

URP 6931. Introduction to Urban Analytics

# Lecture 12: Analytical fairness

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# Disclaimers

1. Today's lecture is about exploratory views, so I am open to discussions and your feedbacks are important.
2. I did not grow up in the US, so I would like to learn socially acceptable methods to discuss fairness.

# Outline

1

Fairness definitions  
in analytics

2

Analytical fairness  
in urban  
applications

3

Computational  
fairness (ML) &  
general comments

4

Lab session  
(two exercises)

5

Guest lecture  
(3:45-4:30)

# Part 1. Fairness definitions in analytics

Equity, equality, and Rawlsian fairness

Equality

Equality is the state of being equal, especially in status, rights and opportunities. Equality means each individual or group of people is given the **same resources and opportunities, regardless of their circumstances.**

Cite: <https://unitedwaynca.org/blog/what-is-equality/>

Equity

Whereas equality means providing the same to all, equity means recognizing that we do not all start from the same place and must acknowledge and **make adjustments to imbalances.**

Cite: <https://www.naceweb.org/about-us/equity-definition/>

Rawlsian fairness

Each person has the same and indefeasible [permanent] claim to a fully adequate scheme of equal **basic liberties [rights]**, which scheme is compatible with the same scheme of liberties for all.

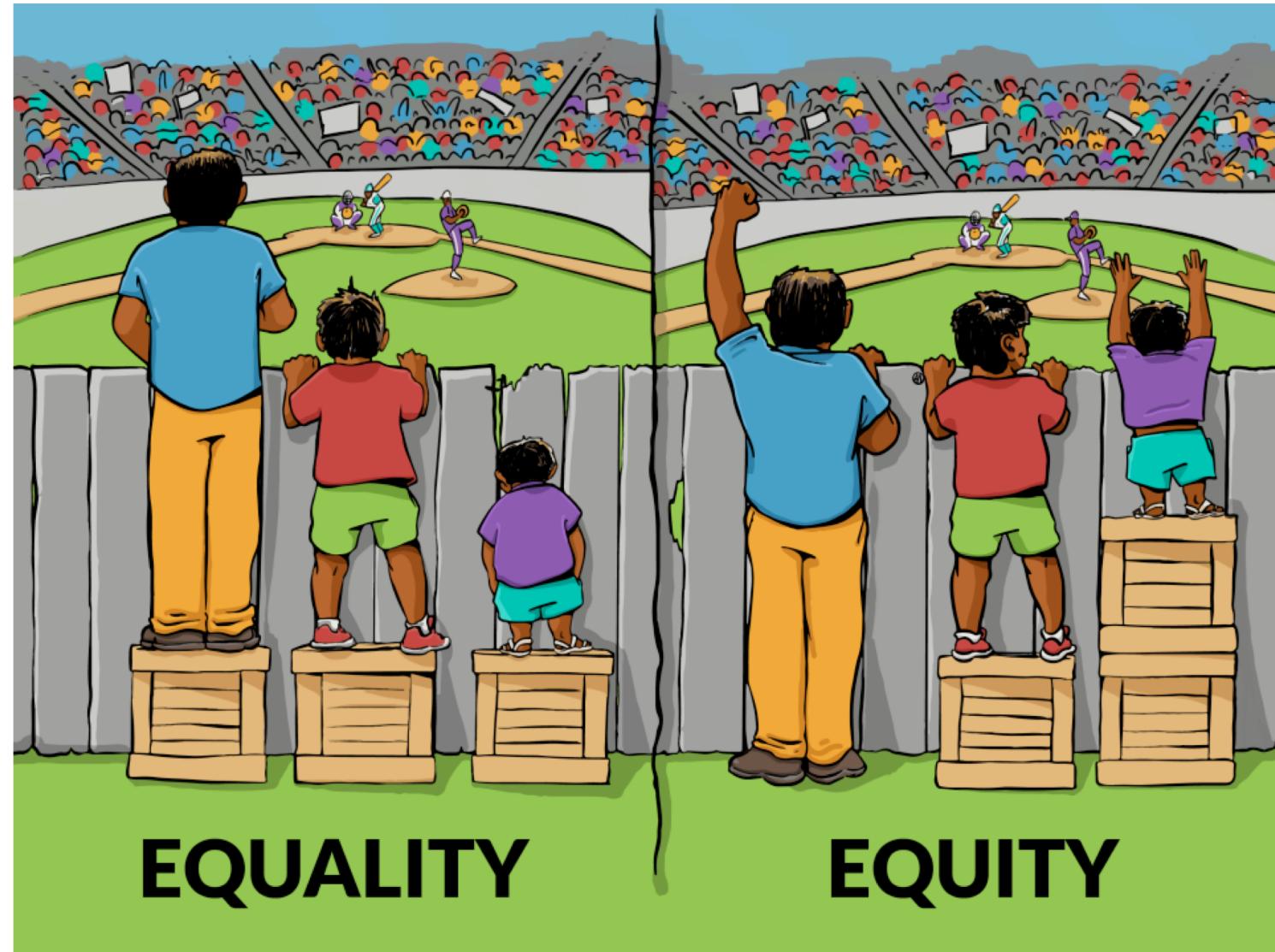
Cite: <https://www.crf-usa.org/bill-of-rights-in-action/bria-23-3-c-justice-as-fairness-john-rawls-and-his-theory-of-justice>

