

PRACTICAL No.1

Topic - Basic of 'R' software.

- 1) R is a software for data analysis and statistical computing.
- 2) This software is used to bring in effective data handling and output storage is possible.
- 3) It is possible of graphical display.
- 4) It is a free software

Ex.

$$1) 2^2 + \sqrt{25} + 35$$

$$\Rightarrow 2^2 + \text{sqrt}(25) + 35$$

[I] 44.

$$2) 2 \times 5 \times 3 + 62 \div 5 + \sqrt{49}$$

[I] 49.4.

$$3) \sqrt{76 \times 4 \times 2} + 9 \div 5$$

$$\Rightarrow \text{sqrt}((76 + 4 * 2 + 9) / 5)$$

[I] 128

$$4) 42 + 1 - 10 | + 7^2 + 9 \times 5$$

$$\Rightarrow [I] 128$$

5) $x=20$ find $x^2y^2, \sqrt{y^3-x^3}, x+y,$
 $y=30$ $|x-y|$
 x^2+y^2
 $x^2+y^2 = [1] 50$ $|x-y|$
 $x^2+y^2 = [1] 100$
 $\sqrt{y^3-x^3}$
 $\text{exp}(y^3-x^3)$
 $OJ 137.84$

6) $[2, 3, 4, 5]^T \cdot c(4, 5, 6, 18) \times 3$
 $c[2, 3, 4, 5]^T \cdot [1] 18, 15, 18, 24$
 $4, 6, 9, 2, 5$

7) $c(2, 3, 5, 7) \times c(-2, -3, -5, -4)$
 $[1] -4, -9, -25, -28$
 $c(1, 2, 3, 4, 5, 6)^T \cdot c(2, 3)$
 $OJ 89, 64, 25, 216$

Find the sum product maximum, minimum of the values
 $5, 8, 6, 7, 9, 10, 15, 5.$

Solⁿ $x = c(5, 8, 6, 7, 9, 10, 15, 5)$
 $\text{length}(x)$
 $[1] 8$
 $\text{Sum}(x)$
 65

Q3 for matrix $\begin{bmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \\ 4 & 8 \end{bmatrix}$

Solⁿ $x \leftarrow \text{matrix}(\text{nrow} = 4, \text{ncol} = 2,$
 $\text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

$$\begin{bmatrix} [1] & [2] \\ [1] & 1 & 6 \\ [2] & 2 & 7 \\ [3] & 3 & 8 \\ [4] & 4 & 9 \end{bmatrix}$$

Q3 for $x = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix} y = \begin{bmatrix} -2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix}$ find $x+y, xxy, 2x+3y.$

Solⁿ $x \leftarrow \text{matrix}(\text{nrow} = 3, \text{ncol} = 3)$
 $\cdot \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8, 9)$

$y \leftarrow \text{matrix}(\text{nrow} = 3, \text{ncol} = 3,$
 $\text{data} = c(1, -2, 10, 4, 8, 6, 10, -11, 12))$

$x+y$	$[1,1]$	$[2,1]$	$[3,1]$	$2xy$	$[1,1]$	$[2,1]$	$[3,1]$
$[1,1]$	3	8	17	$[1,1]$	2	16	70
$[2,1]$	0	13	-3	$[2,1]$	-4	40	-88
$[3,1]$	13	12	21	$[3,1]$	-30	-36	-108

$2x+3y$

8	20	44
-2	34	-17
36	90	54

Q37 $x = c(2, 4, 6, 11, 3, 5, 7, 18, 16, 14, 17, 14, 19, 3, 2, 5, 0, 15, 9, 14, 18, 19, 12)$

$\text{length} = \text{x}$

$a = \text{table}(x)$

$\text{transform}(x)$

$x \quad f_{\text{eq}}$

0 1

1 2

2 3

3 1

4 2

5 1

6 2

7 1

8 1

9 1

10 2

11 1

12 1

13 1

14 2

15 1

16 2

17 1

18 1

19 2

$\triangleright \text{breaks} = \text{seq}(0, 20, 5)$

$\triangleright b = \text{cut}(x, \text{breaks}, \text{right} = \text{F})$

$\triangleright c = \text{table}(b)$

$\text{transform}(c)$

$b \quad f_{\text{reg}}$

[0, 5] 8

[5, 10] 5

[10, 15] 4

[15, 20] 6

\int

PRACTICAL NO. 2

Topic - Problems on pdf and cdf

i) Can following be cdf?

$$i. f(x) = \begin{cases} 2-x & ; 1 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

$$ii. f(x) = \begin{cases} 3x^2 & ; 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$iii. f(x) = \begin{cases} 3x^2 & ; 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

$$iv. f(x) = \begin{cases} 3x(1-x) & ; 0 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

Solution.

$$ii) \int 3x^2 dx = \left[\frac{3x^3}{3} \right]_0^1 = x^3 \Big|_0^1 = 1$$

So pdf.

