) trm = (trm x > trm y) |

```

```

rewrite-termination (Conditional x y cond) trm = (cond  $\longrightarrow$  (trm x > trm y)) |
rewrite-termination (Sequential x y) trm = (rewrite-termination x trm  $\wedge$  rewrite-termination
y trm) |
rewrite-termination (Transitive x) trm = rewrite-termination x trm

```

```

fun intval :: Value Rewrite  $\Rightarrow$  bool where
  intval (Transform x y) = (x  $\neq$  UndefVal  $\wedge$  y  $\neq$  UndefVal  $\longrightarrow$  x = y) |
  intval (Conditional x y cond) = (cond  $\longrightarrow$  (x = y)) |
  intval (Sequential x y) = (intval x  $\wedge$  intval y) |
  intval (Transitive x) = intval x

```

```

fun size :: IRExp  $\Rightarrow$  nat where
  size (UnaryExpr op e) = (size e) * 2 |
  size (BinaryExpr op x y) = (size x) + ((size y) * 2) |
  size (ConditionalExpr cond t f) = (size cond) + (size t) + (size f) + 2 |
  size (ConstantExpr c) = 1 |
  size (ParameterExpr ind s) = 2 |
  size (LeafExpr nid s) = 2 |
  size (ConstantVar c) = 2 |
  size (VariableExpr x s) = 2

```

**named-theorems** *size-simps size simplification rules*

```

method unfold-optimization =
  (unfold rewrite-preservation.simps, unfold rewrite-termination.simps,
   unfold intval.simps,
   rule conjE, simp, simp del: le-expr-def, force?)
| (unfold rewrite-preservation.simps, unfold rewrite-termination.simps,
   rule conjE, simp, simp del: le-expr-def, force?)

```

```

method unfold-size =
  (unfold size.simps, simp add: size-simps del: le-expr-def)?
| (simp add: size-simps del: le-expr-def)?
| (unfold size.simps)?

```

**print-methods**

```

ML <
structure System : RewriteSystem =
struct
  val preservation = @{const rewrite-preservation};
  val termination = @{const rewrite-termination};
  val intval = @{const intval};
end

```

```

structure DSL = DSL-Rewrites(System);

```

```

val - =

```



```

Outer-Syntax.local-theory-to-proof command-keyword ⟨optimization⟩
  define an optimization and open proof obligation
  (Parse-Spec.thm-name : -- Parse.term
    >> DSL.rewrite-cmd);
>
end

```