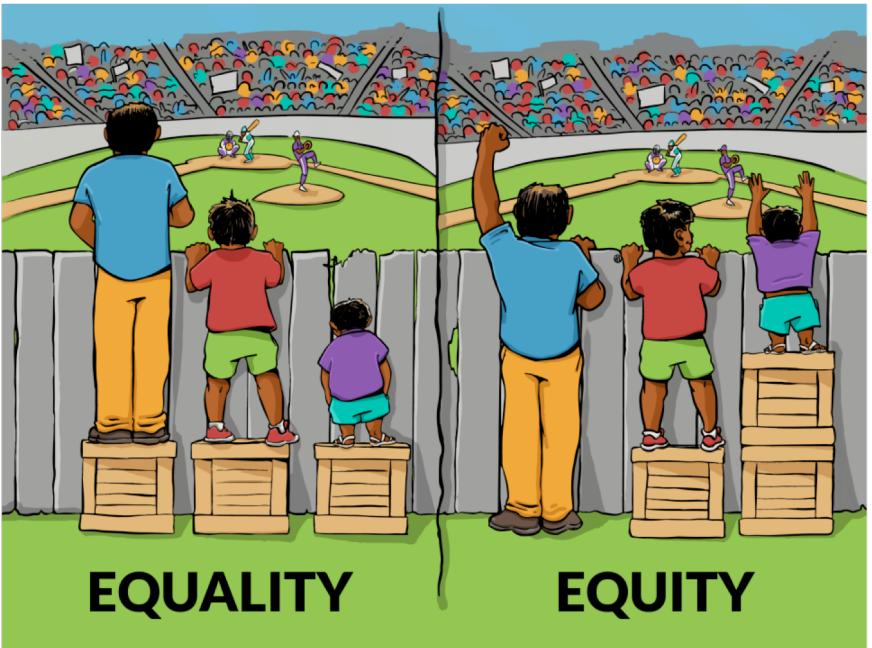
Philosophical discussions could be confusing, but they can be reduced to simple math definitions.

**Note**

- Shenhao's learning trajectory.

# Equality and equity

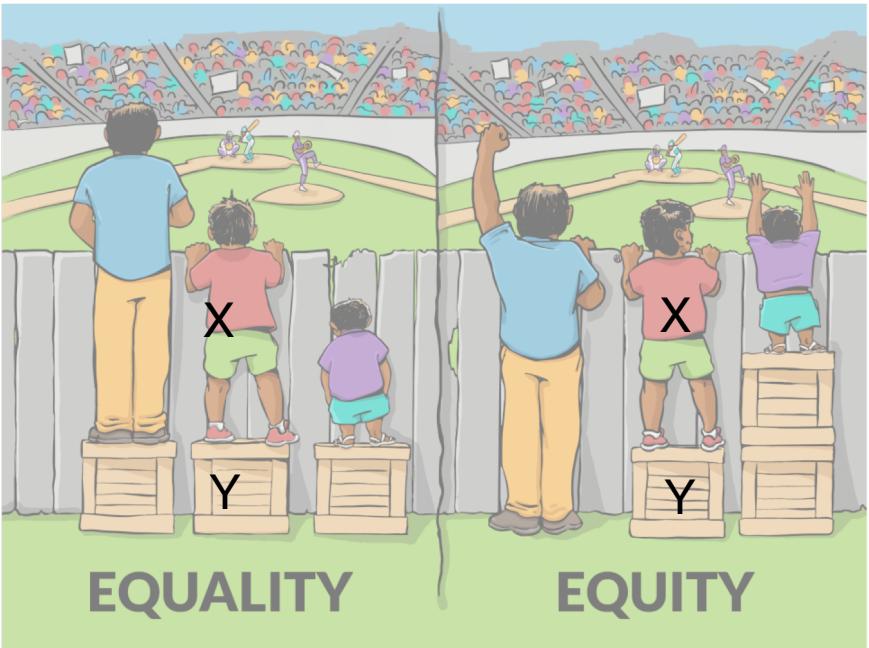




# Equality and Equity

## Question

Could you see **regression lines** from the two pictures?



