

# What is a Linked List

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A linked list is a structure used for storing a collection of data that has the following properties:

- Successive elements are connected with a pointer (*not necessarily contiguous memory*)
- The last element points to **nothing**
- They grow and shrink during the execution of the program (*mutable*)
- Can be made as long as required (memory bound)

## Abstract Data Type

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### Main Operations

- **Insert:** insert an element to the list
- **Delete:** delete an element from the list

### Auxiliary Operations

- *Delete List:* delete the list and all its elements
- *Count:* give the length of the list
- *Find nth node from the end of the list*

## Difference with Array (SArray in Julia)

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Array elements are **contiguous in memory** and can be accessed in constant time (given the pointer at the beginning and the length of each element, you just need to read `n*size(typeof(element))` and move the pointer)

### Advantages

- Read and Write element in  $O(1)$
- Easy to use
- Deletion and insertion at ending is easy (if the array is not full)

### Disadvantages

- **Fixed size:** once the memory is allocated that's the size of the array
- **Block allocation:** need to find the space
- **Waste of space:** if you only use part of the array
- **Complex position based insetion:** If the array is smaller than its maximum size and I want to insert or remove an element at a certain position, I need to move ALL the other elements coming after (expensive at worst  $O(N)$  if it's at the beginning)

# Difference with Dynamic Arrays (is it the implementation of Array in Julia? Not sure)

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Also known as **array lists**, they are similar to static arrays, but when one finishes, I can allocate a new chunk of memory and linking it.

Something in between lists and arrays

## Linked Lists

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### Advantages

- Can insert an element in  $O(1)$ :
  - Create a new element at `new_ptr`
  - Get `tmp -> old_ptr`
  - Change `old_ptr -> new_ptr`
  - Point my new object to `new_ptr`
- I can easily make a linked list of different elements