$$i) f(x) dx = 1 \quad \text{condition for pdf} \\ \int (2-x) dx \Rightarrow \int_1^2 2 dx = \int_1^2 x dx \Rightarrow [2x]_1^2 - [\frac{x^2}{2}]_1^2, \\ (4-2) - (2-0.5) \neq 1 \quad \text{not pdf}$$

$$iii) f(x) = \begin{cases} \frac{3x}{2} (1-\frac{x}{2}) & ; 0 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

$$\Rightarrow f(x) = \int_0^2 \frac{3x}{2} - \frac{3x^2}{4} dx \Rightarrow \int_0^2 \frac{3x}{2} dx = \int_0^2 \frac{3x^2}{4} dx \\ \left[\frac{3x^2}{4} \right]_0^2 - \left[\frac{x^3}{4} \right]_0^2 \Rightarrow \left[\frac{3(2)}{4} - 0 \right] - [2]$$

$$\therefore 3-2=1$$

∴ it's pdf.

2. following be pmf ?.

1.	x	1	2	3	4	5
	$p(x)$	0.2	0.3	-0.1	0.5	0.1

2.	x	0	1	2	3	4	5
	$p(x)$	0.1	0.3	0.2	0.2	0.1	0.1

3.	x	10	20	30	40	50
	$p(x)$	0.2	0.3	0.3	0.2	0.2

Soln

1. Since 1 valid rge rve, so it is not pmf

2. Since $p(x) \geq 0, \forall x$

and $\sum p(x) = 1$ if ex pmf

$$\text{prob} = C(0.1, 0.3, 0.3, 0.2, 0.1, 0.1)$$

sum (prob)

1

$$3. \text{prob} = C(0.2, 0.3, 0.3, 0.2, 0.2)$$

sum (prob)

-1.2

it is not pmf.

3) find $P(x \leq 2), P(2 \leq x \leq 4), P(\text{at least } 4), P(3 \leq x < 6)$

x	0	1	2	3	4	5	6
$p(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$P(x \leq 2) = P(0) + P(1) + P(2) = 0.1 + 0.1 + 0.2 = 0.4$$

$$P(2 \leq x < 4) = P(2) + P(3) = 0.2 + 0.2 = 0.4$$

$$P(\text{at least } 4) = P(4) + P(5) + P(6) = 0.1 + 0.2 + 0.1 = 0.4$$

$$P(3 < x < 6) = P(4) + P(5) = 0.1 + 0.2 = 0.3$$

4) find cmf

x	0	1	2	3	4	5	6
$p(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\text{prob} = C(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)$$

cumsum (prob)

$$[1] 0.1, 0.2, 0.4, 0.6, 0.7, 0.9, 1$$

$$f(x) = 0$$

if $x < 0$

$$\cdot 1 \quad \text{if } 0 \leq x < 1$$

$$\cdot 2 \quad \text{if } 1 \leq x < 2$$

$$\cdot 3 \quad \text{if } 2 \leq x < 3$$

$$\cdot 4 \quad \text{if } 3 \leq x < 4$$

$$\cdot 5 \quad \text{if } 4 \leq x < 5$$

$$\cdot 6 \quad \text{if } 5 \leq x < 6$$

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$$\cdot 124 \quad \text{if } 123 \leq x < 124$$

PRACTICAL No 3

Topic - Probability distribution and binomial distribution.

i) Find the cdf of following pmf and Draw the graph.

x	10	20	30	40	50
$P(x)$	0.15	0.25	0.3	0.2	0.1

Soln

$$x = c(10, 20, 30, 40, 50)$$

$$\text{prob} = c(0.15, 0.25, 0.3, 0.2, 0.1)$$

cumsum(p**prob**)

$$[1] 0.15 \ 0.40 \ 0.7 \ 0.9 \ 1.00$$

$$F(x) = \begin{cases} 0 & \text{if } x < 10 \\ 0.15 & 10 \leq x < 20 \\ 0.40 & 20 \leq x < 30 \\ 0.70 & 30 \leq x < 40 \\ 0.90 & 40 \leq x < 50 \\ 1 & x \geq 50 \end{cases}$$

plot(x, prob, xlab = "values", ylab = "probability", main = "graph 'cdf'")

Binomial distribution

Suppose there are 12 MCQ in a test. Each question has 5 options. Only one of them is correct. Find the probability of having one correct answer. (2) alternate 4 correct answers.