# Equality and Equity

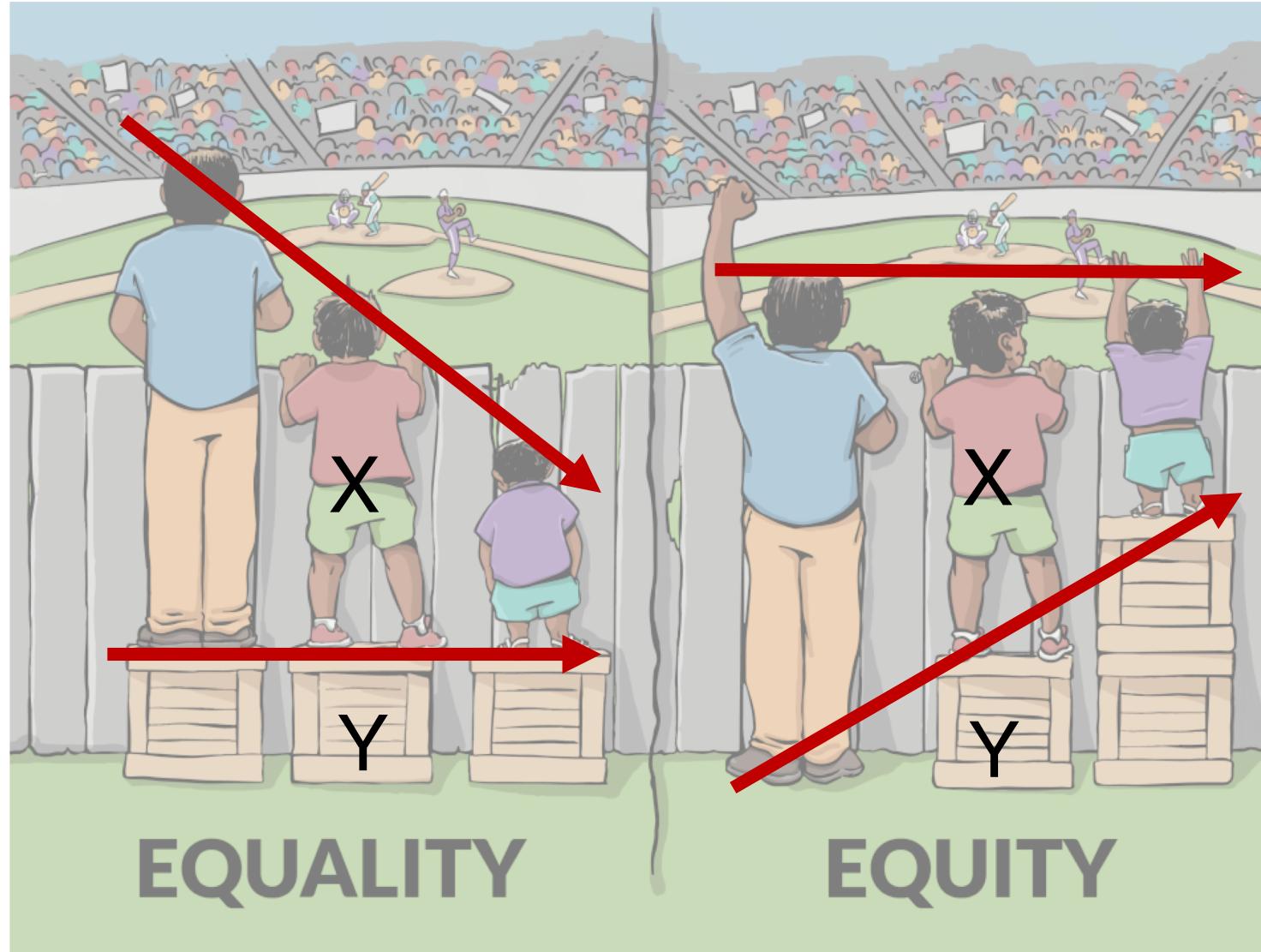
## Question

Could you see regression lines from the two pictures?

