

# Investigation of the Cluster Structure of $^9\text{Be}$ by Reactions with a Deuteron Beam

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**Abstract.** Angular distributions of protons, deuterons, tritons and alpha particles emitted in the  $d + ^9\text{Be}$  reaction at  $E_{lab}=19.5$  and  $35.0$  MeV are measured. The elastic channel is analysed in the framework of both the Optical Model and the Coupled Channel approach. Two kind of optical potentials are analysed: the semi-microscopic Double Folding potential and the phenomenological Woods-Saxon potential. The deformation parameter  $\beta_2$  is obtained for the transition  $\frac{5}{2}^- \rightarrow \frac{3}{2}^-$  in  $^9\text{Be}$ . The (d,p) and (d,t) one nucleon exchange reactions are analysed within the coupled reaction channel approach. The spectroscopic amplitudes for the different nuclear cluster configurations are calculated. Differential cross sections for the reaction channel  $^9\text{Be}(d,\alpha)^7\text{Li}$  are calculated within the coupled reaction channel method including all possible reaction mechanisms. Corresponding contributions to the cross sections are analysed.

*Keywords:* cluster structure, optical model, CRC, DWBA, spectroscopic amplitudes, double folding, elastic and inelastic scattering, few-nucleon transfer reactions

## 1. Introduction

The cluster structure of nuclei arises from a correlated motion of nucleons inside a nucleus. In this regime a simple subgroup can be seen as a single particle. This kind of behaviour can give insights into numerous characteristics of the nucleus, as well as affect the processes of nuclear reactions. Investigation of the cluster structure in nuclei is still one of the priority problems of modern nuclear physics in connection with the intensive developments of experimental devices.

There is a row of stable nuclei exhibiting the cluster structure, but  ${}^9\text{Be}$  is particularly worthy of attention due to the following reasons:

- stable nucleus with the low binding energies of neutron  $S_n=1.665$  MeV, and  $\alpha$ -particle  $S_\alpha=2.462$  MeV [1];
- the deformed shape reflected in the nuclear quadrupole moment,  $Q=+52.9$  mb [2];
- the Borromean structure of the ground state;

These aspects led to take  ${}^9\text{Be}$  as a subject for fundamental as well as applied researches studies.

Regarding nuclear technologies,  ${}^9\text{Be}$  is a good wall material in thermonuclear devices [3, 4]. For instance, for fusion device types a value of some dozens of percent of soft wall material is expected in the case of  ${}^9\text{Be}$  [4]. The nucleus has been chosen as it represents the best compromise based on its ability to be well split into two energetic  $\alpha$ -particles by the use of  $\gamma$  and  $e^-$ , which are efficient promoters of thermonuclear burning. Since they can be confined by electromagnetic fields and their energy affects the temperature of the burning zone.

Scattering of the simplest projectile, such as  ${}^1\text{H}$  or  ${}^3\text{He}$ , on a target is a standard tool for fundamental study the structure of nuclei. This method involves measuring the angular distribution of the nuclear reaction products. It is well known that the energy and angular distributions of projectile-like particles give information about internal structure of target-like nuclei.

In our previous works [5, 6, 7] the  ${}^3\text{He}$  interaction with  ${}^9\text{Be}$  was studied and angular distributions of the reaction products in the following exit channels:  ${}^3\text{He}+{}^9\text{Be}$ ,  ${}^5\text{He}+{}^7\text{Be}$ ,  ${}^5\text{Li}+{}^7\text{Li}$ ,  ${}^6\text{Be}+{}^6\text{He}$ , and  ${}^6\text{Li}+{}^6\text{Li}$ , were measured. The obtained data were analysed within the framework of the Optical Model (OM), the Coupled Channel (CC) and the distorted wave Born approximation (DWBA) approaches. The performed

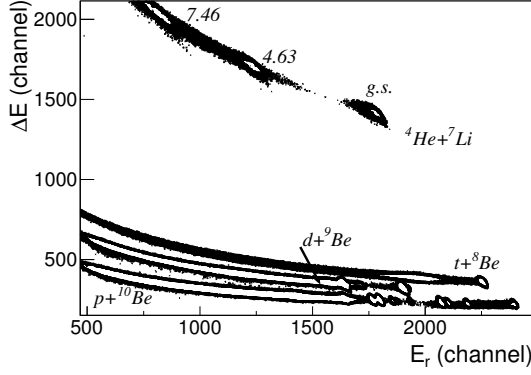
analysis of the experimental data showed sensitivity of cross section on the potential parameters in the exit channels. Moreover, these experiments were designed to study the breakup reactions with  ${}^9\text{Be}$  in attempt to determine contributions of the channels through the  ${}^8\text{Be}+n$  and  ${}^5\text{He}+\alpha$  structure within the inclusive measurements. It was found that the ratio  $2.7 \div 1$  could be assigned to the contributions of these two channels respectively. The determined value justifies that the  ${}^5\text{He}+\alpha$  breakup channel plays an important role as well.

Basing on the Borromean structure of  ${}^9\text{Be}$ , special attention was focused on the breakup processes resulting in the  ${}^9\text{Be}({}^6\text{Li}, {}^6\text{Li}){}^9\text{Be}^*$  nuclear reaction [8, 9]. The excited nucleus  ${}^9\text{Be}^*$  can decay either directly into the  $\alpha + \alpha + n$  three-body system or through one of the unstable nuclei, such as  ${}^5\text{He}$  and  ${}^8\text{Be}$ . Thereby, these relatively recent experimental studies explicitly confirm the cluster structure of  ${}^9\text{Be}$ . The calculated branching ratios show that the low lying excited states, at  $E_x < 4.0$  MeV, are mostly populated with the  ${}^8\text{Be}+n$  configuration. In other case, the  ${}^5\text{He}+\alpha$  configuration plays a significant role.

Another aspect of finding the cluster structure is its attendance in the nuclear reaction mechanisms. Indeed, since the papers of Detraz *et al* [10, 11], the multiparticle-multihole structures have been expected at rather low excitation energies in nuclei. In this case, it can be understood that the nucleons are transferred as a whole strongly correlated cluster, which has the internal quantum numbers of a free particle.

The interaction of deuteron and alpha particles with  ${}^9\text{Be}$  was studied with regard to the cluster structure [12, 13]. The interaction potential of colliding nuclei was built within the framework of the Double Folding model using the three body wave function. Approbation of the double folded potential was carried out within the OM, DWBA at laboratory energies 10-30 MeV/nucleon. Comparison of theoretical cross sections with experimental data led to the applicability of the double folding potential based on the three body wave function.

