

Lecture ÷ Trees-2

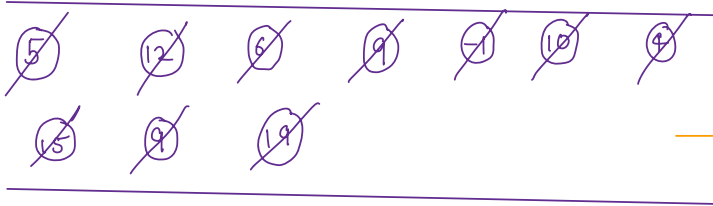
Agenda

- Level order traversal →
- Left and right view.
- Vertical level order →
- Top and bottom view
- Types of Binary tree
- Is tree height balanced? →

Qul Level order traversal.

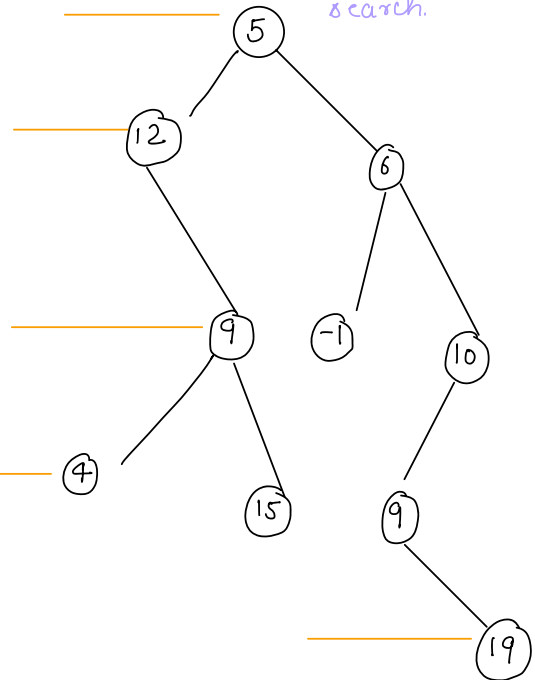
o/p ÷ 5 12 6 9 -1 10
 4 15 9 19

Data structure: Queue.



5 12 6 9 -1 10 4 15
9 19

bfs: Breadth first search.



Code:

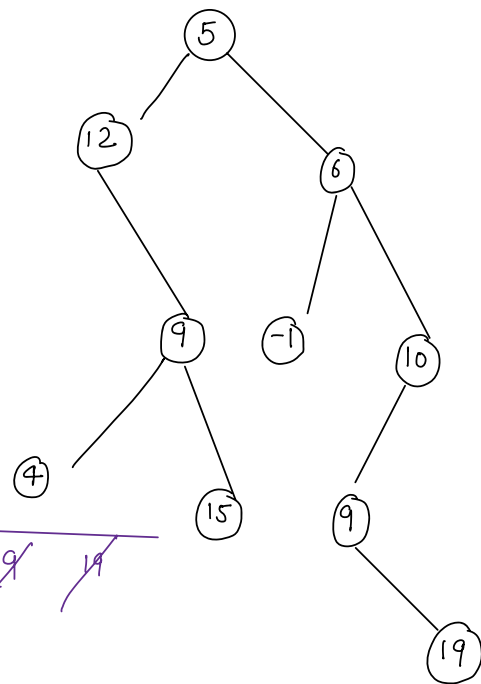
```
void levelorder( Node root) {  
    Queue < Node > q = new LinkedList<>();  
    q.add(root);  
    while( ! q.isEmpty() ) {  
        Node curr = q.poll();  
        print (curr.val);  
        if( curr.left != null ) {  
            q.add( curr.left );  
        }  
        if( curr.right != null ) {  
            q.add( curr.right );  
        }  
    }  
}
```

Tc: $O(n)$

Sc: $O(n)$

Q2: Level order traversal 2.

