

Topic: SLO # 08 Waves

Disturbance in a medium

Wave:- Wave transfer energy from one place to another.

There are two types of waves.

- i) Mechanical Waves:- These are the waves which required medium for their propagation.

Examples:- Sound waves, Water waves.

- ii) Electromagnetic Waves ~~H<sub>2</sub>O~~

These are the waves which don't required medium for their propagation.

Examples:- Light waves, ~~radio~~ Gamma rays,

X-rays.

- \* Progressive Waves:- The wave ~~not~~ which transfer energy from the source of disturbance.

- \* Transverse Waves:- These are the waves in which particle of the medium are displaced in a direction perpendicular to the direction of propagation of wave.

- \* Longitudinal Waves

These are the waves in which particle of the medium are displaced in a direction parallel to the direction of propagation of wave.



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\* Periodic Waves:-

These are the waves which repeat itself in equal interval of time.

\* Wavelength:-

Distance between any two consecutive crest or trough is called wavelength.

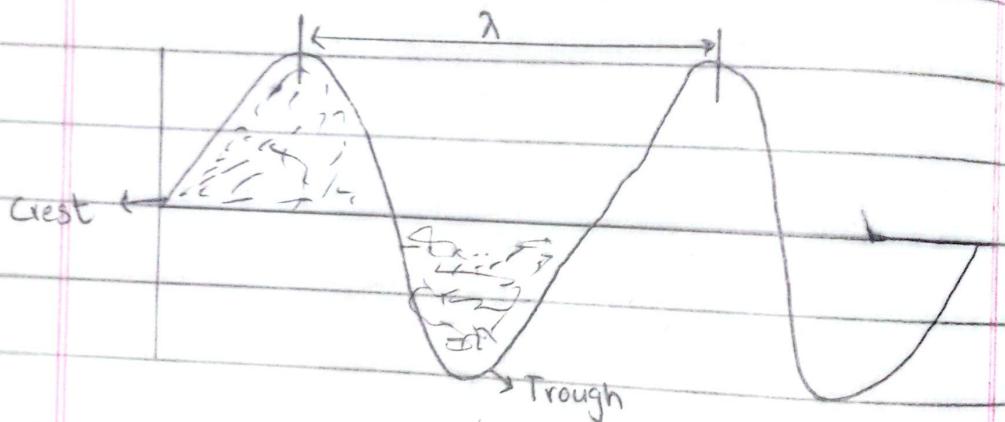
It is denoted by  $\lambda$ .

\* Crest :-

The above portion of wave from mean position.

\* Trough :-

The below portion of wave from mean position.



\* Wave equation:-

Velocity = Displacement

time

$$V = \frac{\lambda}{t}$$

$$V = \lambda \times f$$

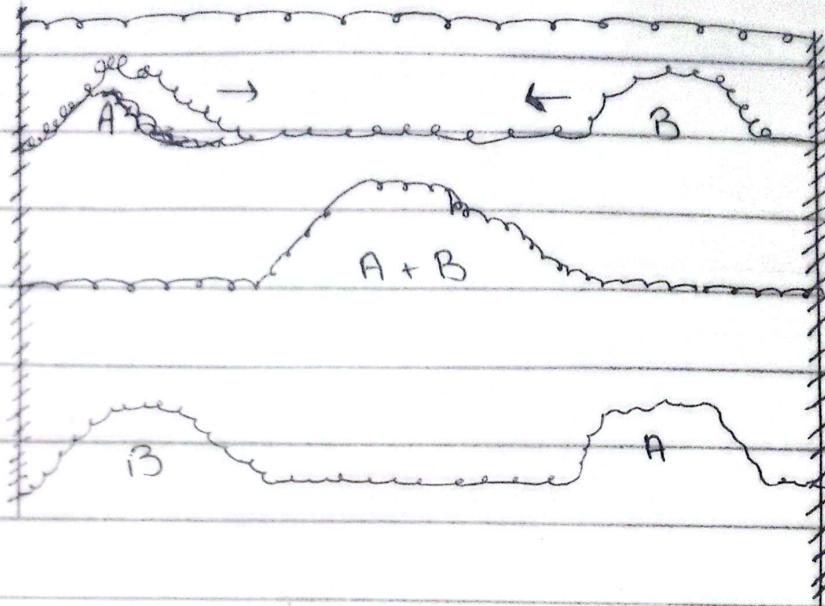
$$\therefore f = \frac{1}{t}$$

$V = f \lambda$  This is called wave equation

Topic: Physics.