The current work devoted to the investigation of the cluster structure of the  ${}^9\text{Be}$  nucleus studying the nuclear reactions caused by a deuteron beam at 19 MeV and 35 MeV energies. In the exit channel the simplest particles, such as p, d, t, and  $\alpha$ -particles, were registered and their angular distributions were obtained. A comparative analysis of experimental data



**Figure 1.** Particle identification plots for the products of the  $^2\text{H}+^9\text{Be}$  reaction:  $p$ ,  $d$ ,  $t$ , and  $^4\text{He}$ .  $\Delta E$  is the energy loss and  $E_r$  is the residual energy. Excited states for the  $^7\text{Li}$  reaction channel  $^7\text{Li}+\alpha$  are indicated.

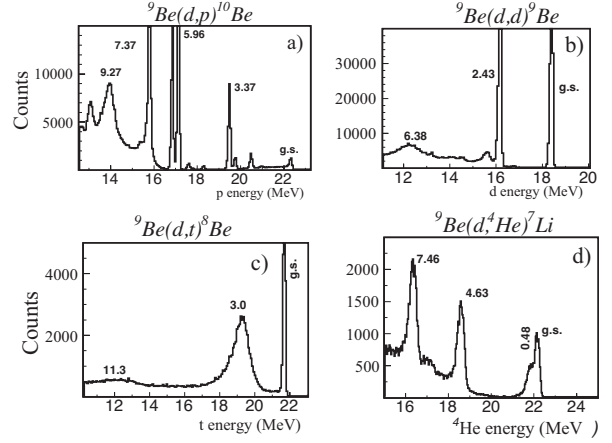
and theoretical calculations has been performed.

## 2. Experimental Method

The experiment has been performed at the INP (Řež, Czech Republic) and in the Physics Department of Jyväskylä University (Jyväskylä, Finland). The beam energy of  $^2\text{H}$  ions produced from the cyclotrons were at energies 19.5 and 35 MeV. The average beam current during the experiment was maintained at 20 nA. The self-supporting  $^9\text{Be}$  target was prepared from a thin beryllium foil with the 99 % purity. A set of four telescopes was used with the purpose of registering the simplest particle of output channels. Each telescope was contained the  $\Delta E_0$ ,  $\Delta E$ ,  $E_r$  detectors with the respective thickness of 12  $\mu\text{m}$ , 100  $\mu\text{m}$  and 3 mm. To detect reaction product in narrow divergence, telescopes were mounted at a distance of  $\sim 25$  cm from the target. Each telescope was shielded by a Cu-Pb collimator with thickness of 3 mm and hole with diameter of 3 mm. The telescopes were mounted on rotating supports, which allow us to obtain data from  $\theta_{lab} = 20^\circ$  to  $107^\circ$  in steps of  $1 - 2^\circ$ .

The particles were identified based on the energy-loss measurements of  $\Delta E$  and the residual energy  $E_r$ , i.e., by the so-called  $\Delta E$ - $E_r$  method. An example of two-dimensional plots (yield vs. energy loss  $\Delta E$  and residual energy  $E_r$ ) is shown in Fig. 1.

The capability of current experimental technique is in identification of the particles  $p$ ,  $d$ ,  $t$ , and  $\alpha$  and in the determination of their total deposited energies. The spectra of total deposited energy are shown in Fig. 2. All the peaks from Fig. 2 has been identified and assigned to the ground and the excited states of the  $^{10}\text{Be}$ ,  $^9\text{Be}$ ,  $^8\text{Be}$ ,  $^7\text{Li}$  nuclei as the complementary products for the detected particles



**Figure 2.** Total deposited energy spectra measured at  $\theta_{lab}=32^\circ$  for the detected  $p$  (panel a),  $d$  (panel b),  $t$  (panel c), and  $\alpha$  (panel d). The ground and the excited states of  $^7\text{Li}$  for the detected complementary product  $\alpha$  as well as the ground states and the excited states for  $^8\text{Be}$ ,  $^9\text{Be}$ , and  $^{10}\text{Be}$  in the case of detected  $t$ ,  $d$ , and  $p$ , as complementary products, respectively, are unambiguously identified.

$p$ ,  $d$ ,  $t$ ,  $\alpha$ , respectively.

## 3. Data Analysis and Results

### 3.1. Elastic scattering

The theoretical calculations of the deuteron elastic scattering on  $^9\text{Be}$  at 19.5 and 35 MeV energies have been made in the framework of the OM. The model suggests interaction between two colliding nuclei in the following way:

$$U(R) = -V^V(R) - iW^V(R) + iW^D(R) + V^{SO}(R)(\mathbf{l} \cdot \boldsymbol{\sigma}) + V^C(R), \quad (1)$$

where  $V^V$ ,  $W^V$ ,  $W^D$ ,  $V^{SO}$ , and  $V^C$  are volume, imaginary volume and surface, spin-orbit and Coulomb potentials, respectively. In this work the real part of the optical potential were used in two forms, firstly the double folding potential (DF)

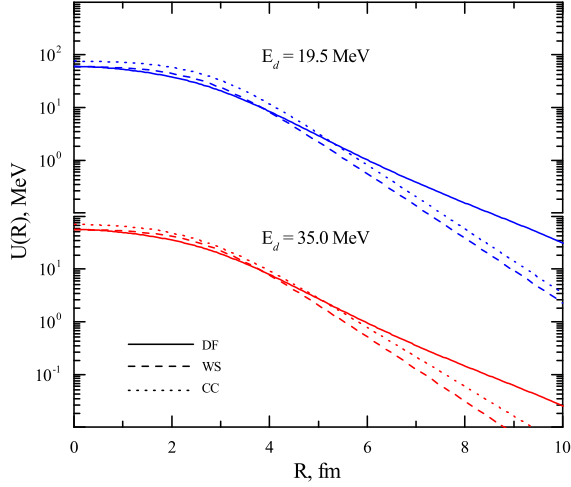
$$V^V(R) = N_R V^{DF}(R) \quad (2)$$

with normalization factor  $N_R$  and, secondly the phenomenological Woods-Saxon (WS) potential:

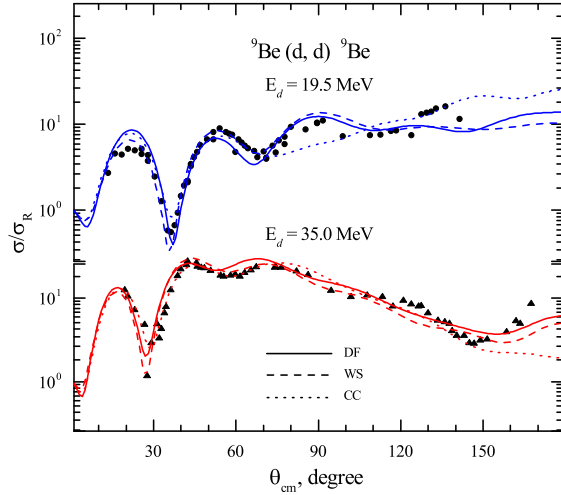
$$V^V(R) = V_0^V f^{R_V, a_V}(R), \quad (3)$$

$$f^{R_V, a_V}(R) = \frac{1}{1 + \exp \frac{R - R_V}{a_V}}. \quad (4)$$

The DF potential was calculated using the effective M3Y-Paris nucleon-nucleon potential and the nuclear-matter-densities of projectile and target nuclei. In order to calculate the  $^9\text{Be}$  matter distribution we applied the  $\alpha + \alpha + n$  three body model [12]. The matter density of the deuteron projectile was chosen in form ... [?].