5
12 6
9 -1 10
4 15 9
19



~~5~~ ~~12~~ ~~6~~ ~~9~~ ~~-1~~ ~~10~~ ~~4~~ ~~15~~ ~~9~~ ~~19~~

currLevel = ~~1~~ ~~0~~ ~~1~~ ~~1~~ ~~0~~ ~~1~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~
 ↑ ↑
 queue.size()

Print: 5 /n
12 6 /n
9 -1 10 /n
4 15 9 /n
19

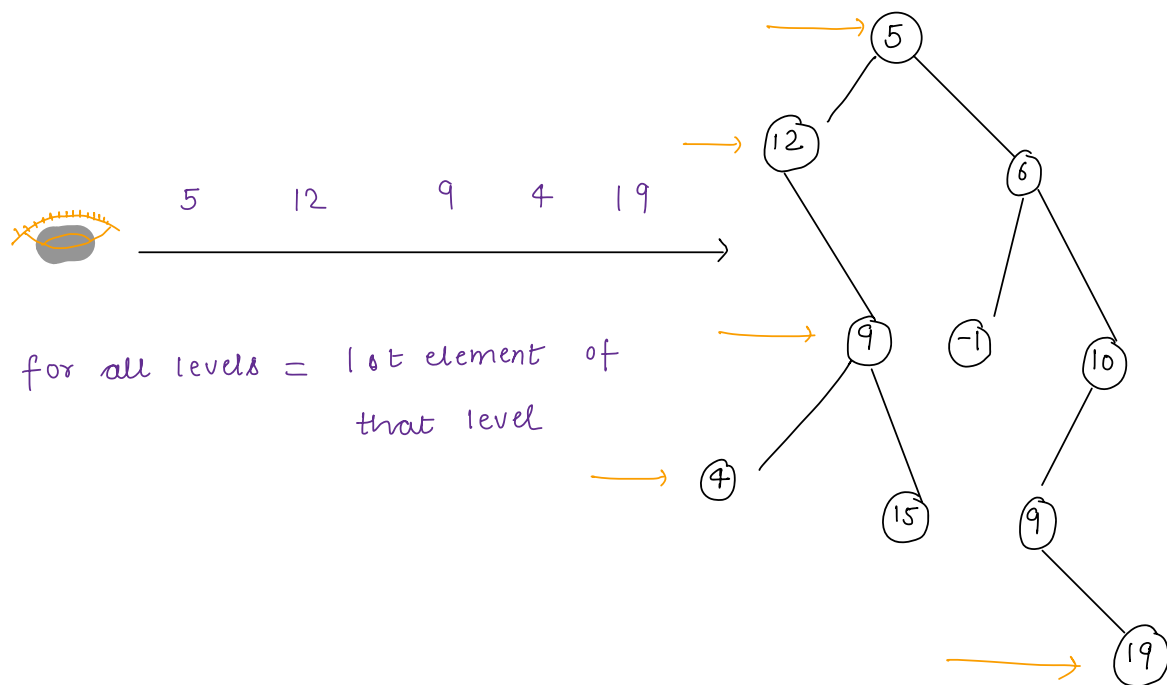
Code:

```
void levelorder(Node root) {  
    Queue< Node > q = new LinkedList<>();  
  
    q.add(root);  
  
    while(! q.isEmpty()) {  
        currLevel = q.size();  
        for(i=1; i<=currLevel i; i++) {  
            Node curr = q.poll();  
  
            print(curr.val);  
  
            if(curr.left != null) {  
                q.add(curr.left);  
            }  
  
            if(curr.right != null) {  
                q.add(curr.right);  
            }  
        }  
        system.out.println(); ← Java  
        print("\n"); → may be some other language  
    }  
}
```