\* Principle of superposition:-

When two waves meet in a medium their resultant amplitude is equal to the sum of their individual amplitudes of two waves.



Interference of Waves:-

When two waves having same frequency and travelling in same direction meet in a <sup>same</sup> ~~some~~ speed medium then at some points they rise the effect of each others and at some other points they cancel the effects of each others. This is called interference of two waves.

There are two types of interference of waves:-

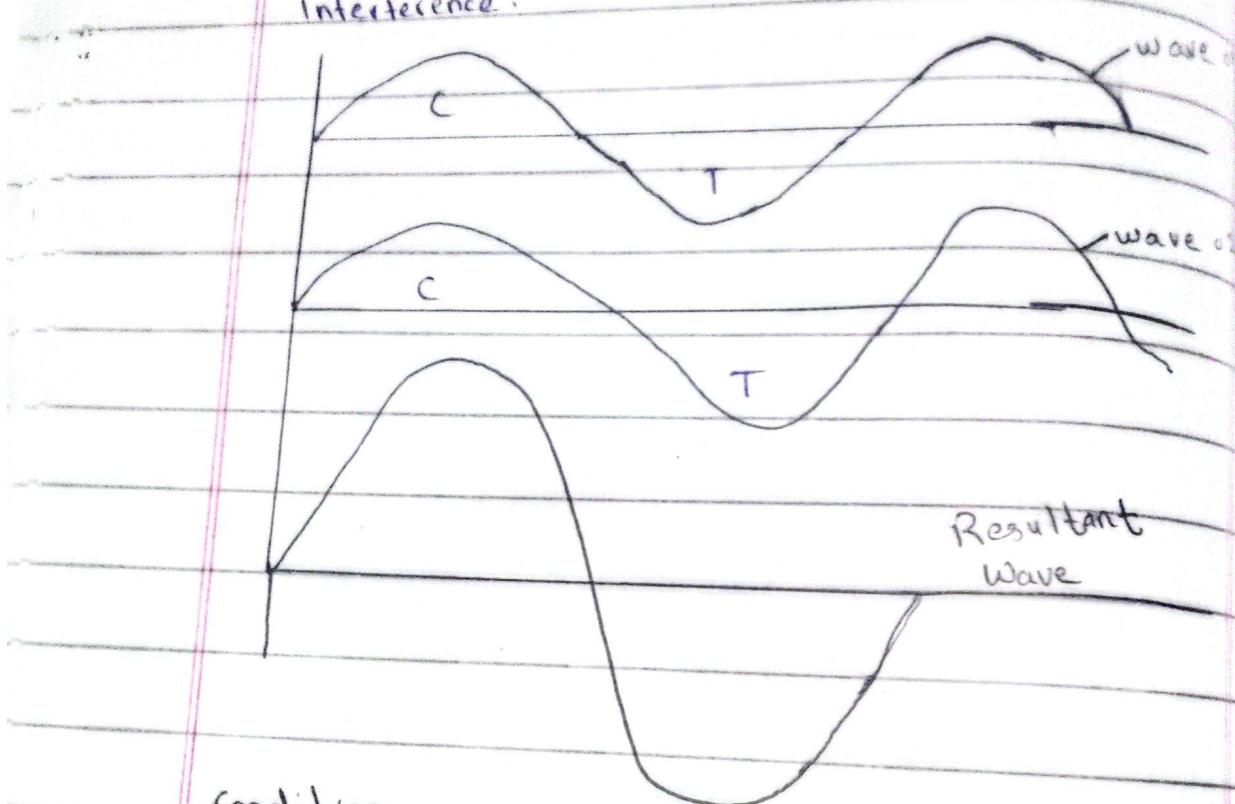
a) Constructive Interference:-

When two waves meet in a medium in such



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a way that crest of one wave fall on crest of other waves and trough of one wave falls on trough of other wave they rise the effects of each other and this type of interference is called constructive interference.