**Figure 3.** Radial dependence of the real part of the nuclear potentials used in the elastic scattering analysis.



**Figure 4.** The angular distributions of elastic scattering data of d from  $^9\text{Be}$  at laboratory energies 19.5 MeV (full circle) and 35 MeV (full triangle) in comparison with theoretical calculations within optical and couple channel model.

The surface and spin-orbit terms have standard form

$$W^D(R) = -4a_D W_0^D \frac{d}{dR} f^{R_D, a_D}(R), \quad (5)$$

$$V^{SO}(R) = V_0^{SO} \left( \frac{\hbar}{m_\pi c} \right)^2 \frac{1}{R} \frac{d}{dR} f^{R_{SO}, a_{SO}}(R). \quad (6)$$

The Coulomb term has been taken as the interaction of a point-charge with a uniformly charged sphere

$$V^C(R) = \begin{cases} \frac{Z_1 Z_2 e^2}{2R_C} \left( 3 - \frac{R^2}{R_C^2} \right), & \text{for } R \leq R_C, \\ \frac{Z_1 Z_2 e^2}{R}, & \text{for } R > R_C. \end{cases} \quad (7)$$

The parameters of the real and imaginary parts of the optical potential were obtained by fitting the theoretical cross sections to the experimental data at 19.5 MeV and 35 MeV energies. As a starting point one of the available global parametrization [14] was used. The obtained potential parameters after fitting are listed in Table 1 with labels DF and WS for the double folding and Woods-Saxon potentials, correspondingly.

The elastic scattering cross sections were also calculated within the couple channel approach taking into account coupling with the states belonging to the  $^9\text{Be}$  rotational band (see details in the next section). Parameters of the corresponding interaction potential are given in Table 1 with labels CC.

Figure 3 shows the real parts of the different nuclear potentials used here. A specific feature of the double folding potential in comparison with the empirical ones is slow descending in peripheral region  $r \geq 6$  fm. This is due to the broad matter density distribution of the valence neutron in  $^9\text{Be}$ , which also decreases slowly [12].

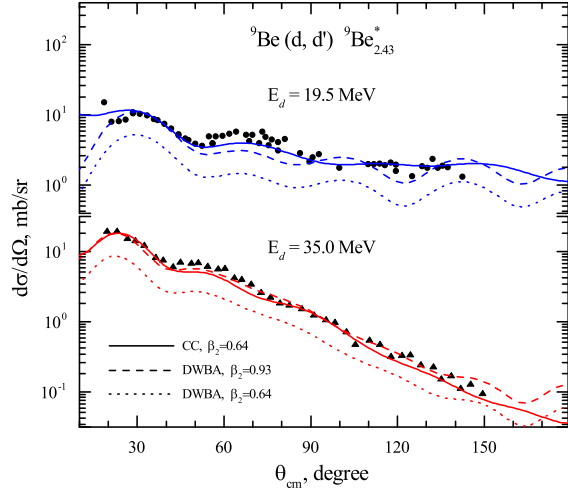
The comparison of the measured data on the elastic scattering with the results of theoretical calculations are plotted in Fig. 4. The cross sections obtained within the optical model with the double folding and Woods-Saxon potentials are shown as the solid and dashed curves. The dotted curve represents the couple channel results. All the calculations provide

**Table 1.** Potential parameters of the d+ $^9\text{Be}$  system used in the OM, the CC and the DWBA calculations.

$E_d$ , MeV	Potential label	$V_0$ , MeV	$r_V^a$ , fm	$a_V$ , fm	$W_0^D$ , MeV	$r_D^a$ , fm	$a_D$ , fm	$V_0^{SO}$ , MeV	$J_V^b$ , MeV fm <sup>3</sup>	$J_W^b$ , MeV fm <sup>3</sup>	$\chi^2$
19.5	DF		$N_R = 1.93$		14.89	0.630	0.854	5.56	617.4	69.7	7.3
35.0	DF		$N_R = 1.81$		14.89	0.630	0.88	5.56	587.7	71.2	5.2
19.5	WS	61.97	0.799	0.707	7.45	0.762	1.044	5.52	575.7	51.4	4.8
35.0	WS	58.01	0.799	0.707	7.52	0.762	1.044	5.52	435.1	51.8	3.4
19.5	CC	77.87	0.831	0.780	7.12	0.816	0.802	2.8	690.9	47.2	8.4
35.0	CC	73.9	0.752	0.770	7.47	0.816	0.802	2.8	524.0	49.6	7.1

<sup>a)</sup> Radii of the potential were defined as  $R_i = r_i (A_P^{1/3} + A_T^{1/3})$ .

<sup>b)</sup> The volume integrals are divided by  $(A_P + A_T)$  value.



**Figure 5.** The cross sections of inelastic scattering  ${}^9\text{Be}(d,d){}^9\text{Be}^*$  ( $E_{exc}=2.43$  MeV) at laboratory energies 19.5 MeV (full circle) and 35 MeV (full triangle). Theoretical curves are described in the text.

good description of the elastic scattering cross sections that is confirmed by the  $\chi^2$  values (see in Table 1).

### 3.2. Inelastic scattering

The CC and the DWBA approaches have been applied to analyse the measured inelastic scattering data corresponding to the  ${}^9\text{Be}(5/2^-, 2.43$  MeV) excitation. Calculations were performed employing the FRESKO code [15] and the DWUCK5 code [16] which are available in the NRV knowledge-base [17].

In order to describe measured experimental data one consider the  ${}^9\text{Be}$  target having the quadrupole deformation. Thus the  ${}^9\text{Be}$  spectrum consists the rotational band including the ground state,  $5/2^-$  state at 2.43 MeV and  $7/2^-$  state at 6.38 MeV. Coupling to these states were taken into account within the couple channel approach. The spin reorientations were also taken into account. The coupling interaction has the usual form:

$$V_\lambda(R) = -\beta_\lambda R_V \left| \frac{dV^V}{dR} \right| - i\beta_\lambda R_W \left| \frac{dW^D}{dR} \right|, \quad (8)$$

where  $\beta_\lambda$  is the deformation parameter of  $\lambda$  multipole describing the target-nucleus form. Here we as usual neglect the contribution of the Coulomb interaction.