Soln

It is given that $n=12$, $p=1/5$, $q=4/5$

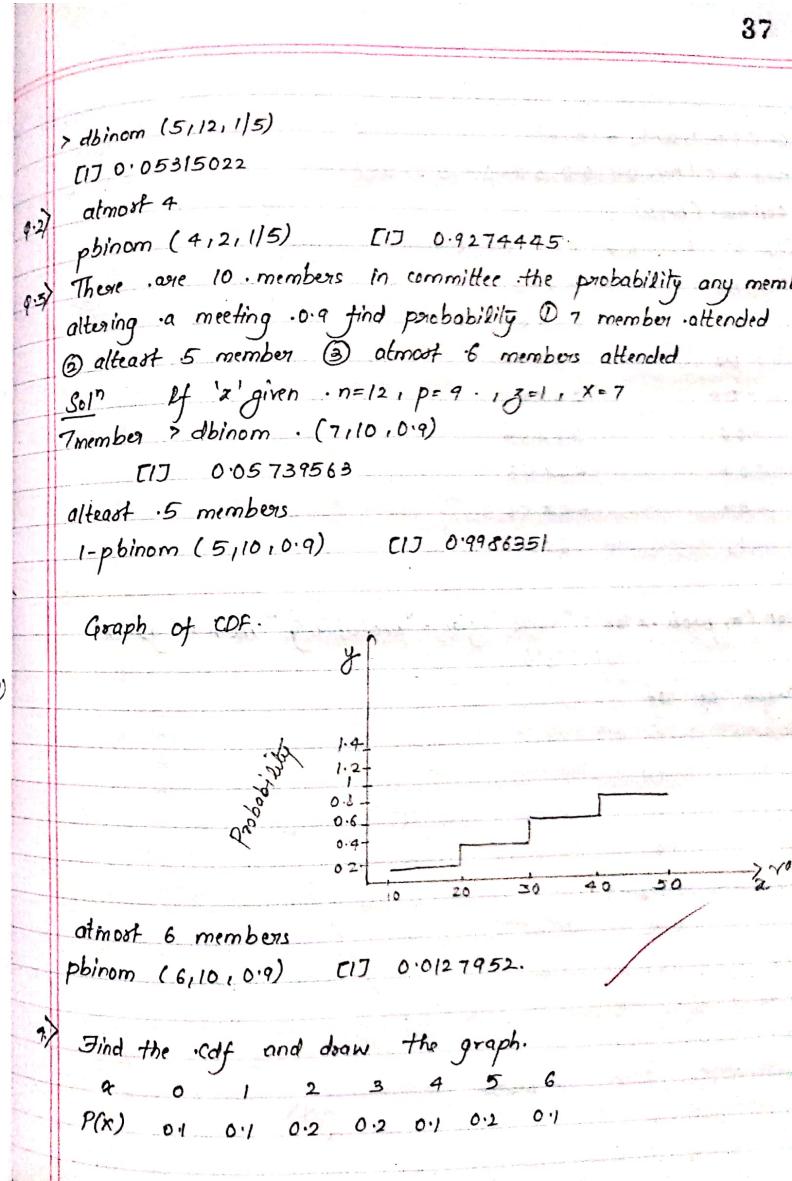
$X = \text{total no. of correct answers}$.

$\sim B(n, p)$

$$>p = 1/5$$

$$>n = 12$$

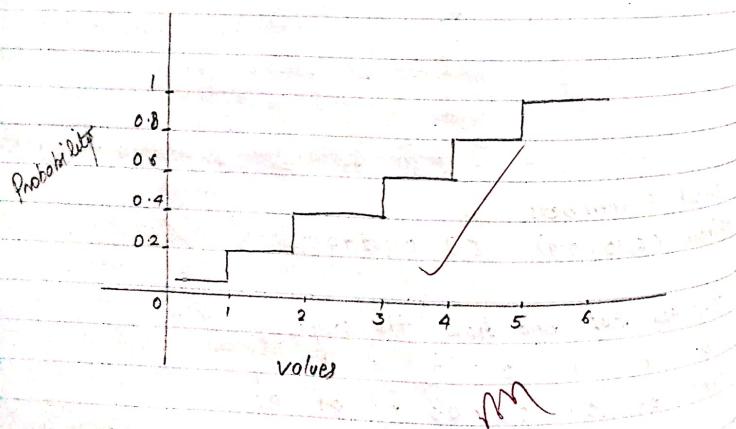
$$>q = 4/5$$



$x = c(0, 1, 2, 3, 4, 5, 6)$
 $prob = c(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)$
 cumsum (prob)
 [I] 0.1 0.2 0.4 0.6 0.7 0.9 1
 $P(x) = 0$ if $x < 0$
 $= 0.1$ if $0 \leq x \leq 1$
 $= 0.2$ if $1 \leq x \leq 2$
 $= 0.4$ if $2 \leq x \leq 3$
 $= 0.6$ if $3 \leq x \leq 4$
 $= 0.7$ if $4 \leq x \leq 5$
 $= 0.9$ if $5 \leq x \leq 6$
 $= 1$ if $6 \leq x \leq 7$

$\text{plot}(x, prob, xlab = "value", ylab = "probability", main = "graph", cdf = "s")$

Graph of cdf



PRACTICAL NO.4 - Binomial Distribution

- 1) Find the complete binomial distribution when $n=5$ and $p=0.1$
 2) Find the probability of exactly 10 success. $n=100$. trial with $p=0.1$
 3) x follows binomial distribution with $n=12$, $p=5$, find

- ① $P(x=5)$
- ② $P(x \leq 5)$
- ③ $P(x \geq 7)$
- ④ $P(5 \leq x \leq 7)$

⇒ The probability of salesman make a sell to a customer is 0.15
Find the probability.