Condition:-

$$\text{Path of difference} = \Delta s = n\lambda$$

Where  $n = 0, 1, 2, 3, \dots$

a)

b)

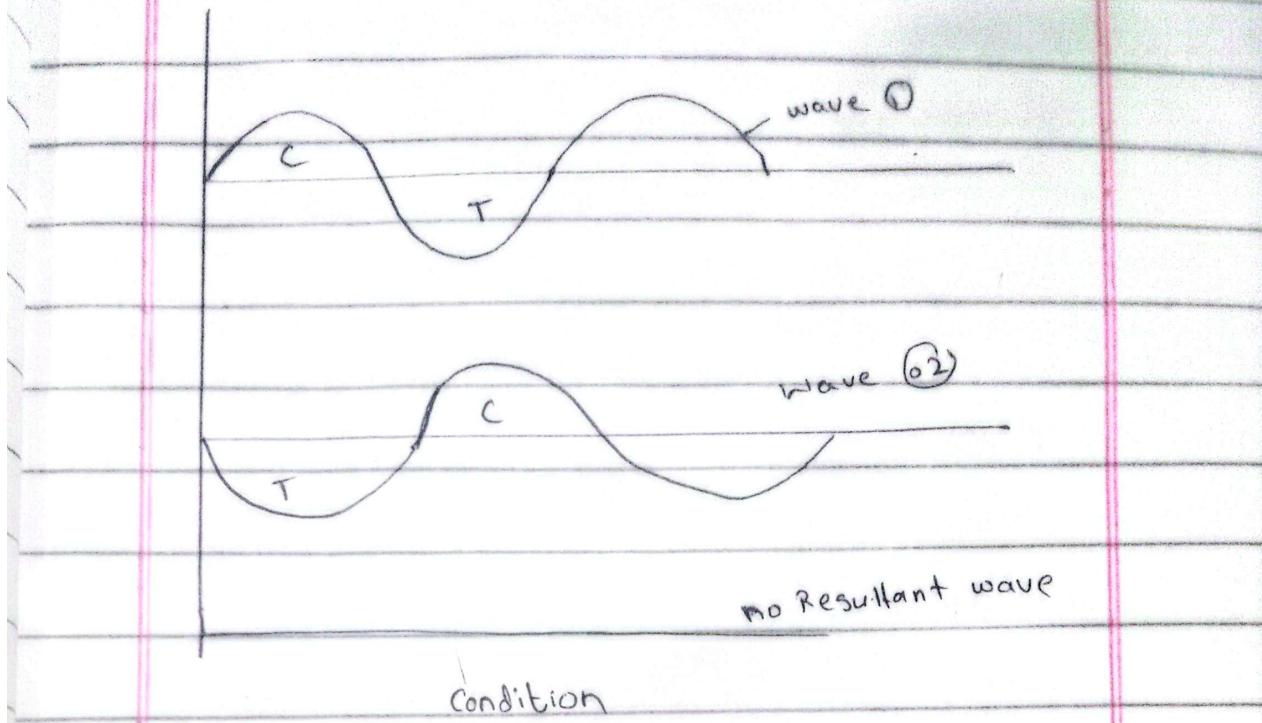
Destructive Interference:-

When two waves meet in a medium is such a way that crest of one wave falls on trough of other wave and trough of one wave falls on crest of other wave. In this case

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they will cancel the effect of each other  
and this type of interference is called destructive  
interference.



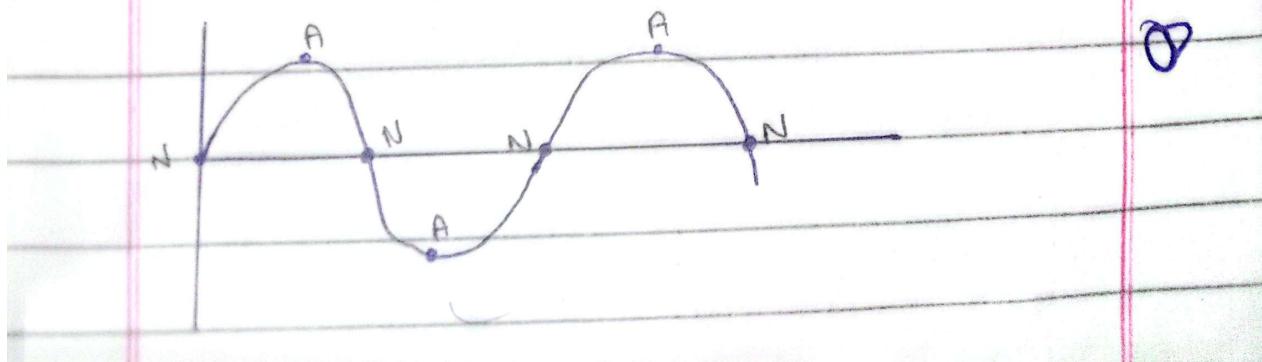
$$\text{Path difference} = \Delta S = (2n+1) \frac{\lambda}{2}$$

\* Beats:- Fluctuation of sound wave is called

Beats. Pg # 175 fig r 8.9 Refrence.