The calculated cross sections for inelastic scattering are shown in Fig. 5. The solid curves correspond to the results obtained within the CC approach, while the dashed and dotted curves were obtained within the DWBA approach using different values of the deformation parameter  $\beta_2$ . The parameters of the CC potential are listed in Table 1.

All the results in Fig. 5 are in good agreement with experimental data. The quadrupole deformation

parameter  $\beta_2 = 0.64$  extracted within couple channel model is in consistence with the previous studies [5, 18].

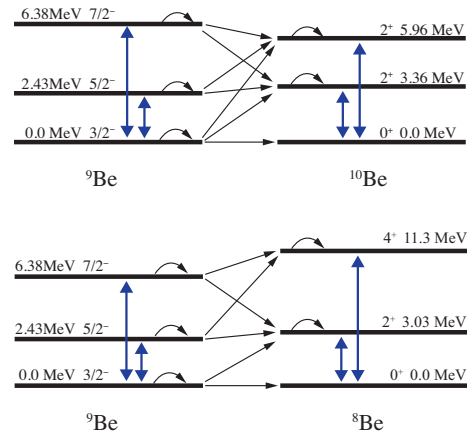
In the case of DWBA calculations one use the DF potential (see Table 1) for both the entrance and the exit channels. The DWBA angular distributions very well reproduce the structure of experimental data but distinctly underestimate them when the deformation parameter  $\beta_2 = 0.64$  is used (see the dotted curves in Fig. 5). In order to get the best fit the deformation parameter must be increased up to  $\beta_2 = 0.93$  which is quite close to the values reported in previous studies (see, for example, [19, 20]).

Thus one may confirm that channel coupling and the effects of spin re-orientation enhance the cross section that results in the reduction of the deformation parameter. However, the DWBA approach takes into account only first order contributions to the transition amplitude. In particular, it also describes only general features of the angular distributions and overestimates the deformation parameter in order to compensate the difference between the experimental data and the DWBA cross sections.

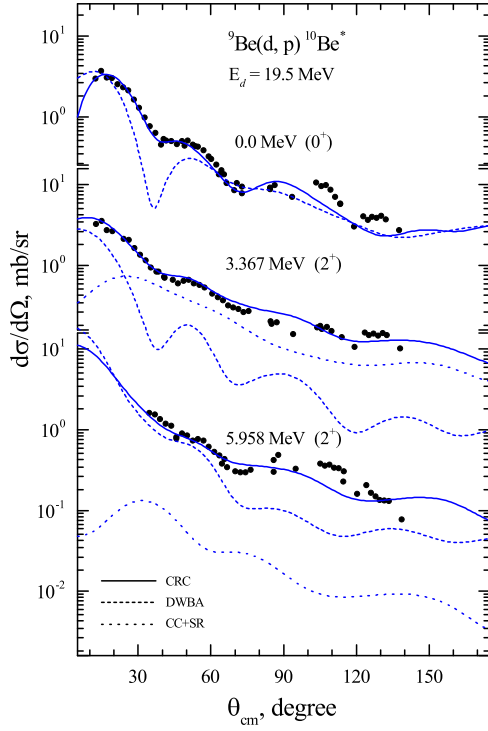
### 3.3. One nucleon transfer reactions

The one neutron pick-up  ${}^9\text{Be}(d,t){}^8\text{Be}$  and stripping  ${}^9\text{Be}(d,p){}^{10}\text{Be}$  reactions were analyzed here within the framework of the Coupled Reaction Channels (CRC).

The couple channel potentials given in Table 1 were used in the CRC calculations for the entrance channel as well as the global optical parametrizations from Ref. [21, 22] were used for the exit channels. The coupling schemes of target nuclei for the  ${}^9\text{Be}(d,p){}^{10}\text{Be}$  and  ${}^9\text{Be}(d,t){}^8\text{Be}$  reactions are illustrated in Fig. 6. The states of  ${}^{10}\text{Be}$ ,  $2_1^+$  and  $2_2^+$ , as well as the low-lying excited states of  ${}^8\text{Be}$ ,  $2^+$  and  $4^+$ , were implemented



**Figure 6.** The target coupling schemes in the  ${}^9\text{Be}(d,p){}^{10}\text{Be}$  (upper) and the  ${}^9\text{Be}(d,t){}^8\text{Be}$  (lower) nuclear reactions. The bold two headed arrows indicate  $E\lambda$  transitions. The spin re-orientation effects are indicated as back pointing arrows.



**Figure 7.** Differential cross sections for the  ${}^9\text{Be}(d,p){}^{10}\text{Be}^*$  reactions at 19.5 MeV for the neutron transferred to the different final states (indicated near the curves) of the  ${}^{10}\text{Be}$  product. The experimental data are shown in comparison with theoretical results obtained within the CRC method.

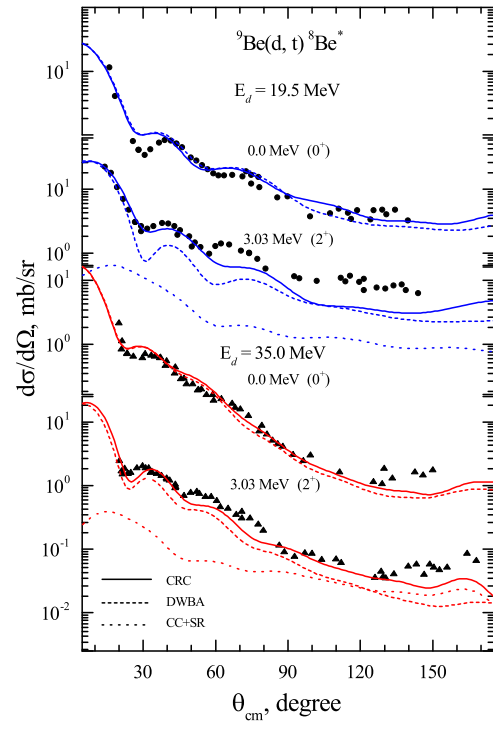
to the coupling scheme. Also, the schemes take into account the spin reorientation effects of states on the condition  $J \neq 0$ .

In order to construct the bound state wave functions of the transferred particle in entrance and exit channels one employed the common method, i.e. fitting the depth of the corresponding Woods-Saxon potential to the known binding energy. The reduced radius and diffuseness in this case are set to be equal  $r = 1.25$  fm and  $a = 0.65$  fm correspondingly. If the transfer takes place to the final unbound states, the depth of the potential for this state was adjusted to provide the binding energy equal to  $-0.1$  MeV in accordance with the recommendation given in Ref. [18].