- ① No sale for 10 customers, no more than 3 sale in 20 customers
 ② A student write 5 MCQs, each question that 4 options out of which 1 correct calculate the probability atleast 3 correct answer.

NOTE - $P(x=x) = \text{dbinom}(x, n, p)$

$P(x \leq x) = \text{pbisnom}(x, n, p)$

$P(x \geq x) = 1 - \text{pbisnom}(x, n, p)$

To find the value of 'x' for which the probability is p , command is $\text{qbinom}(p, n, p)$

- 1) $n=5$ $p=0.1$
 $\text{dbinom}(0:5, 5, 0.1)$
 [I] 0.59049 0.32805 0.07290 0.00810 0.00004 0.00001
 2) $\text{dbinom}(10, 100, 0.1)$ $n=100$
 [I] 0.1318653
 3) $n=12$ $p=0.25$
 $\text{dbinom}(5:12, 0.25) \cdot P(x=5)$
 [I] 0.1032414

$$\text{ii. } p(x \leq 5) \\ p\text{binom}(5, 12, 0.25)$$

[IJ] 0.9455

$$\text{iii. } p(x > 7) = 1 - p(x \leq 7) = 1 - p\text{binom}(7, 12, 0.25) \\ [IJ] 0.00278151$$

$$\text{iv. } p(5 < x < 7) \\ p\text{binom}(6, 12, 0.25) \\ 0.04014945$$

$$4) 1. n=10, p=0.15, x=0 \\ p\text{binom}(0, 10, 0.15) \\ [IJ] 0.1980744$$

$$\text{ii. } n=20, p=0.15 \\ p(x \geq 3) = 1 - p(x \leq 2) = 1 - p\text{binom}(3, 20, 0.15) \\ [IJ] 0.1980744 0.3522148$$

$$5) n=5, p=0.25, x=3 \\ p(x \geq 3) = 1 - p(x \leq 2) \\ = 1 - p\text{binom}(2, 5, 0.25) \\ [IJ] 0.1035156$$

6) X follows binomial distribution $n=10, p=0.4$ plot the graph of pdf and cdf.

$$\text{Soln} \quad n=10; p=0.4 \rightarrow x=0:n$$

$$pprob = p\text{binom}(x, n, p)$$

$$cumpprob = p\text{binom}(x, n, p)$$

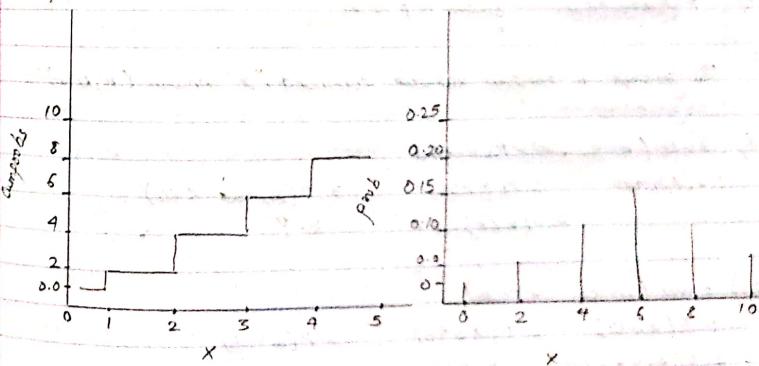
$$d = \text{dataframe}\left(\{"x value": x, "probability": pprob\}\right)$$

print(d)

x values	probability
0	0.00606466176
1	0.0403107840
2	0.120932520
3	0.2149908480
4	0.2508226560
5	0.2006581248
6	0.1114767360
7	0.424673280
8	0.0106168320
9	0.0015728640
10	0.0001048576

plot(x, sum, prob, "s")

plot(x, prob, "h")



PRACTICAL No.5

Topic - Normal Distribution.

$$1) P[z=x] = \text{dnorm}(x, \mu, \sigma)$$

$$2) P(x \leq z) = \text{pnorm}(z, \mu, \sigma)$$

$$3) P(x \geq z) = 1 - \text{pnorm}(z, \mu, \sigma)$$

$$4) P(z_1 < z < z_2) = \text{pnorm}(z_2, \mu, \sigma) - \text{pnorm}(z_1, \mu, \sigma)$$

To find the value of 'k' we shown that

$$5) P(X \leq k) = p, \quad qnorm(p, \mu, \sigma)$$

To generate 'n' random variable command, "x" $\sim \text{rnorm}(n, \mu, \sigma)$

Q.1) $X \sim N(\mu=50, \sigma^2=100)$. Find

$$\begin{array}{lll} 1. P(z \leq 40) & 2. P(z \geq 55) & 3. P(40 \leq z < 60) \\ 4. P(z \leq k) = 0.7 & & k=? \end{array}$$

Q.2) $X \sim N(\mu=100, \sigma^2=96)$

$$\begin{array}{lll} 1. P(z \leq 10) & 2. P(z \leq 95) & 3. P(z > 115) \\ 4. P(95 \leq z \leq 105) & 5. P(z \leq 15) = 0.4 & k=? \end{array}$$

Q.3) Generate 10 random numbers from a normal distribution with mean = 60, sd = 5. Also calculate sample mean, median, variance & sd.