\* Node:- It is a point when amplitude is zero.

\* Anti-node:- It is a point where amplitude is max.



## Topic: Physics

- \* Stationary Waves

Stationary waves do not transfer energy from one place to another

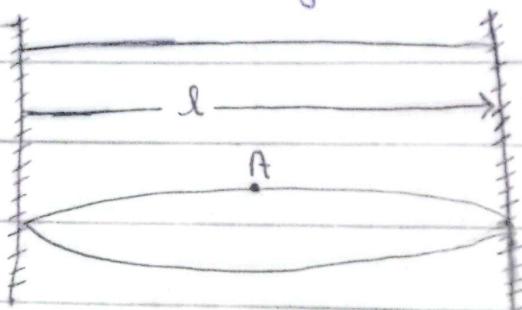
- \* Energy oscillates b/w nodes and antinodes

- \* Stationary Waves in stretched string

Case ①:-

Consider a string of length  $l$  fixed at both ends.

If the string is plucked at the center.



$$L = \frac{\lambda_1}{2}$$

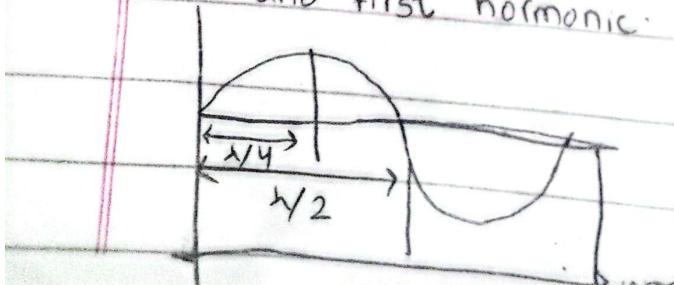
$$f_1 = \frac{V}{\lambda_1}$$

$$\lambda_1 = 2L$$

$$\text{As } V = f\lambda$$

$$f_1 = \frac{V}{2L}$$

This is called fundamental frequency and first harmonic.



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Case 2 :-If the string is plucked at  $1/4$ .

$$v = f\lambda$$

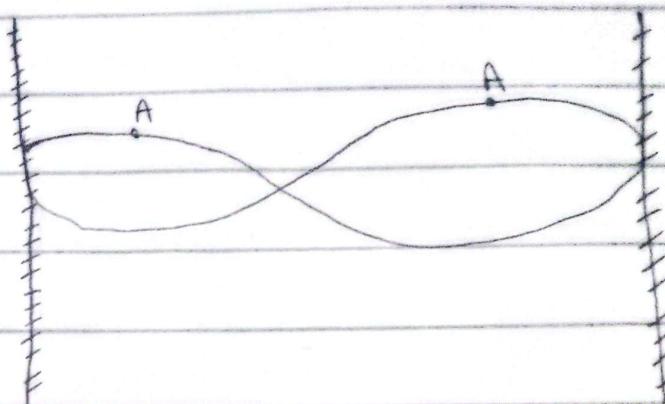
$$f_2 = \frac{v}{\lambda_2}$$

$$f_2 = v/l$$

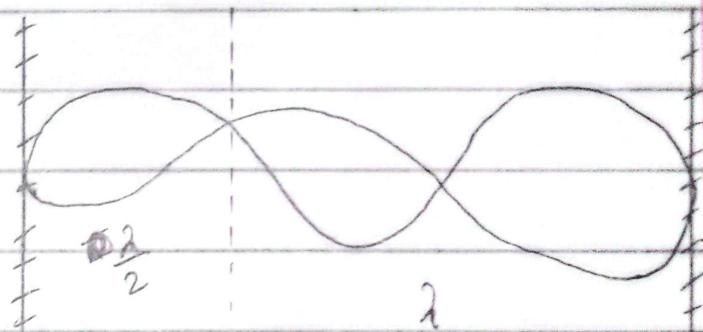
$$f_2 = 2 \left( \frac{v}{2l} \right)$$

$$l = \lambda^2$$

$$\therefore f_2 = 2f_1$$

Case 3 :-

$$l = \lambda + \frac{\lambda}{2}$$



$$\frac{2\lambda + \lambda}{2}$$

$$\text{As } v = f\lambda$$

$$f_3 = v/\lambda_3 \quad \text{This is called}$$

$$l = \frac{3\lambda}{2}$$

$$f_3 = \frac{v}{2\lambda/3} \quad \text{third harmonic}$$

& second overtone.