TC: $O(n)$

SC: $O(n)$

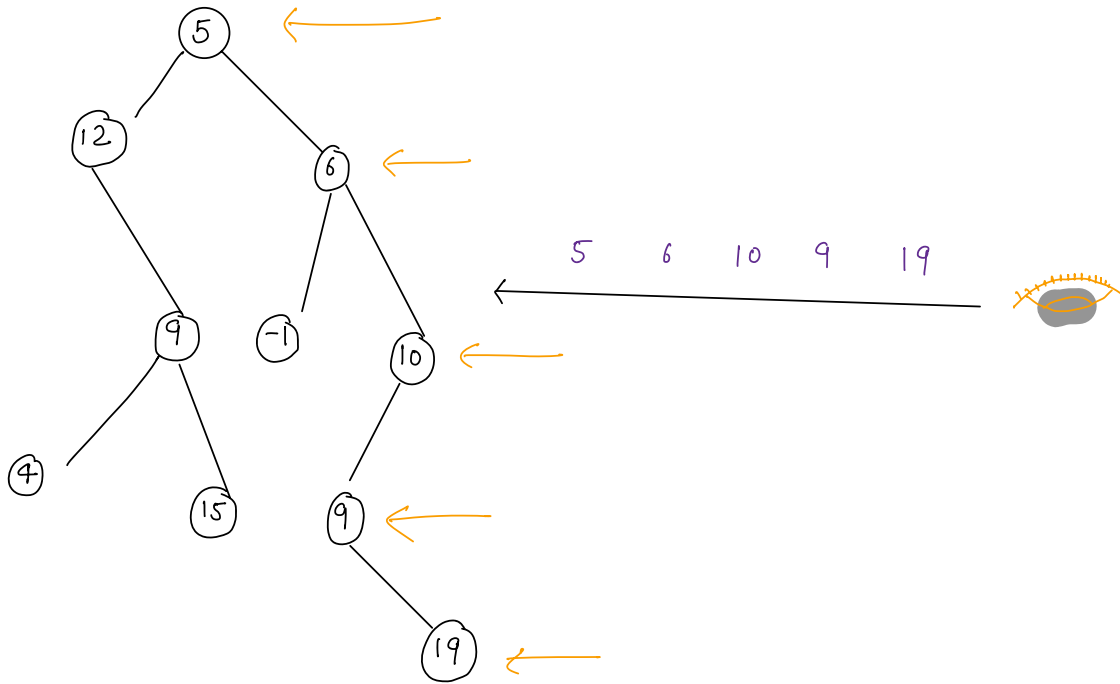
Ques Left view of BT.



Code:

```
void leftview (Node root) {  
    Queue < Node > q = new LinkedList<>();  
    q.add(root);  
    while (! q.isEmpty()) {  
        currLevel = q.size();  
        for (i=1; i<=currLevel i; i++) {  
            Node curr = q.poll();  
            if (i==1) {  
                print (curr.val);  
            }  
            if (curr.left != null) {  
                q.add (curr.left);  
            }  
            if (curr.right != null) {  
                q.add (curr.right);  
            }  
        }  
        System.out.println(); ← Java  
        print ("|n"); → may be some other language  
    }  
}
```

Qu4: Right view of B.T.