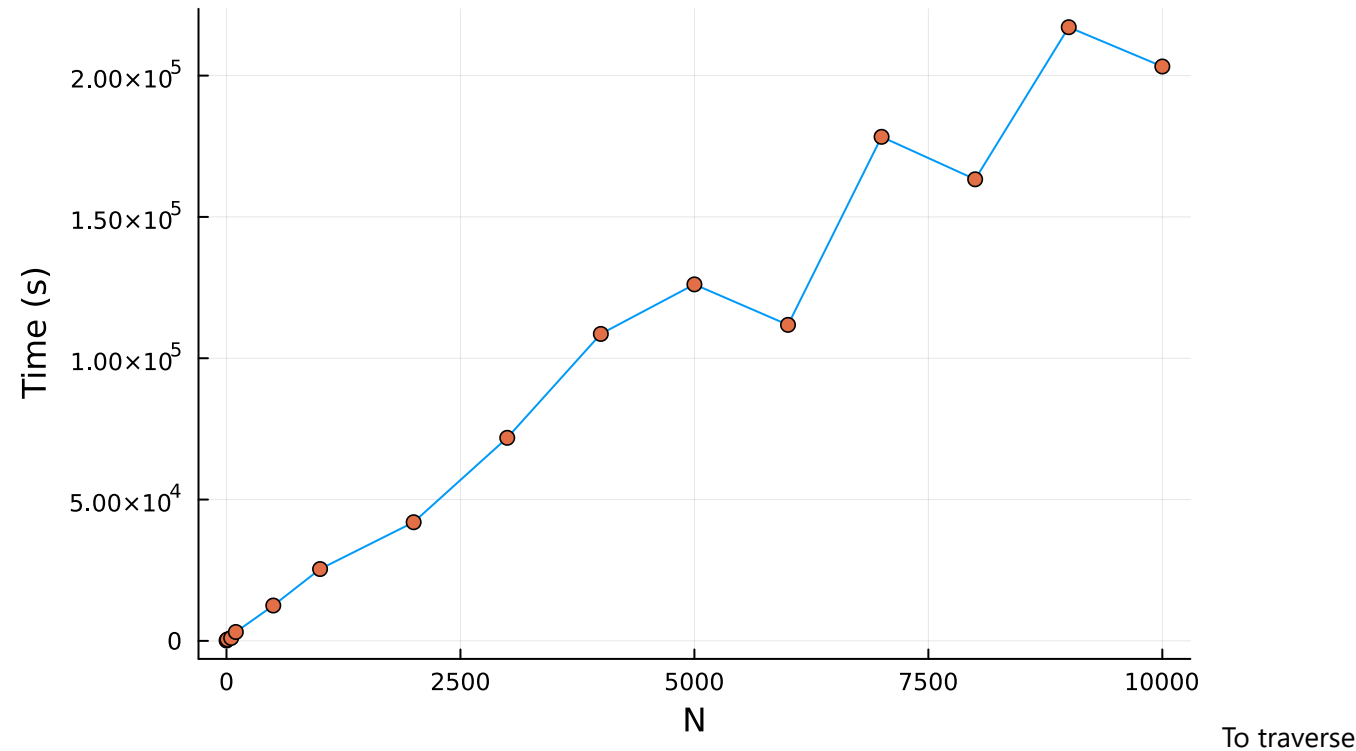
### Disadvantages

- Reaching any point except the beginning can take  $O(N)$  (thus for insertion I need to take that into account)

### Single Linked List

Traverse:

### Time to compute length List

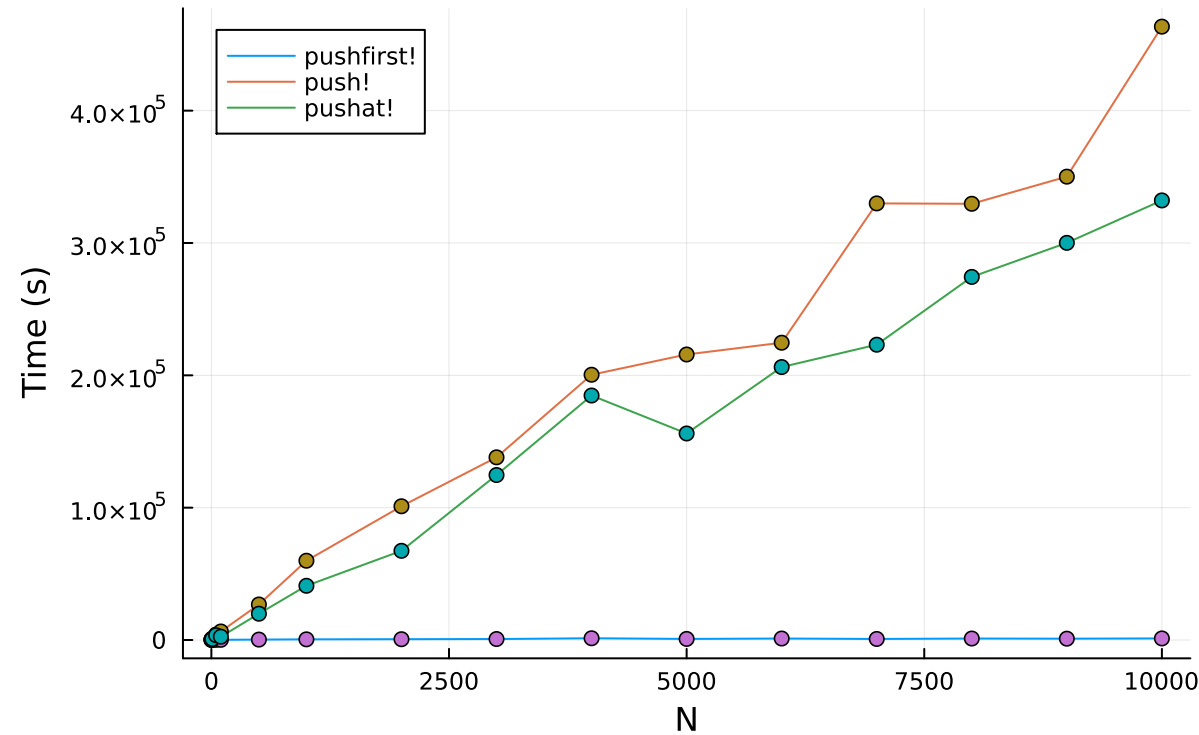


it I need to get all the elements in the list until I hit **Nothing** (see **ListLength**)

- Time Complexity: O(N) [to traverse while counting]
- Space Complexity: O(1) [to allocate counter]

Insert Node:

### Time to insert element



Insert at the beginning (**pushfirst!**)

- Create new element **new\_node**

- Make new\_node point at head
- Substitute pointed to head to pointer to new\_node
- Time Complexity:  $O(1)$
- Space Complexity:  $O(1)$