$$2l = 3\lambda$$

$$f_3 = 3 \left( \frac{v}{2l} \right)$$

$\lambda_3 =$	$\frac{2l}{3}$
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$$f_3 = 3f_1$$

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$$f_2 = 2f_1$$

$$f_3 = 3f_1$$

$$f_4 = 4f_1$$

The general relation

$$f_n = nf_1$$

where  $n = 1, 2, 3, 4, \dots$

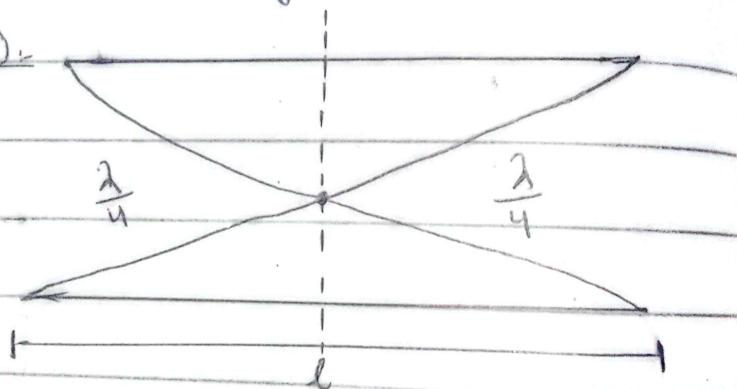
$$\lambda_n = \frac{2L}{n}$$

\* Stationary Waves in air column

- a) Open pipe ~~or~~ open pipe is a pipe which is open from both ends. At open end always anti-node is formed.

At closed end always node is formed.

\* Case(1)-



$$l = \frac{\lambda}{4} + \frac{\lambda}{4}$$

$$N = f\lambda$$

$$f_1 = \frac{V}{\lambda_1}$$

$$l = \frac{2\lambda}{4^2}$$

$$f_1 = V/2L$$

$$l = \frac{\lambda}{2}$$

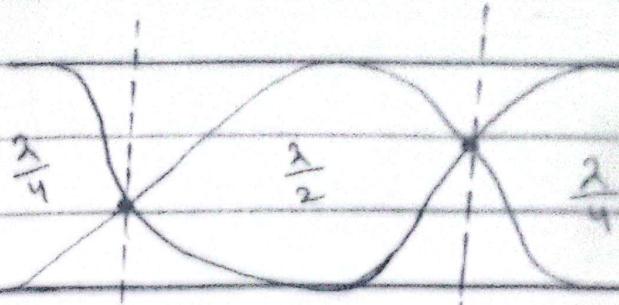
$$\lambda_1 = 2L$$

This is called fundamental frequency and first harmonic.

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Case(2)



$$l = \frac{3}{4} + \frac{3}{2} + \frac{3}{4} \quad \text{as } v = 5\lambda$$

$$\frac{2+2+2}{4}$$

$$f_2 = v/2l \approx f_{n=2}$$

$$f_2 = v/l$$

$$2\left(\frac{v}{2l}\right) \quad f_2 = 2f_1$$

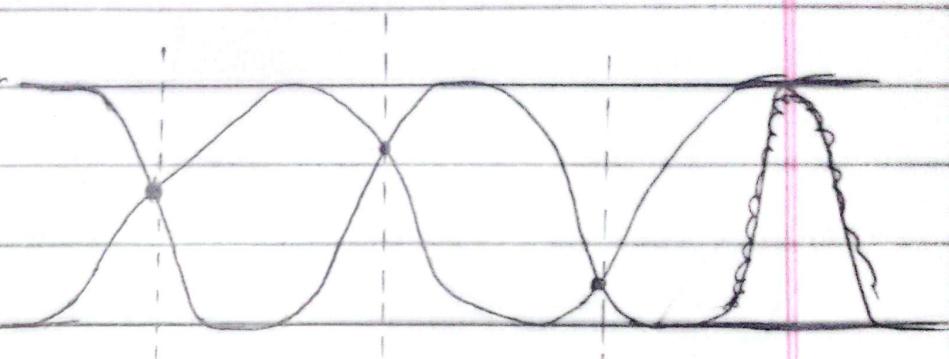
$$l = \frac{4\lambda}{4}$$

This is called second

harmonic &amp; first overtone.