### X&Y

- Y: resources.
- X: socially sensitive group, including advantaged and disadvantaged subgroups. (measured by discrete or continuous variables)

# Equality and equity



Y: resources

X: socially sensitive groups

**Equality:** Y does not vary with X.

**Equity:** Y increases as X increases.

**Question:** How are equality and equity corresponding to  $\hat{\beta}_1$ ?

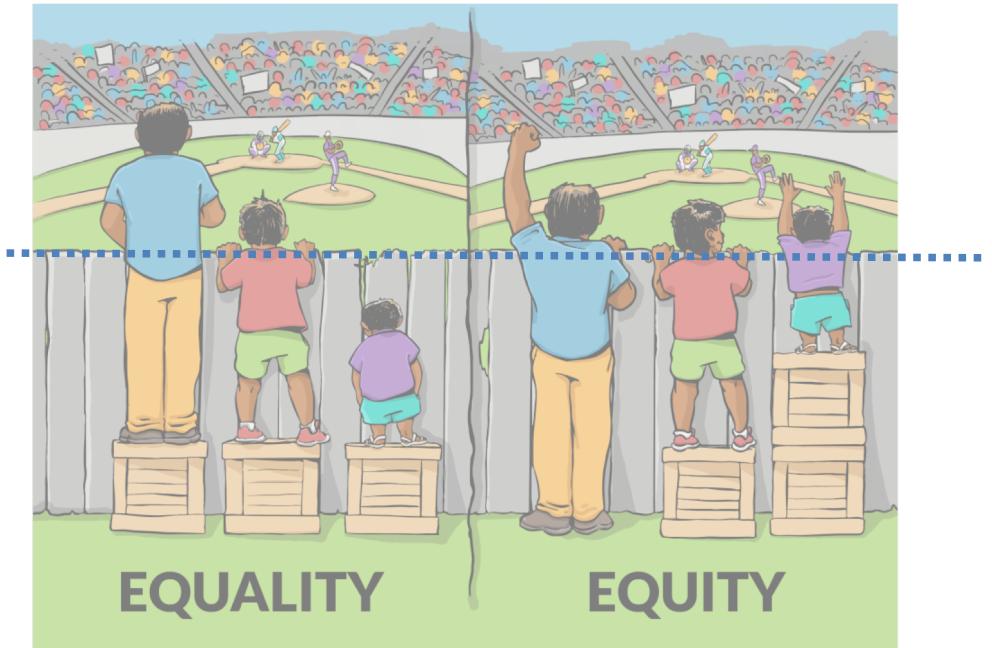
Equality:  $\hat{\beta}_1 = 0$

Equity:  $\hat{\beta}_1 <> 0$

**Example.** Y: food access. X: age.

Equality:  $\hat{\beta}_1 = 0$

Equity:  $\hat{\beta}_1 > 0$