The spectroscopic amplitude  $\mathcal{S}$  for an addition of particle from a Core  $J_{core}$  to a Composite  $J_{com}$  is related to the matrix element of the creation operator  $\hat{a}^\dagger$ :

$$\mathcal{S}_{NL_J} = \frac{\langle J_{com} || \hat{a}_{NL_J}^\dagger || J_{core} \rangle}{\sqrt{2J_{com} + 1}} \quad (9)$$

where  $NL_J$  is the set of particle quantum numbers. The spectroscopic amplitudes for one particle states were calculated by means of the *ANTOINE* code [23] using the effective Cohen-Kurath interaction for  $p$ -shell



**Figure 8.** Differential cross sections for the  ${}^9\text{Be}(d,t){}^8\text{Be}^*$  reactions at 19.5 and 35 MeV corresponding to the  ${}^8\text{Be}$  product in the different final states (indicated near the curves) in the exit channel. The experimental data are shown in comparison with theoretical results obtained within the CRC method.

nuclei [24]. The calculated spectroscopic amplitudes for the one nucleon transfer reactions are listed in Tab. 2.

Angular distributions of the  ${}^9\text{Be}(d,p){}^{10}\text{Be}$  nuclear reaction at  $E_d=19.5$  MeV are shown in comparison with the theoretical curves in the Fig. 7. The theoretical calculations of the direct neutron stripping carried out with the DWBA (dashed curve) underestimate the experimental data, but reproduce the behaviour well. However, one should take into account here the couplings between  $d+{}^9\text{Be}$  and  $p+{}^{10}\text{Be}$  channels, spin re-orientations and electromagnetic transitions, which are plotted as dotted curve and marked as "CC" in Fig. 7. Within the CRC method, i.e. taken together the latter and the DWBA calculations, we could obtain a good agreement of theoretical calculations with experimental data. It is interesting to note that we managed to describe the differential cross section of the  ${}^9\text{Be}(d,p){}^{10}\text{Be}^{gs}$  nuclear reaction in all scattering angles, including the range  $40^\circ$ - $60^\circ$ , where they were not covered in the Ref. [27, 19].

The Figure 8 illustrates the cross sections of the  ${}^9\text{Be}(d,t){}^8\text{Be}$  nuclear reaction at both 19.5 MeV and 35 MeV energies. As in the case of the (d,p) reactions, the (d,t) reactions also show the strong channel coupling effects, especially in the

**Table 2.** Spectroscopic amplitudes used in CRC calculations for the Composite = Core + Cluster system. The one nucleon spectroscopic amplitudes calculated by means of the *ANTOINE* code [23]. The alpha spectroscopic amplitudes were taken from [25, 26].

Composite	2J <sub>com</sub>	Core	2J <sub>core</sub>	Cluster	2J	SA	Composite	2J <sub>com</sub>	Core	2J <sub>core</sub>	Cluster	2J	SA
<sup>9</sup> Be	3	<sup>8</sup> Be	0	n	3	-0.761	<sup>9</sup> Be	3	<sup>8</sup> Li	2 <sub>1</sub>	p	1	-0.444
<sup>9</sup> Be	3	<sup>8</sup> Be	4	n	3	0.816	<sup>9</sup> Be	3	<sup>8</sup> Li	6	p	3	-0.592
<sup>9</sup> Be	3	<sup>8</sup> Be	4	n	1	-0.242	<sup>9</sup> Be	3	<sup>8</sup> Li	2 <sub>2</sub>	p	3	-0.236
<sup>9</sup> Be	5	<sup>8</sup> Be	4	n	3	0.986	<sup>9</sup> Be	3	<sup>8</sup> Li	2 <sub>2</sub>	p	1	0.036
<sup>9</sup> Be	5	<sup>8</sup> Be	4	n	1	-0.417	<sup>9</sup> Be	5	<sup>8</sup> Li	4	p	3	0.593
<sup>9</sup> Be	5	<sup>8</sup> Be	8	n	3	-0.374	<sup>9</sup> Be	5	<sup>8</sup> Li	4	p	1	0.515
<sup>9</sup> Be	7	<sup>8</sup> Be	4	n	3	-0.457	<sup>9</sup> Be	5	<sup>8</sup> Li	2 <sub>1</sub>	p	3	-0.672
<sup>9</sup> Be	7	<sup>8</sup> Be	8	n	3	0.919	<sup>9</sup> Be	5	<sup>8</sup> Li	6	p	3	-0.571
<sup>9</sup> Be	7	<sup>8</sup> Be	8	n	1	-0.429	<sup>9</sup> Be	5	<sup>8</sup> Li	6	p	1	-0.171
<sup>8</sup> Be	0	<sup>7</sup> Li	3	p	3	-1.204	<sup>9</sup> Be	5	<sup>8</sup> Li	2 <sub>2</sub>	p	3	0.200
<sup>8</sup> Be	0	<sup>7</sup> Li	1	p	1	0.736	<sup>9</sup> Be	7	<sup>8</sup> Li	4	p	3	-0.323
<sup>8</sup> Be	4	<sup>7</sup> Li	3	p	3	-0.748	<sup>9</sup> Be	7	<sup>8</sup> Li	6	p	3	-0.899
<sup>8</sup> Be	4	<sup>7</sup> Li	3	p	1	-0.612	<sup>9</sup> Be	7	<sup>8</sup> Li	6	p	1	-0.564
<sup>8</sup> Be	4	<sup>7</sup> Li	1	p	3	0.667	<sup>7</sup> Li	3	<sup>6</sup> Li	2	n	3	0.657
<sup>8</sup> Be	4	<sup>7</sup> Li	7	p	3	0.624	<sup>7</sup> Li	3	<sup>6</sup> Li	2	n	1	-0.538
<sup>8</sup> Be	4	<sup>7</sup> Li	5 <sub>2</sub>	p	3	0.079	<sup>7</sup> Li	3	<sup>6</sup> Li	6	n	3	0.744
<sup>8</sup> Be	4	<sup>7</sup> Li	5 <sub>2</sub>	p	3	-0.146	<sup>7</sup> Li	3	<sup>6</sup> Li	4	n	3	-0.032
<sup>8</sup> Be	8	<sup>7</sup> Li	7	p	3	0.864	<sup>7</sup> Li	3	<sup>6</sup> Li	4	n	1	0.399
<sup>8</sup> Be	8	<sup>7</sup> Li	7	p	1	0.687	<sup>7</sup> Li	1	<sup>6</sup> Li	2	n	3	-0.925
<sup>8</sup> Be	8	<sup>7</sup> Li	5 <sub>2</sub>	p	3	0.374	<sup>7</sup> Li	1	<sup>6</sup> Li	2	n	1	0.197
<sup>8</sup> Li	4	<sup>7</sup> Li	3	n	3	-0.988	<sup>7</sup> Li	1	<sup>6</sup> Li	4	n	3	-0.555
<sup>8</sup> Li	4	<sup>7</sup> Li	3	n	1	0.237	<sup>7</sup> Li	7	<sup>6</sup> Li	6	n	3	-0.936
<sup>8</sup> Li	4	<sup>7</sup> Li	1	n	3	0.430	<sup>7</sup> Li	7	<sup>6</sup> Li	6	n	1	0.645
<sup>8</sup> Li	4	<sup>7</sup> Li	7	n	3	-0.496	<sup>7</sup> Li	7	<sup>6</sup> Li	4	n	3	-0.456
<sup>8</sup> Li	4	<sup>7</sup> Li	5	n	3	-0.665	<sup>7</sup> Li	5 <sub>2</sub>	<sup>6</sup> Li	2	n	3	-0.650
<sup>8</sup> Li	4	<sup>7</sup> Li	5 <sub>2</sub>	n	1	-0.275	<sup>7</sup> Li	5 <sub>2</sub>	<sup>6</sup> Li	6	n	3	0.732
<sup>8</sup> Li	2 <sub>1</sub>	<sup>7</sup> Li	3	n	3	0.567	<sup>7</sup> Li	5 <sub>2</sub>	<sup>6</sup> Li	6	n	1	0.549
<sup>8</sup> Li	2 <sub>1</sub>	<sup>7</sup> Li	3	n	1	0.351	<sup>7</sup> Li	5 <sub>2</sub>	<sup>6</sup> Li	4	n	3	0.200
<sup>8</sup> Li	2 <sub>1</sub>	<sup>7</sup> Li	1	n	3	0.905	<sup>7</sup> Li	5 <sub>2</sub>	<sup>6</sup> Li	4	n	1	-0.114
<sup>8</sup> Li	2 <sub>1</sub>	<sup>7</sup> Li	1	n	1	0.331	<sup>6</sup> Li	2	d	2	α	0	0.907
<sup>8</sup> Li	2 <sub>1</sub>	<sup>7</sup> Li	5 <sub>2</sub>	n	3	0.767	<sup>6</sup> Li	2	d	2	α	4	0.077
<sup>8</sup> Li	6	<sup>7</sup> Li	3	n	3	0.581	<sup>6</sup> Li	6	d	2	α	4	0.943
<sup>8</sup> Li	6	<sup>7</sup> Li	5 <sub>2</sub>	n	3	-0.660	<sup>6</sup> Li	6	d	2	α	8	0.028
<sup>8</sup> Li	6	<sup>7</sup> Li	5 <sub>2</sub>	n	1	-0.541	<sup>6</sup> Li	4	d	2	α	4	0.929
<sup>8</sup> Li	6	<sup>7</sup> Li	7	n	3	0.973	<sup>9</sup> Be	3	<sup>5</sup> He	3	α	0	-0.925
<sup>8</sup> Li	6	<sup>7</sup> Li	7	n	1	-0.404	<sup>9</sup> Be	3	<sup>5</sup> He	3	α	4	0.784
<sup>8</sup> Li	2 <sub>2</sub>	<sup>7</sup> Li	3	n	3	-0.617	<sup>9</sup> Be	5	<sup>5</sup> He	3	α	4	0.974
<sup>8</sup> Li	2 <sub>2</sub>	<sup>7</sup> Li	3	n	1	-0.841	<sup>9</sup> Be	5	<sup>5</sup> He	3	α	8	-0.260
<sup>8</sup> Li	2 <sub>2</sub>	<sup>7</sup> Li	1	n	3	0.178	<sup>9</sup> Be	7	<sup>5</sup> He	3	α	4	0.882
<sup>8</sup> Li	2 <sub>2</sub>	<sup>7</sup> Li	1	n	1	0.331	<sup>9</sup> Be	7	<sup>5</sup> He	3	α	8	-0.737
<sup>8</sup> Li	2 <sub>2</sub>	<sup>7</sup> Li	5	n	3	0.231	<sup>7</sup> Li	3	t	1	α	1	0.970
<sup>9</sup> Be	3	<sup>8</sup> Li	4	p	3	-0.947	<sup>7</sup> Li	1	t	1	α	1	0.961
<sup>9</sup> Be	3	<sup>8</sup> Li	4	p	1	-0.319	<sup>7</sup> Li	7	t	1	α	3	0.952
<sup>9</sup> Be	3	<sup>8</sup> Li	2 <sub>1</sub>	p	3	0.454	<sup>7</sup> Li	5 <sub>2</sub>	t	1	α	3	0.223