$$l = 2\lambda$$

\* Case(3)r



$$l = \frac{6\lambda}{4}$$

$$\text{As } v = f\lambda$$

$$f_3 = v/2l$$

$$l = \frac{3\lambda}{2}$$

$$f_3 = \frac{v}{2l} \quad \sqrt{\frac{2l}{3}}$$

$$\frac{2l}{3} = \lambda_3$$

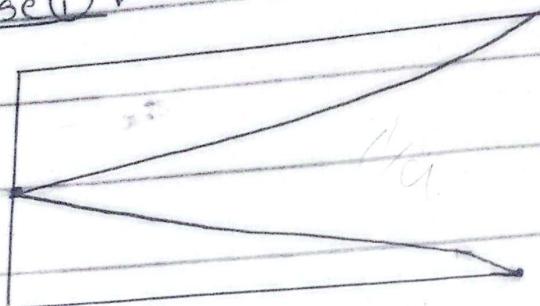
$$f_3 = 3\left(\frac{v}{2l}\right)$$

$$(v/2l)^3$$

$$f_3 = 3f_1$$

b) Close Pipe <sup>Date</sup>  
Close pipe is a pipe which is open from one end and other end is closed.

Case 1



$$l = \frac{2}{4}$$

$$\lambda = 4l$$

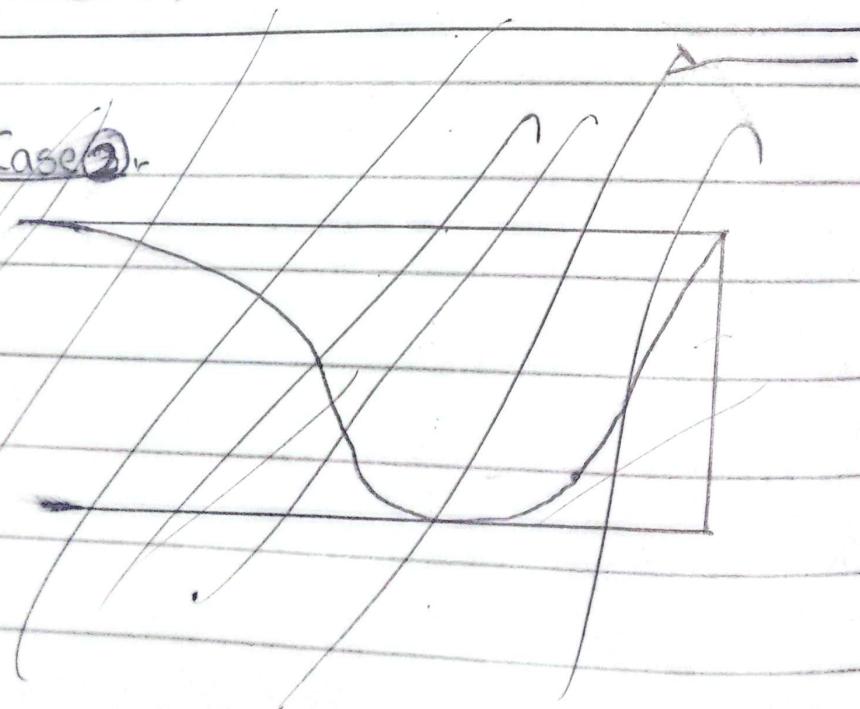
$$\text{As } V = f\lambda$$

$$f_1 = V/4l$$

$$f_1 = \frac{V}{4l}$$

This is called fundamental and first Harmonic.

