标签 通项公式 下的文章

「TJOI / HEOI 2016」求和 (https://blog.orzsiyuan.com/archives/TJOI-HEOI-2016-Sum/)

> 题目链接：LOJ 2058 (https://loj.ac/problem/2058)

在 2016 年，佳媛姐姐刚刚学习了第二类斯特林数，非常开心。

现在他想计算这样一个函数的值：

$f(n) = n\sum i=0 i\sum j=0 S(i, j) \cdot 2^j \cdot j!$

$S(i, j)$ 表示第二类斯特林数，递推公式为: $S(i, j) = j \cdot S(i - 1, j) + S(i - 1, j - 1), 1 \le j \le i - 1$。

边界条件为：$S(i, i) = 1(i \ge 0), S(i, 0) = 0(i \ge 1)$。

你能帮帮她吗?

数据范围：$1 \le n \le 10^5$。

Siyuan（https://blog.orzsiyuan.com/author/1/） 2019 年 08 月 31 日

「算法笔记」生成函数求数列通项公式 (https://blog.orzsiyuan.com/archives/Sequence-of-General-Term-Formula/)

√ 利用生成函数，可以求解数列的通项公式。本文以「斐波那契数列」为例。

Siyuan（https://blog.orzsiyuan.com/author/1/） 2019 年 06 月 27 日

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