<sup>9</sup>Be(d,t)<sup>8</sup>Be<sup>2+</sup> reaction. Theoretical calculations made within the CRC method shows good agreement with experimental data.

The results obtained within the CRC approach for the <sup>9</sup>Be(d,p)<sup>10</sup>Be and <sup>9</sup>Be(d,t)<sup>8</sup>Be reactions shows strong coupling effects in both entrance and exit channels. The effects of such kind were also emphasized in Ref. [18, 28].

### 3.4. Cluster transfer reaction

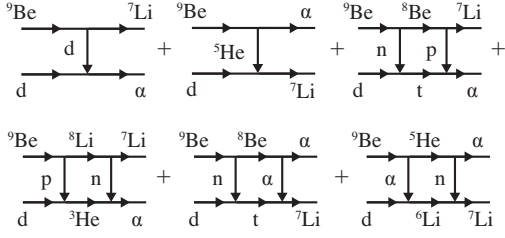
Differential cross sections for the nuclear reaction <sup>9</sup>Be(d,α)<sup>7</sup>Li are of particular interest. The reason

is in specific behaviour of the cross section at large scattering angles, that shows possibility for the <sup>5</sup>He cluster transfer. In addition, the cross section calculated within the DWBA approach underestimates data even at forward scattering angles. Therefore, in order to cure the distinction between theory and experiment, the following transfer mechanisms are suggested (see Fig. 10):

- direct transfer of heavy clusters *d* and <sup>5</sup>He;
- sequential two-step transfer of n-p, p-n, n-α and α-n;

The resulting differential cross section for the





**Figure 10.** The scheme illustrates the reaction mechanisms taken into account in CRC calculations of the cross sections for  ${}^9\text{Be}(d, \alpha){}^7\text{Li}$  reaction.