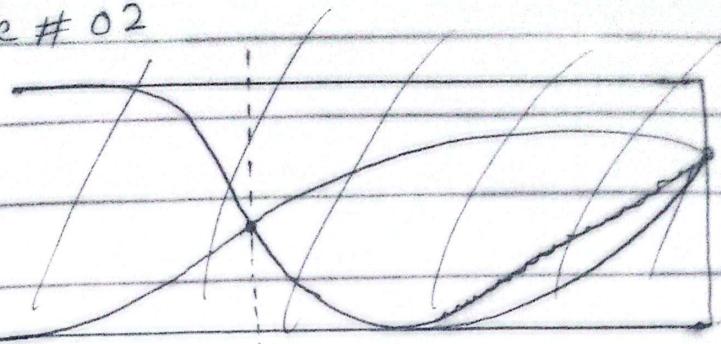
Case 2



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Case # 02



$$l = \frac{3\lambda}{4}$$

$$As \quad V = f\lambda$$

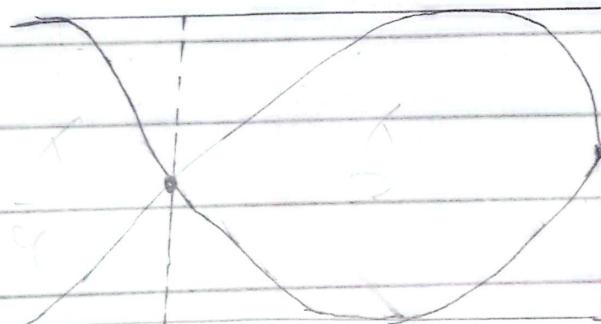
$$\frac{4l}{3} = \lambda_2$$

$$f_2 = V/\lambda_2$$

$$\frac{4l}{3}$$

$$f_2 = \frac{V}{\frac{4l}{3}} = f_2 = 3(V)_{4l}$$

$$f_2 = 3f_1$$

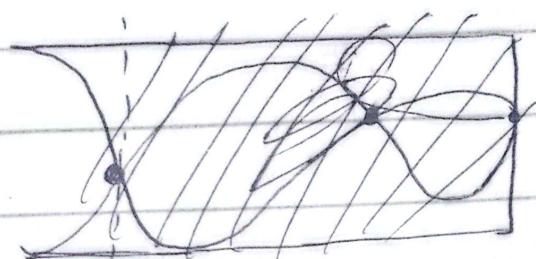


Topic

# Physics

\* Close Pipe

case 03



$$l = 2 \frac{2}{4}$$

$$\frac{4\lambda + 2}{4}$$

$$l = \frac{5\lambda}{4}$$

$$4l = 5\lambda$$

$$\lambda_3 = 4l/5$$

$$v = f_2$$

$$f_3 = v/2\lambda \quad \therefore f_3 = 5f_1$$

$$f_3 = \frac{v}{4l/5}$$

$$f_3 = 5 \left( \frac{v}{4l} \right)$$

$$f_2 = 3f_1$$

$$f_3 = 5f_1$$

$$f_4 = 7f_1$$

The general relation  $f_n = n f_1$

$$n = 1, 3, 5, 7, \dots$$

## \* Doppler's Effect

The apparent change in the frequency of sound is called Doppler's effect.

\* Doppler's effect is applicable to both sound waves & electromagnetic waves.

### Cases:-

a) Case #01:- When an observer is moving towards the stationary source.



From wave equ.

$$v = f \lambda$$

$$f_A = \left( \frac{v + u_o}{v} \right) f$$

$$\lambda = v/f$$

$$f_A = \frac{v + u_o}{\lambda} \quad \text{①} \quad \text{Then}$$

$$f_A > f$$

Again

$$v = f \lambda$$

$$\lambda = v/f$$

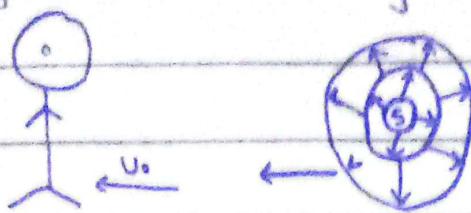
Put in eqn ①

$$f_A = \frac{v + u_o}{v/f}$$

Result:

The apparent frequency of sound increases.