## Where is the basic right?

**Rawls: even the most disadvantaged group has a **basic right**.**

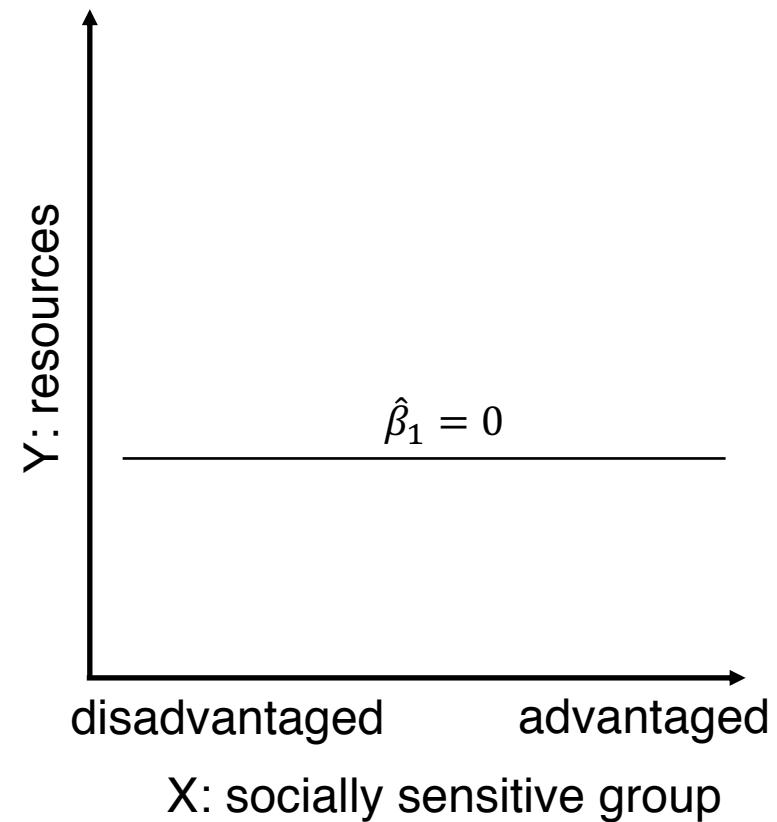
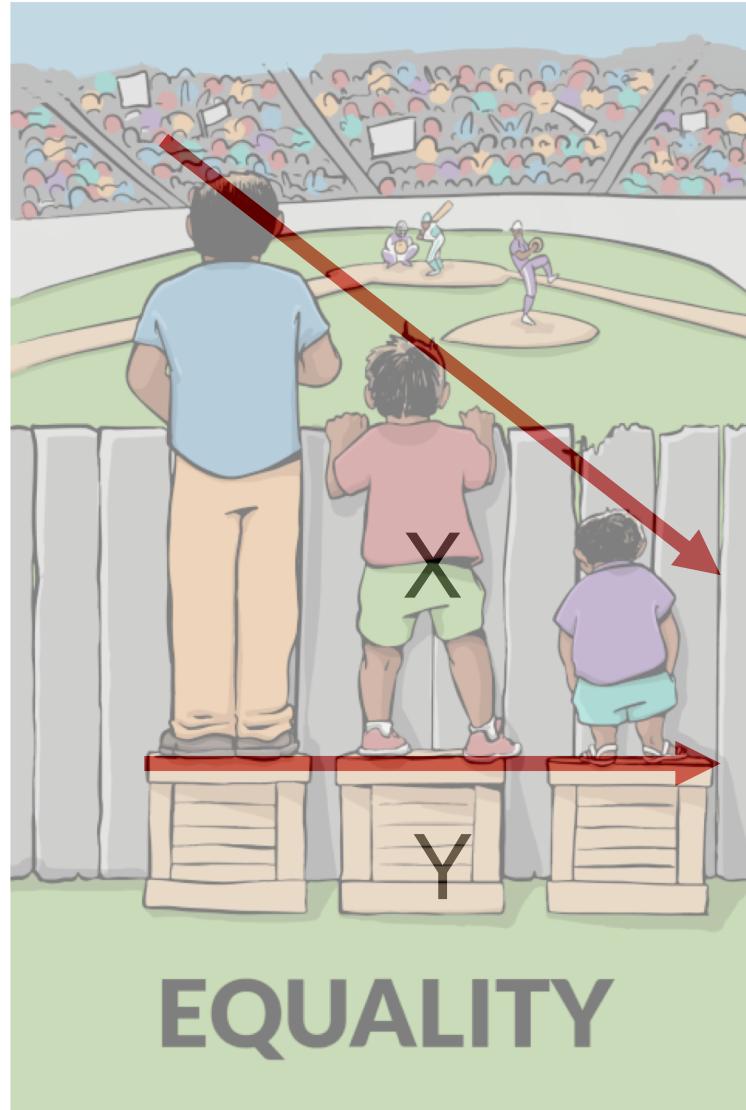
Y: resources

X: socially sensitive groups (larger X indicates more advantaged group)

Interpretation of  $\hat{\beta}_0$  actually aligns with the basic right intuition.

**Basic right:**  $\hat{\beta}_0 > \text{threshold}$

# Analytical fairness in a univariate regression: equality rule



## Define fairness

- Equality:  $Y$  does not vary with  $X$ . ( $\hat{\beta}_1 = 0$ )