4) Draw the graph of standard normal distribution

$$1) a = \text{pnorm}(40, 50, 10)$$

$$\text{cat}("p(z \leq 40) = ", a)$$

$$\Rightarrow p(z \leq 40) = 0.1586553$$

$$2) b = 1 - \text{pnorm}(55, 50, 10)$$

$$\text{cat}("p(z > 55) = ", b)$$

$$p(z > 55) = 0.3085375$$

$$3) c = \text{pnorm}(60, 50, 10) - \text{pnorm}(42, 50, 10)$$

$$\text{cat}("p(42 \leq z \leq 60) = ", c)$$

$$p(42 \leq z \leq 60) = 0.6294893$$

$$4) d = \text{qnorm}(0.7, 50, 10)$$

$$\text{cat}("p(z \leq k) = 0.7, k is = ", d)$$

$$p(z \leq k) = 0.7, k is = 55.24401$$

$$5) e = \text{qnorm}(0.4, 100, 6)$$

$$\text{cat}("p(z \leq k) = 0.4, k is = ", e)$$

$$p(z \leq k) = 0.4, k is = 98.47992$$

$$6) f = \text{pnorm}(95, 100, 6)$$

$$\text{cat}("p(z \leq 95) = ", f)$$

$$p(z \leq 95) = 0.2023284$$

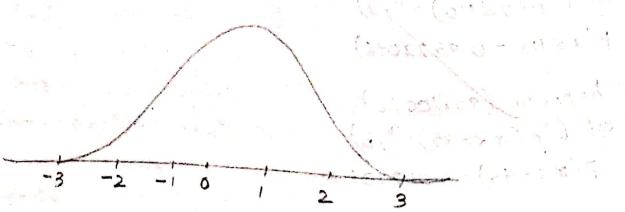
四

$\sigma = \text{sqrt}(m)$	(10, 60, 5)
$n = 10$	
$\mu = 60$	
$\sigma = 5$	
[1] 58.45543	55.02759
60.54697	61.79573
mean (a)	n=10
[1] 61.18175	variance = $(\sum x - \bar{x})^2 / n$
median (a)	[1] 23.22858
[1] 60.27534	$sd = \text{sqrt}(\text{variance})$
sd(a)	• 4.819604
• 5.080309	101107322
$\sigma^2(a)^{1/2}$	
25.80954	

$$4) x = \text{neq}(-3, 3, b_4 = 0.1)$$

$$y = dnorm(x)$$

```
plot(x,y, xlab = "z value", ylab = "probability", main = "standard normal distribution", "l").
```



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PRACTICAL NO. 6

Topic -

Test the hypothesis (H_0):

17) Test $H_0: \mu = 10$ against $H_1: \mu \neq 10$

A sample of size 400 is selected which gives mean 10.2 and $sd = 2.25$.
Test the H_0 @ 5% level of significance.

m_0 = mean of population.

m_x = mean of size

sd = standard deviation

$$z_{cal} = (m_x - m_0) / (C_{sd} \sqrt{n}))$$

```
cat ("zcal is ", zcal)
```

z_{cal} is 1.77778

pvalue = 2 * (1 - pnorm (abs (zcal)))

--pvalue

[1] 0.07544036

Since 0.07544036 is more than 0.05 : we will accept the H_0 .

2) Test the (H_0) $\mu = 75$ $H_1: \mu \neq 75$.

A sample of size 100 is selected and sample mean = 80 with $sd = 3$.
Test the (H_0) @ 5% level of significance.

`zcal = (mx - mo) / (sd * sqrt(n))`
`cat("zcal is:", zcal)`

4) Experience has shown that 20% students of college smoke. A sample of 400 students reveal that out of 400 only 50 smoke. Test the H_0 that experience gives the correct proportion or not.

$$zcal = (p - P) / \sqrt{P(1-P)/n}$$

cat ("zcal is =", zcal)

-3.75

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

pvalue

[1] 0.0001768346

P

[1] 0.125

5) Test the H_0 : $P = 0.5$ against H_1 : $P \neq 0.5$

A sample of 200 is selected and sample proportion is calculated (p) = 0.56
Test H_0 @ 1% of (H_0)

$$zcal = (p - P) / \sqrt{P(1-P)/n}$$

cat ("zcal is =", zcal)

= 1.697056

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

pvalue

[1] 0.08965602

P

[1] 0.56

Value accepted.

AM
97.0170

$$zcal \text{ is } 16.6667$$

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

pvalue

[1] 0

3) Test the H_0 : $\mu = 25$ against H_1 : $\mu \neq 25$

0.5% level of significance. The following of sample 30 is selected.