- \* Case #2: When an observer is moving away from the stationary source.



from wave equ

$$v = f\lambda$$

$$f = v/\lambda$$

$$f_B = \frac{v - u_o}{\lambda} \quad \text{--- (1)}$$

Again:-

$$v = f\lambda$$

$$\lambda = v/f$$

Put in equ - ①

$$f_B = \frac{v - u_o}{v/f}$$

$$v/f$$

$$f_B = \left( \frac{v - u_o}{v} \right) f$$

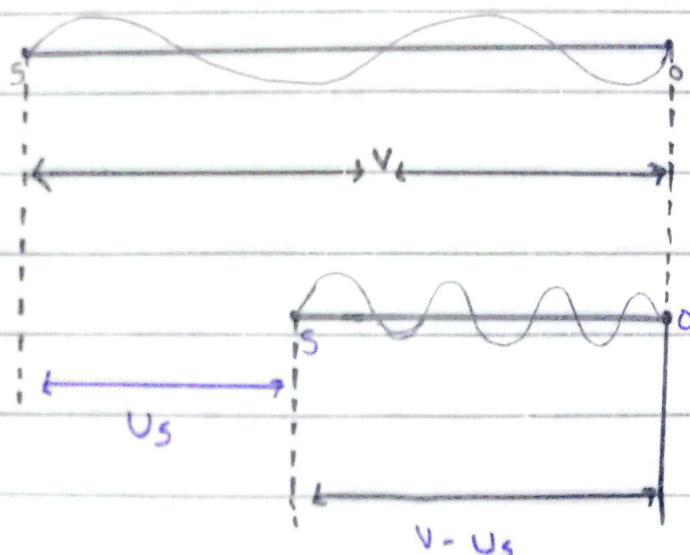
$$\frac{v - u_o}{v} < 1$$

$$\checkmark$$

Then  $f_B < f$

Result: The apparent frequency of sound decreases.

- \* Case #3: When a source is moving towards the stationary observer.



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From wave equ:

$$V = f \lambda$$

$$\lambda = \frac{V}{f}$$

$$\lambda = \frac{V - U_s}{f} \quad \text{①}$$

$$f_c = \frac{V}{V - U_s}$$

$$f_c = \left( \frac{V}{V - U_s} \right) f$$

Again:-

$$V = f \lambda$$

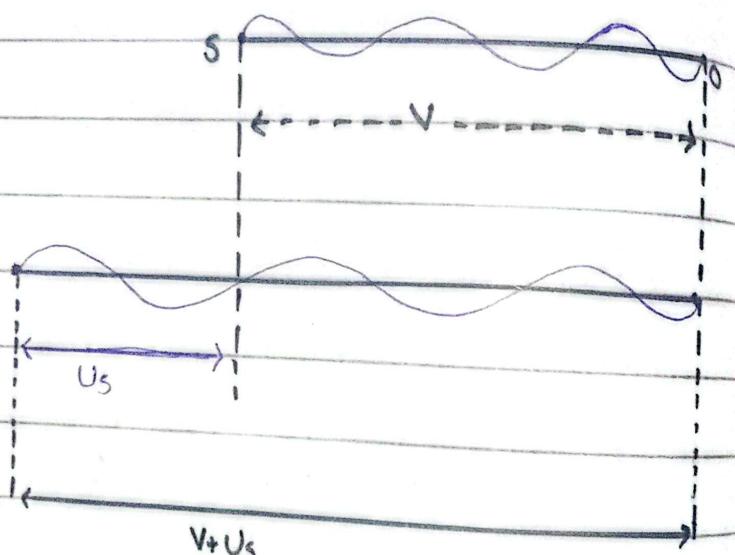
$$f_c = V / \lambda$$

As  $V \rightarrow 1$

$$V - U_s$$

$$f_c > f$$

\* Case # 04:- When a source is moving away from stationary observer.



From wave equ

$$V = f \lambda$$

$$\lambda = \frac{V}{f}$$

$$\lambda = \frac{V + U_s}{f} \quad \text{①}$$

Again  $V = f \lambda$

$$f_c = \frac{V}{V + U_s}$$

$$f_c = \left( \frac{V}{V + U_s} \right) f$$

$$\frac{V}{V + U_s} < 1 \quad f_c < f$$

## Topic Physics.

\* Doppler's effect.

Case # 05:- When both observer and source are moving towards each others.

$$f_B = \left( \frac{v + u_o}{v - u_s} \right) f$$

Case # 06:- When both observer and source are moving away from each others.

$$f_F = \left( \frac{v - u_o}{v + u_s} \right) f$$

\* Applications:-

- a) Radar system:- It is a device which transmits radio waves to determine the elevation and speed of Air plane. If an air plane approaches towards toward the radar, then the wavelength of the wave reflected from air plane would be shorter.

If an air plane moving away from the radar then the wavelength would be longer.

- b) Sonar (sound navigation and Ranging):-

- c) Bat.