### Insert at the end (push!)

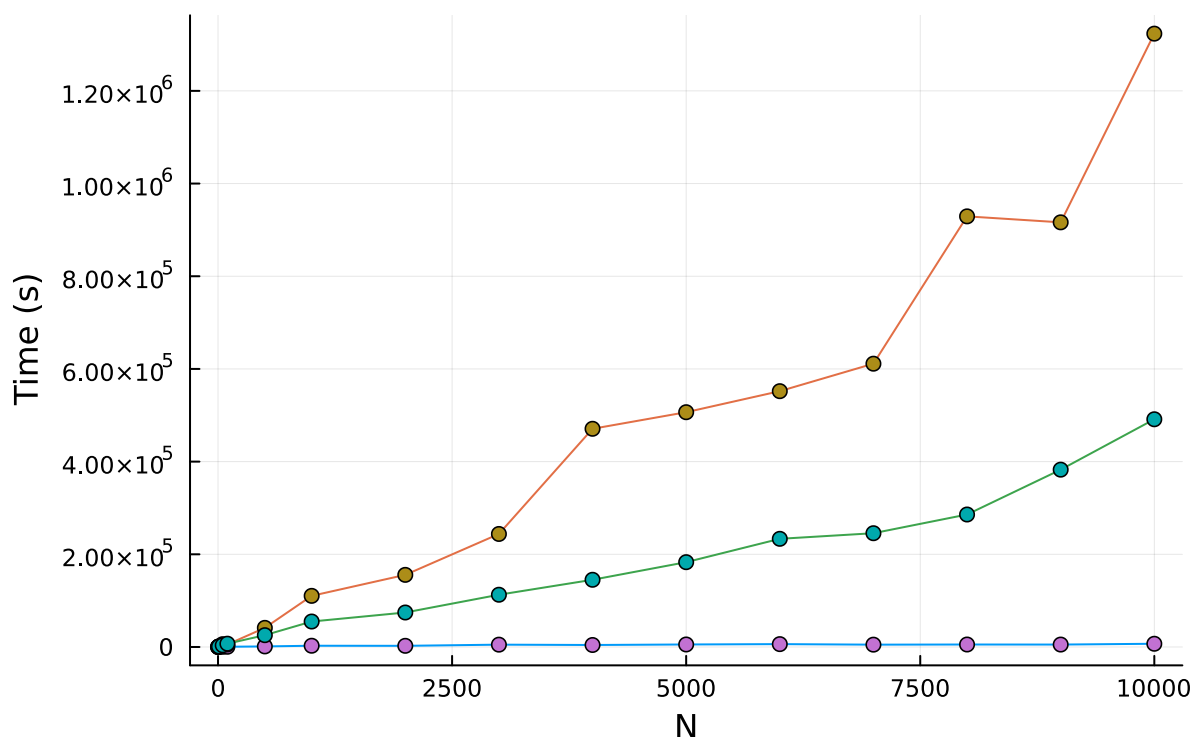
- Create new element new\_node
- Travel to the end ( $O(N)$ )
- Modify last pointed to nothing -> new\_node
- Time Complexity:  $O(N)$
- Space Complexity:  $O(1)$

### Insert in the middle (pushat!)

- Create new element new\_node
- Travel to  $n-1$  nodes
- copy pointer of  $n-1$  in tmp
- change pointer of  $n-1$ ->new\_pointer
- Point new pointer to tmp
- Time Complexity:  $O(N)$
- Space Complexity:  $O(1)$

### Delete Node

Time to compute Pop List



### Delete at the beginning (popfirst!)

- `new_head = next(head)`
- `list.head = new_head`
- no need to get rid of the node: **garbage collection**
- Time Complexity:  $O(1)$
- Space Complexity:  $O(1)$

### Delete at the end (**pop!**)

- Create new element `new_node`
- Travel to the end-1  $O(N)$
- Set `end-1` node.next to `nothing`
- garbage collection
- Time Complexity:  $O(N)$
- Space Complexity:  $O(1)$

### Delete in the middle

- Create new element `new_node`
- Travel to `i-1` node (up to  $O(N)$ )
- set `new_node.next` -> `i-1` node.next
- set `i-2` node.next -> `new_node`
- Time Complexity:  $O(N)$
- Space Complexity:  $O(1)$