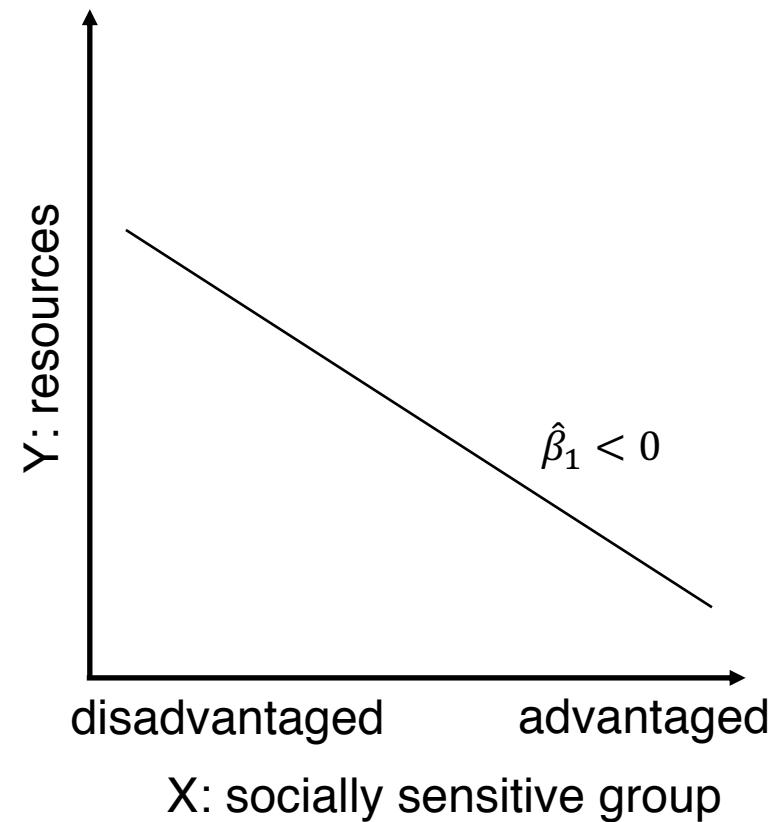
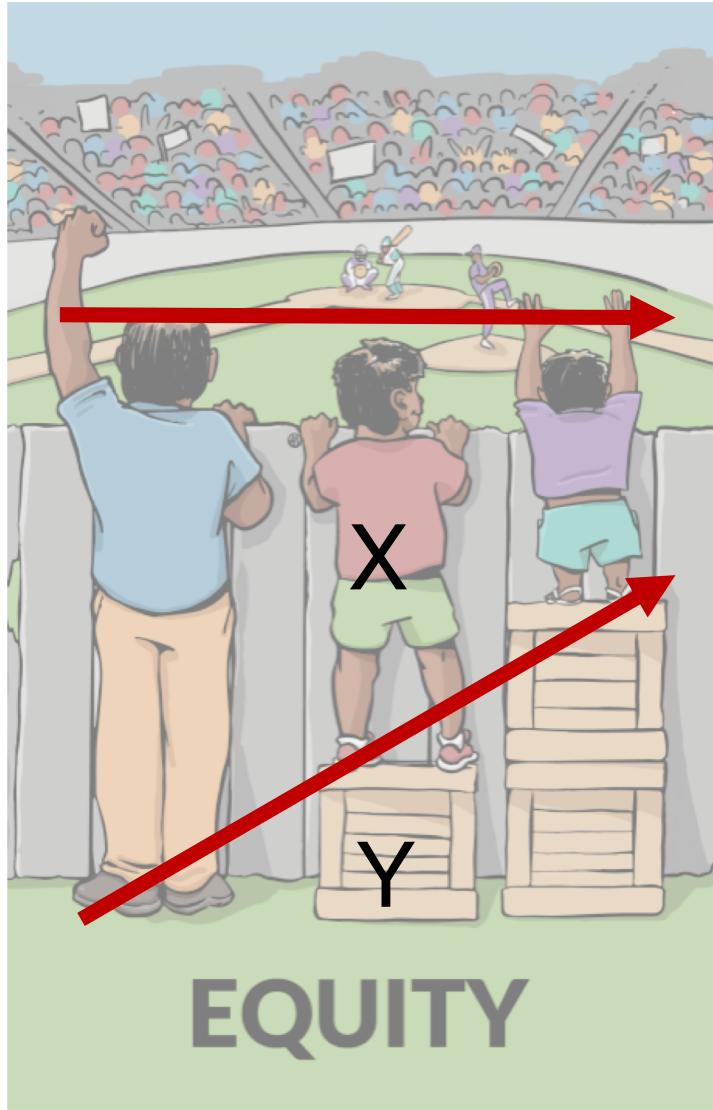
## Identify the context & run the regression

- $Y$ : resources
- $X$ : socially sensitive groups
- Recovering  $\hat{\beta}_1$

## Make normative evaluation

- Fair vs. Unfair

# Analytical fairness in a univariate regression: **equity** rule



## Define fairness

- Equity:  $Y$  varies with  $X$ . ( $\hat{\beta}_1 < 0$ )