20, 24, 27, 35, 30, 46, 26, 27, 10, 20, 30, 37, 35, 21, 22, 23, 24, 25,
26, 27, 28, 29, 30, 39, 27, 15, 19, 22, 20, 18

$$\bar{x} = \text{mean}(x)$$

\bar{x}

[1] 30 26.067

$$n = \text{length}(x)$$

n

[1] 30

$$\text{variance} = (30-1) * \text{var}(x) / 30$$

variance

[1] 7.279

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

pvalue

[1] 0.42

$$zcal = (\bar{x} - 25) / (\text{sd})(\sqrt{n})$$

cat ("zcal is =", zcal)

0.8025454

Practical No.7

Topic - Large Sample Test.

A study of noise level into hospital is calculated below. test the hypothesis of noise level in two hospital are same or not.

	Hos A	Hos B
No. of sample	84	34
obs		
Mean	.61	59
sd	7	8

$\Rightarrow H_0$ = Noise level .

$$n_1 = 84$$

$$m_x = 61$$

$$m_y = 59$$

$$sdx = 7$$

$$sdy = 8$$

$$z = (m_x - m_y) / \sqrt{(sdx^2/n_1) + (sdy^2/n_2)}$$

$$z$$

$$[1] 1.273682$$

egt ("z calculated is = 'z'")

z calculated is = 1.273682

$$pvalue = 2 * (1 - pnorm(abs(z)))$$

pvalue

$$0.04350026$$

$$0.2027$$

H_0 is at 5% level of significance.

$$p_2 = 0.155$$

$$p = (n_1 \cdot p_1 + n_2 \cdot p_2) / (n_1 + n_2)$$

$$q = 1 - p$$

$$P \\ 0.175$$

$$Z \\ = 0.82225.$$

$$\bar{z} = (p_1 - p_2) / \sqrt{p \cdot q \cdot (1/n_1 + 1/n_2)}$$

$$Z \\ 1.76547$$

$$pvalue = 2 * (1 - pnorm(abs(z)))$$

$$0.0774$$

We accept the H_0 at 5% level of significance.

- 4) From each of following boxes of apples a sample size of 200 is collected. It is found that there are 44 bad apples in first sample and 30 in second sample. Test hypothesis that 2 boxes are equivalent in number of bad apples?

$\Rightarrow H_0$ = Two boxes

$$p_1 = 44/200$$

$$p_2 = 30/200$$

$$n_1 = 200$$

$$n_2 = 200$$

$$P = (n_1 \cdot p_1 + n_2 \cdot p_2) / (n_1 + n_2)$$

$$P \\ 0.185.$$

$$q = 1 - p$$

$$0.815$$

$$Z = (p_1 - p_2) / \sqrt{p \cdot q \cdot (1/n_1 + 1/n_2)}$$

$$Z$$

- 2) Two random sample areas of size 1000 and 2000 are drawn from two populations with mean 67.5 and 68 respectively. SD of test hypothesis the mean of population are equal.

H_0 = Two population

$$n_1 = 1000$$

$$n_2 = 2000$$

$$mx_1 = 67.5$$

$$my_1 = 68$$

$$sdx = 2.5$$

$$sdy = 2.5$$

$$y = (mx_1 - my_1) / \sqrt{(sdx^2/n_1) + (sdy^2/n_2)}$$

$$y \\ -5.163978$$

cat ('y calculated is = "y")

$$y calculated is = -5.163978$$

$$pvalue = 2 * (1 - pnorm(abs(y)))$$

pvalue.

$$2.415764.$$

We reject the H_0 at 5% level of significance

- In a first year class 20% of random sample of 400 students had defective eye sight. In second class 15.5% of 500 students is the difference of proportion same?

H_0 = proportion of population

$$n_1 = 400$$

$$n_2 = 500$$

$$p_1 = 0.2$$

$$1.802741 \\ \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

0.07142

pvalue < 0.05 accept the H_0 5% level of significance

5) In MA class of sample 60 mean height is 63.5 inch withsd 2.5 in a

In mean M.Com class out of 50 student mean height 69.5 inch withsd 2.5.

Test the hypothesis mean of MA & M.Com

$\Rightarrow H_0$ = mean of MA and M.Com

$$n_1 = 60$$

$$n_2 = 50$$

$$m_x = 63.5$$

$$m_y = 69.5$$

$$sd_1 = 2.5$$

$$sd_2 = 2.5$$

$$y = (m_x - m_y) / \sqrt{(sd_1^2/n_1 + sd_2^2/n_2)}$$

$$y$$

$$-12.53359$$

cat('y calculated is = "y")

y calculated is = -12.53359

pvalue = $2 * (1 - \text{pnorm}(\text{abs}(y)))$

pvalue

0

We reject the H_0 of 5%

level of significance.

Practical No. 8

Topic - Small Sample Test.

1) The flowers 10 selected and the weight founded 63, 68, 69, ..., 71, 72. Test the hypothesis that the mean weight 66cm or not at 1%.