${}^9\text{Be}(d, \alpha){}^7\text{Li}$  reaction has form of a coherent sum of two amplitudes

$$\frac{d\sigma}{d\Omega}(\theta) = |f_I(\theta) + f_{II}(\theta)|^2, \quad (10)$$

where the amplitude

$$f_I(\theta) = f_{5\text{He}}(\pi - \theta) + f_{n-\alpha}(\pi - \theta) + f_{\alpha-n}(\pi - \theta) \quad (11)$$

describes the transfer of the heavy  ${}^5\text{He}$ -cluster and sequential two-step transfer of  $n-\alpha$  and  $\alpha-n$ , and the amplitude

$$f_{II}(\theta) = f_d(\theta) + f_{n-p}(\theta) + f_{p-n}(\theta) \quad (12)$$

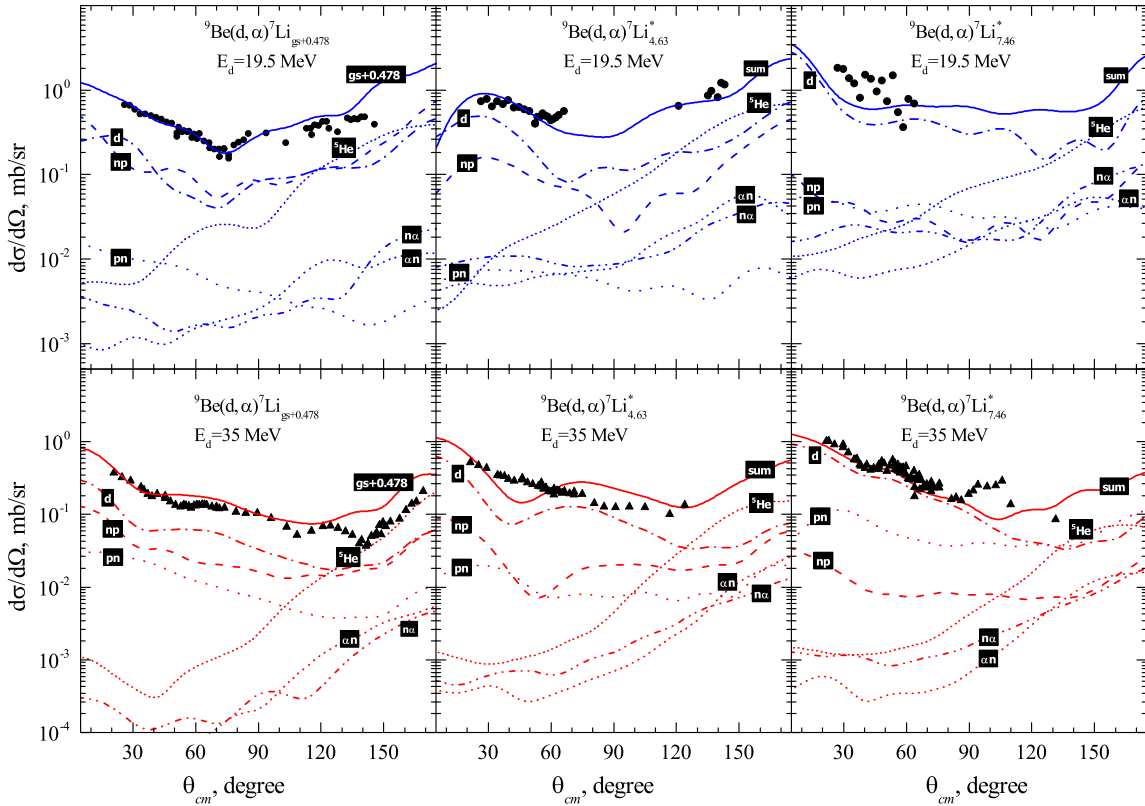
corresponds to the deuteron pick-up and sequential two-step transfer of  $n-p$  and  $p-n$ .

The CC potential (see Tab. 1) for the entrance channel and global optical potential parameterizations from Ref. [22, 29, 30] for intermediate and exit channels were used in the analysis. The prior form for the first coupling, and the post form for the second coupling were chosen for two-step transfer reactions in order to avoid the non-orthogonal terms in the calculations of transition amplitudes.

The spectroscopic amplitudes of the  $d$  and  ${}^5\text{He}$  clusters were taken from Ref. [31], while the alpha-cluster spectroscopic amplitudes given in Tab. 2 were provided by Dr. A. Volya within the method reported in Ref. [26].

The calculated cross sections are shown in Fig. 9 with the  $\alpha$ -particle angular distributions formed in the  ${}^9\text{Be}(d, \alpha){}^7\text{Li}^*$  reaction at energies 19.5 and 35 MeV and corresponding to the low-lying excitation of the  ${}^7\text{Li}$  nucleus in exit channels. The transfer of the deuteron (dash-dotted curve) provides the dominant contribution in all the channels. Despite the fact that the spectroscopic amplitude of the deuteron  $S_{1D_3} = 0.558$  in the  ${}^9\text{Be}$  nucleus is not of great importance, a noticeable cross section is due to the large value of the deuteron spectroscopic amplitude  $S_{1S_1} = 1.732$  of  ${}^4\text{He}$ .

The angular distribution of deuteron transfer has



**Figure 9.** Differential cross sections for the  ${}^9\text{Be}(d, \alpha){}^7\text{Li}$  reactions measured at 19.5 MeV and 35 MeV energy with the  ${}^7\text{Li}$  observed in the ground or low-lying excited states in the exit channels.



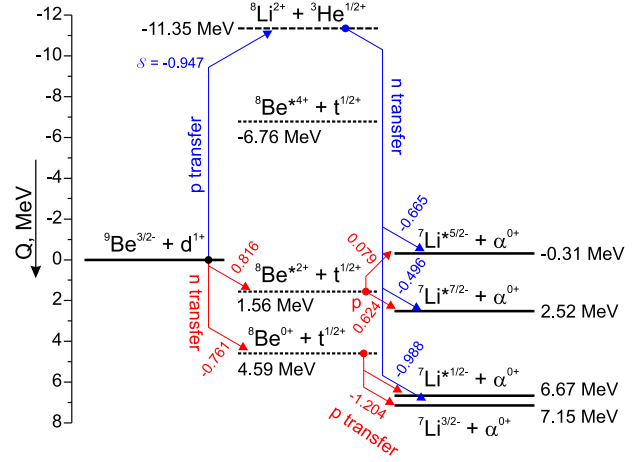
a significant cross section also at the back scattering angles, which is mainly caused by the contribution of the  $D$  wave. This symmetrical behaviour of the cross section of  $D$  waves is very similar to the cross section of evaporation residue. Tanaka et al. [32] analyzed the role of the compound process in  ${}^9\text{Be}(d,\alpha){}^7\text{Li}$  reaction and claimed the domination of the compound nucleus channels at the 12.17 MeV and 14.43 MeV energies. However, in Ref. [19] the negligible contribution of mechanism through the compound nucleus was shown at 7 MeV using the DWBA analysis. In this regard, our theoretical results based on the CRC method shows that there is no need to take into account the mechanism through the compound nucleus at energies of 19.5 and 35.0 MeV.

In all channels starting from scattering angle  $\theta_{c.m.} = 120^\circ$  the transfer of the  ${}^5\text{He}$  cluster, labeled as  ${}^5\text{He}$  in Fig. 9, has a predominant contribution. It should be noted that the similar result was mentioned early in Ref. [19]. One-step transfer of the  ${}^5\text{He}$  cluster was also indicated as a dominant process by Jarczyk *et al* [33] studying the  ${}^{12}\text{C}({}^{11}\text{B}, {}^6\text{Li}){}^{17}\text{O}$  and  ${}^{12}\text{C}(d, {}^7\text{Li}){}^7\text{Be}$  reactions.