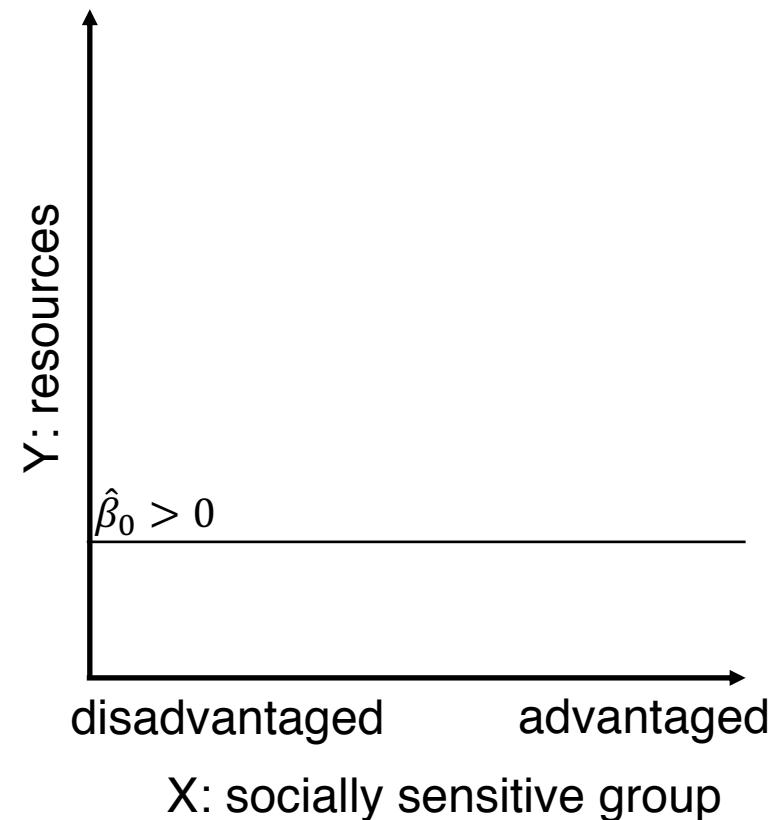
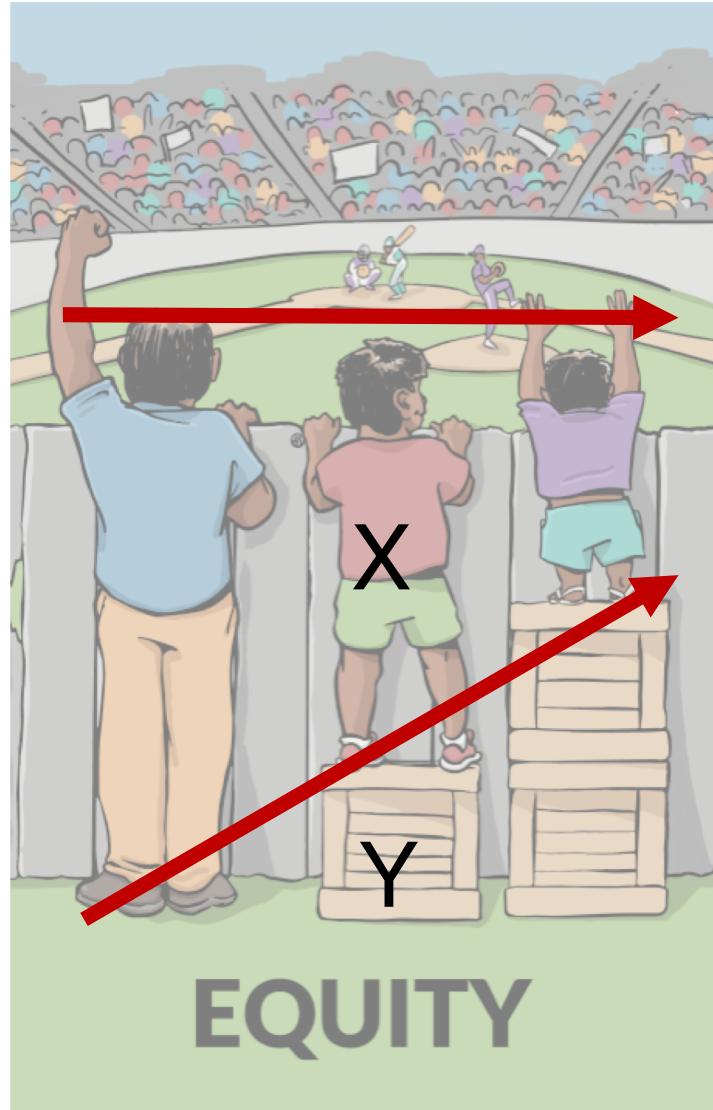
## Identify the context & run the regression

- $Y$ : resources
- $X$ : socially sensitive groups
- Recovering  $\hat{\beta}_1$

## Make normative evaluation

- Fair vs. Unfair

# Analytical fairness in a univariate regression: Rawlsian rule



## Define fairness

- Rawlsian: Weakest group has positive resource. ( $\hat{\beta}_0 > 0$ )

## Identify the context & run the regression

- Y: resources
- X: socially sensitive groups
- Recovering  $\hat{\beta}_0$

## Make normative evaluation

- Fair vs. Unfair

Equality

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$$\hat{\beta}_1 = 0$$

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# Two Questions

- Q1. How to deal with the **conflicting** fairness rules?
- Q2. How about the **multivariate** regressions?

