Path and Hash Chain Splitting