\Rightarrow Mean = 66cm

$$x = c(63, 68, 69, 71, 71, 72)$$

t = test(x).

data = x

$$t = 4.794, df = 6$$

pvalue = 5.322.

alternative hypothesis

True mean is not equal to 0

Percent confidence level interval:

$$64.66479 \quad 71.62092$$

Sample estimate:

Mean of x

$$68.14286$$

pvalue less than 0.01, reject H_0 at 1% level of significance

2) 2 Random sample drawn from 2 different population sample = 8, 11, 16, 15, 18, 7

Sample 2 = 20, 15, 18, 9, 8, 10, 11, 12, 15, 18, 17, 16.

Test the hypothesis that there is no difference mean b/w the mean at 5%.

$\Rightarrow x = c(5, 10, 12, 11, 18, 15, 7)$
 $y = c(20, 15, 18, 9, 10, 11, 12, 8)$
 $t\text{-test}(x, y)$

data = x and y

t = 0.36247

df = 13.387

p-value = 0.7225

alternative hypothesis - True difference in means not equal to 0
percent confidence interval.

-5.192719

3.692719

Sample estimated:

Mean of x and y.

12.125 12.875

p-value greater than 0.05.

Accept H_0 at 5% of level of significance.

3) Following are weight 10 people before and after diet program
Test hypothesis that it effect or not.

Before 100, 125, 95, 96, 98, 112, 115, 104, 109, 110

After 95, 80, 95, 90, 100, 110, 85, 100, 101

$x = c(100, 125, 95, 96, 98, 112, 115, 104, 109, 110)$

$y = c(95, 80, 95, 90, 100, 110, 85, 100, 101)$

data : x and y.

t = 2.6991

df = 18.801

pvalue = 0.985

95 percent confidence interval

-18.72908

mean of difference

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pvalue greater than 0.5.

Accept H_0 at 5% level of significance.

4) Mark before and after a training program as given below.

Before : 20, 25, 32, 28, 27, 36, 35, 25

After : 30, 35, 32, 37, 37, 40, 40, 23

$\Rightarrow x = c(20, 25, 32, 28, 27, 36, 35, 25)$

$y = c(30, 35, 32, 37, 37, 40, 40, 23)$

$t\text{-test}(x, y, \text{paired} = \text{T}, \text{alternative} = \text{'greater'})$.

paired t-test.

data : x and y

t = -3.3859

df = 7

p-value = 0.9942

Mean is greater than 0

Percent confidence interval :

-8.957399

Sample estimate.

Mean of difference

-5.75

We accept H_0 at 5% level of significance

Q) 2 Random Sample were drawn from 2 random population and the values are.

$$A = 66, 67, 65, 75, 76, 82, 84, 88, 90, 92$$

$$B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 45, 97$$

Test whether the population have same variance at 5%.

$$x = c(66, 67, 65, 75, 76, 82, 84, 88, 90, 92)$$

$$y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 45, 97)$$

variance(x,y)

Compare 2 variance

data: x and y

$$F = 6.708660$$

$$\text{num df} = 3$$

$$\text{denom df} = 10$$

$$\text{p-value} = 0.6354$$

ratio of variance.

$$0.7063567$$

pvalue greater than 0.5

Accept H₀ at 5% level of significance.

Q) The arithmetic mean of sample of 100 observation is 52. if $sd = 7$. Test the hypothesis that the population mean = 55 or not at 5%.

$$\Rightarrow H_0: \text{population mean} = 55$$

$$n = 100$$

$$mx = 52$$

$$m_0 = 55$$

$$sd = 7$$

$$z = (mx - m_0) / (sd / \sqrt{n})$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$\text{pvalue} =$$

$$1.82153$$

$$\text{pvalue} < 0.05$$

Reject the 5% level of significance.

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Practical No. 9.

Chi-Square Distribution and ANOVA Box.

Q) Use the following data to test whether clearly new home dependent upon other condition or not:

\Rightarrow code of Home

code of child	Clean		Dirty	
	fairly	Dirty	70	50
	80		20	
	35		45	

H₀: col. of home and child are independent.

$$x = c(70, 80, 35, 50, 20, 45)$$

$$m = 3$$

$$n = 2$$

$$y = \text{matrix}(x, nrow = m, ncol = n)$$

y

[1] [2]

[1] 70 50

[2] 50 20

[3] 35 45

pv = chisq.test(y)

pv

pearson chi-square :

data: y

Pvalue is less than 0.05 we reject H₀ at 5%.

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\Rightarrow Table below shows a relation between the performance of mathematics and computer of CS student

Math

Comp	HG	MG	IG
	56	71	12
	47	163	38
	14	42	85

H₀: performance b/w Maths and computer are independent.

$$x = c(56, 47, 14, 71, 163, 42, 12, 38, 85)$$

$$m = 2$$

$$y = \text{matrix}(x, nrow = m, ncol = 3)$$

C1	C2	C3
[1]	56	12
[2]	47	38
[3]	14	85

$$pv = \text{chisq.test}(y)$$

pv

Pearson's chi-square test

data: y

x-square = 145.78, df = 4, p-value < 2.2e-16.

pvalue < 0.05. We reject H₀ at 5% test

3) Perform ANOVA for following data.