## Part 2. Analytical fairness in urban applications

# Wide urban applications with analytical fairness

## Examples about X and Y

1. Socially sensitive group: disadvantaged vs. advantaged social subgroups.
  - Examples: income (poor vs. rich), age (senior vs. young), race (majority vs. minority), gender (female vs. male), household (large vs. small sizes), etc.
2. Resources.
  - Examples: food, transportation, housing, economic growth, new technology, etc.

**Any combination between 1&2 can leads to a valid urban application about fairness.**

## Example 1

1. Sensitive group: **income**; disadvantaged vs. advantaged social subgroups: low vs. high-income groups
2. Resources: **food accessibility**.
3. Process: (1) define fairness, (2) run regression, and (3) make fairness evaluation

## Example 2

1. Sensitive group: **age**; disadvantaged vs. advantaged social subgroups: senior vs. other groups
2. Resources: **housing**
3. Process: (1) define fairness, (2) run regression, and (3) make fairness evaluation.

# Process of evaluating fairness

This standard structure exists in **ANY** fairness evaluation.

This step is the **new** contents (lec12)

## 1. Major premise

Fairness is defined as the equity rule (a.k.a.  $\hat{\beta}_1 <> 0$ )

This step is the **old** contents (lec03-05)

## 2. Minor premise

Choose Y = food access and X = age.

Run the regression and recover the  $\hat{\beta}$  values.

## 3. Conclusion

Compare the fairness definition from step 1 and the signal from step 2. Then conclude the food access in Florida is fair/unfair to the seniors.

# Process of criticizing fairness evaluation

Q: How do you define fairness?

## 1. Major premise

Fairness is defined as the equity, equity, Rawlsian rule, or anything else?

Q: How do you analyze your data?

## 2. Minor premise

- How to choose the appropriate X & Y.
- A1: omitting variable bias.
- A2: function misspecification problem.
- Others: sampling, etc.

## 3. Conclusion

Compare the fairness definition from step 1 and the signal from step 2. Then previous conclusions will change.

## Part 3. Computational fairness (ML)

# From statistics to ML: computational fairness

1. This term was created in the ML field around 5~10 years ago.
2. ML focuses on the prediction accuracy, so the key is to treat **prediction accuracy as resource**.
3. Examples & consequences of unequal prediction accuracy
  - Predicting economic development for rich vs. poor areas.
  - Predicting transit demand for senior vs. young people.
  - Predicting the adoption of new technology for racial minority vs. majority groups.
4. Unequal prediction accuracy leads to further unequal treatment.
  - Fewer infrastructure investment in poor areas
  - Less transit development for the senior areas.
  - Less new technology delivery in racial minority groups.
5. ML approaches could introduce **regularization** to rebalance prediction accuracy across disadvantaged vs. advantaged social subgroups to achieve **computational fairness**.

# Various concepts in computational fairness

## Definition of fairness in ML

- Accuracy parity. (similar to  $\hat{\beta}_1 = 0$ )
- Threshold parity. (similar to  $\hat{\beta}_0 = 0$ )
- Positive discrimination. (similar to  $\hat{\beta}_1 <> 0$ )
- Others: equal opportunities, etc.

## Example: accuracy parity

$$P(\hat{y} = y | x = 1) = P(\hat{y} = y | x = 0)$$

Sometimes it is hard to obtain the exact equality form, so we examine:

$$\lambda_1 < \frac{P(\hat{y} = y | x = 1)}{P(\hat{y} = y | x = 0)} < \lambda_2$$

# What analytical fairness (Stats & ML) can and cannot do

## Can do:

1. Major premise - Provide **exact definitions for fairness**

- Rawlsian fairness
- Equity
- Equality
- etc.

2. Minor premise - Provide **rigorous analytics** about facts/evidence

- Statistical regressions
- Network analysis
- ML

3. Concluding fairness evaluation

## Cannot do:

Choose the ultimate fairness rule.

- Equity and equality rules inherently conflict.
- Rawlsian fairness and equity may not be satisfied simultaneously
- Rawlsian fairness and equality may not be satisfied simultaneously
- etc.

## Comments

1. However, traditional planning practices cannot identify the ultimate fairness rule either.
2. This fundamental conflict among fairness rules reveals the **power** of analytical fairness, not weakness.
3. The single ultimate fairness rule is context-dependent, and heavily depend on social preferences.