Using the CRC method, we are able to estimate the contribution of the sequential transfer of the  ${}^5\text{He}$ , which was not studied before. Corresponding cross sections are shown in Fig. 9 as curves labeled  $n\alpha$  and  $\alpha n$ . It turned out that the  $n\alpha$  and the  $\alpha n$  transfer processes provide indeed the contribution more than one order of magnitude lower in comparison with the one-step  ${}^5\text{He}$  transfer. Nevertheless, it should be noted that the contribution of the  $n\alpha$  and the  $\alpha n$  transfer channels increases with the  ${}^7\text{Li}$  excitation increases, where they should not be ignored.

The two-step  $n$ - $p$  transfer is another mechanism providing noticeable contribution to the cross section. It is due to the prominent cluster structure of the  ${}^9\text{Be}$  nucleus having the weakly bound neutron. This structural feature explains also the weakness of the  $p$ - $n$  sequential transfer contribution to the cross section corresponding the  ${}^7\text{Li}(g.s.)$  in the exit channel. However curves in Fig. 11 with increasing the  ${}^7\text{Li}$  excitation energy these two mechanisms change their places and the  $p$ - $n$  transfer begins to play a leading role, providing, in particular, almost 10 times large contribution in the case of reaction at the  $E_{lab} = 35$  MeV with  ${}^7\text{Li}^*(7.46 \text{ MeV})$  in exit channel.

In Fig. 11 the possible scenarios of the  $n$ - $p$  and  $p$ - $n$  sequential transferring for the reaction under consideration are shown in respect to the  $Q$ -values. One may see that all the steps of the  $n$ - $p$  sequential transfer have the positive  $Q$ -values, while the  $p$ - $n$  transfer goes through the intermediate channel  ${}^8\text{Li} + {}^3\text{He}$  having considerable negative  $Q$ -value. Together with large values of the spectroscopic amplitudes

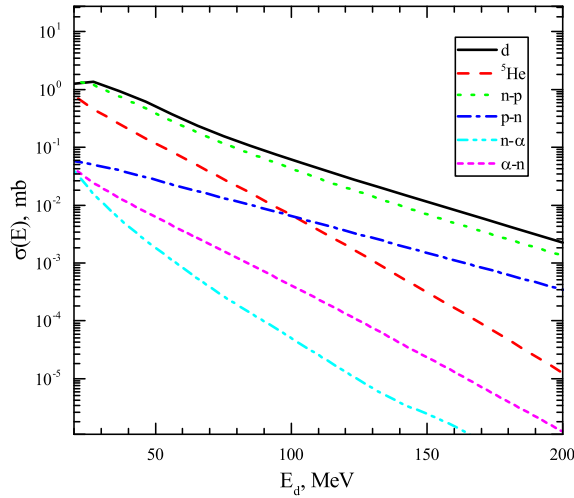


**Figure 11.** The scheme illustrates the energy balance of the different intermediate stages for the two-step mechanisms of  ${}^9\text{Be}(d,\alpha){}^7\text{Li}$  transfer reaction. The  $Q$ -values for the different intermediate channels are shown near the corresponding lines. The numbers near the arrows correspond to the spectroscopic amplitudes of the heaviest reaction participants. For example, spectroscopic amplitude for the  ${}^9\text{Be} = {}^8\text{Li} + p$  configuration is equal  $S = -0.947$ .

(shown near the arrows in Fig. 11) it explains the leading role of the  $(d,t;t,\alpha)$  mechanism in populating the ground state of the  ${}^7\text{Li}$  in the exit channel.

The situation becomes quite different in the case of the  ${}^7\text{Li}^*(5/2^-)$  in the exit channel. First of all the population of this state through the  $n$ - $p$  transferring includes the  ${}^9\text{Be} = {}^8\text{Be}^*(2^+) + n$  intermediate configuration where  ${}^8\text{Be}$  cluster has to be in  $2^+$  excited state. Note that the  ${}^8\text{Be}(0^+)$  ground state is inappropriate because of angular momentum coupling mismatch in entrance and exit configurations. Second circumstance is an extremely small spectroscopic amplitude of the  ${}^8\text{Be}^*(2^+) = {}^7\text{Li}^*(5/2^-) + p$  configuration which is equal  $S = 0.079$ . These two factors lead to the suppression of the contribution of  $(d,t;t,\alpha)$  mechanism in population of the  ${}^7\text{Li}^*(5/2^-)$  state in the exit channel. Therefore the  $p$ - $n$  sequential transfer prevails over the  $n$ - $p$  one. With rising the collision energy the suppression of the  $(d,t;t,\alpha)$  mechanism is even enhanced due to decrease the reaction time while the presence of the  ${}^8\text{Be}^*(2^+)$  intermediate state indicates that the process actually becomes multi-step one that requires more time.

Figure 12 shows the contributions of all the mechanism mentioned above into the total cross section of the  ${}^9\text{Be}(d,\alpha){}^7\text{Li}_{g.s.}$  reaction (see Fig. 10) as a function of the deuteron energy. One may conclude that only four mechanisms form the cross section of this reaction mainly. The transfer of the deuteron-cluster is predominant channel at the all collision energies. The sequential  $n$ - $p$  and  $p$ - $n$  transfers play significant role at the high energies. The  ${}^5\text{He}$ -cluster



**Figure 12.** Contributions of the different mechanisms into the cross section of the  ${}^9\text{Be}(d,\alpha){}^7\text{Li}_{g.s.}$  reaction. See Fig. 10 for explanation of the curve notations.

transfer gives almost 20% of the cross section at low energies and outgoes the sequential p-n transfer in this energy domain. Thus it allows us to claim that the configurations  $n+{}^8\text{Be}$  and  $\alpha+{}^5\text{He}$  provide noticeable contributions into the ground state wave function of the  ${}^9\text{Be}$  nucleus. These conclusions agree well with the previous experimental studies [8, 9].

#### 4. Conclusion

In the present work, the deuteron induced reactions with  ${}^9\text{Be}$  target have been studied at the collision energies 19.5 and 35 MeV. The following conclusions can be made during the analysis:

- The double-folding potential, which is characteristic of the interaction of deuteron with  ${}^9\text{Be}$ , differs from phenomenological optical potentials;
- The deformation parameter has been obtained for the excited state 2.43 MeV of  ${}^9\text{Be}$ ;
- The strong coupling effects in the nuclear reactions with one nucleon transfer have been revealed;
- It was found that in the  ${}^9\text{Be}(d,\alpha){}^7\text{Li}$  nuclear reaction the  ${}^5\text{He}$  heavy cluster is transferred mainly simultaneously, and the contribution of its sequential transfer is an order of magnitude lower;
- The importance of taking into account the mechanism of sequential transfer of the n-p system has been revealed.

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