Variety	Observation
A	50, 52
B	53, 55
C	60, 58, 57, 56
D	52, 54, 55, 55

H₀: The mean of variety A, B, C, D are .

$$x_1 = c(50, 52)$$

$$x_2 = c(53, 55)$$

$$x_3 = c(60, 58, 57, 56)$$

$$x_4 = c(52, 54, 55, 55)$$

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```
d = stack(c.list(b1=x1, b2=x2, b3=x3, b4=x4))
names(d)
```

"values" "ind"

one way test (value data=d, var=equal=T)

one way analysis of means

data values and ind

F=11.735, num df=3, denom df=9, p-value=0.00183

aov=aov [value ~ ind, data=d]

summary (aov)

	Df	Sum Sq	Mean Sq	F-value	P>F(>F)
Td	3	71.06	23.687	11.73	0.00183 **
Residuals	9	13.17	2.019		

pr < 0.05 we reject H₀ at 5%.

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4) type observations

A	6,7,8
B	4,6,5
C	5,6,10
D	6,9,9

H₀: The mean of variety A,B,C,D equal

$$x_1 = c(6,7,8)$$

$$x_2 = c(4,6,5)$$

$$x_3 = c(5,6,10)$$

$$x_4 = c(6,9,9)$$

```
d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
name(d)
```

"values" "ind"

one way test (value ~ ind, data=d, var.equal=T)

one way analysis of means

data = values and ind

F=0.667, num df=3, denom df=8, pralyp=0.1139.

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aov=aov (value ~ ind, data=d)

summary (aov)

	Df	Sqmean	Sqf	values	P>(gt)
ind	3	18	6.00	2.667	0.119
Residuals	8	18	2.25		

p-value > 0.05 we accept H₀ at 0.05, at 5%

z = read csv("C:/users/Admin/Desktop")

x:

Practical 10

Non-parametric Test.

- 1) Following are the amount of sulphur oxide emitted by factory.
 data : 17, 15, 20, 23, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 19, 15, 23, 24, 26

Apply sign test to test hypothesis that the population median is 21.5 against alternative it is less than 21.5

H_0 : population median equal to 21.5
 it is less than 21.5

$$x = c$$

$$m = 21.5$$

$$sp = \text{length}(\mathbf{x}[\mathbf{x} > m])$$

$$sn = \text{length}(\mathbf{x}[\mathbf{x} < m])$$

$$n = sp + sn$$

$$pr = \text{binom}(sp, n, 0.5)$$

$$p \cdot r = 0.41$$

pvalue > 0.05 we accept 5% level of significance

NOTE - If alternative is greater than median.

- 2) For observation 12, 19, 31, 28, 23, 43, 40, 55, 42, 70, 63 apply sign test to population median is 25 against the alternative it is more than 25.

H_0 : population median equal to 25

H_1 : it is more than 25

$$m = 25$$

$$\mathbf{x} = c(12, 19, 31, 28, 43, 40, 55, 49, 70, 63)$$

$$sp = \text{length}(\mathbf{x}[\mathbf{x} > m])$$

$$sn = \text{length}(\mathbf{x}[\mathbf{x} < m])$$

$$n = sp + sn$$

$$pr = \text{binom}(sn, n, 0.5)$$

$$p \cdot r$$

$$EIJ = 0.0541875$$

pvalue is less than 0.05 we reject.

- 3) For following data

60, 65, 63, 89, 61, 71, 58, 51, 48, 56 test the hypothesis using wilcoxon sign rank test for testing the hypothesis.

The median is 60 against the alternative it is greater than 60

$$\Rightarrow H_0 : \text{Median } 60$$

$$H_1 : \text{greater than } 60$$

$$x = c(60, 68, 65, 89, 61, 71, 58, 51, 48, 56)$$

$$mu = 60$$

$$\text{wilcox} = \text{test}(x, "greater", mu = 60)$$

wilcoxon signed test with continuity correction
 data : \mathbf{x}

$$v = 29 \quad p\text{-value} = 0.2386$$

alternative hypothesis : true locations is greater than 60
 pvalue < 0.5 we reject H_0

NOTE - If the alternative is less

$$\text{wilcox.ttest}(x, alter = "less", mu = 60)$$

if the alternative is not equal to

$$\text{wilcox.ttest}(x, alter = 2\text{-sided})$$

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4) Using wilcoxon test the hypothesis median is 12 against the alternative is less than 12

12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 3, 20

$\Rightarrow H_0 = \text{Median } 15/12$

$H_1 = \text{less than } 12$

$x = c(12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20)$

wilcox. test(x, alter = "less", mu = 12)

wilcoxon signed rank test with continuity correction

data: x

V = 25; p-value = 0.2521

alternative hypothesis: true location is less than 12

pvalue value is 12.