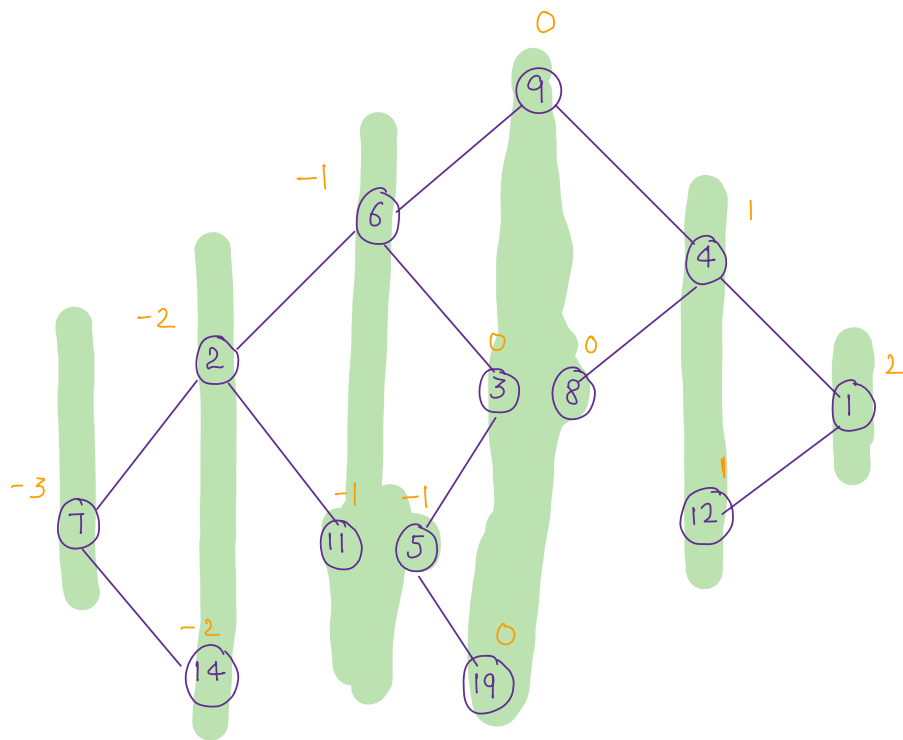


curr level = Last el of that level.

Code:-

```
void rightview (Node root) {  
    Queue < Node > q = new LinkedList<>();  
  
    q.add(root);  
  
    while (! q.isEmpty()) {  
        currLevel = q.size();  
        for (i=1; i<=currLevel i; i++) {  
            Node curr = q.poll();  
            if (i==currLevel 1) {  
                print (curr.val);  
            }  
            if (curr.left != null) {  
                q.add(curr.left);  
            }  
            if (curr.right != null) {  
                q.add(curr.right);  
            }  
        }  
        System.out.println(); ← Java  
        print ("|n"); → may be some other language  
    }  
}
```

Qu Vertical level traversal



```

7
2  14
6  11  5
9  3  8  19
4  12
1

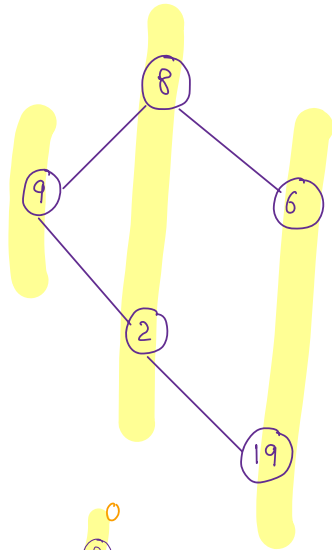
```

```

0 : 9 , 3 , 8 , 19
-1 : 6 , 11 , 5
1 : 4 , 12
-2 : 2 , 14
2 : 1
-3 : 7

```

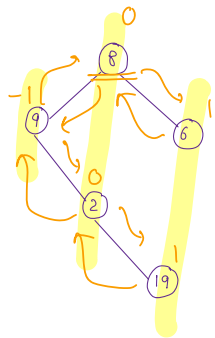
Example:



9
8 2
6 19

Pre-order:

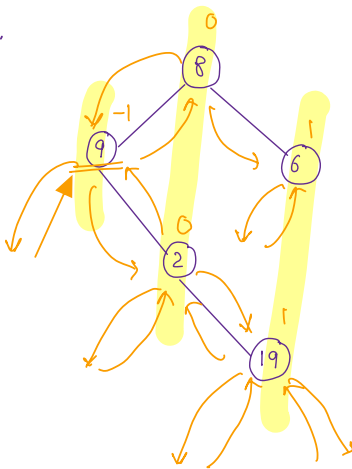
D L R



0 : 8, 2
-1 : 9
1 : 19, 6

X

In-order:

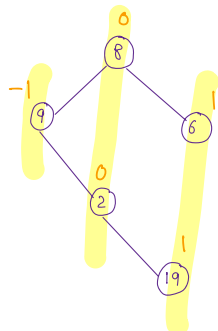


-1 : 9
0 : 2, 8
1 : 19, 6

X

Postorder: Try out [Also wrong]

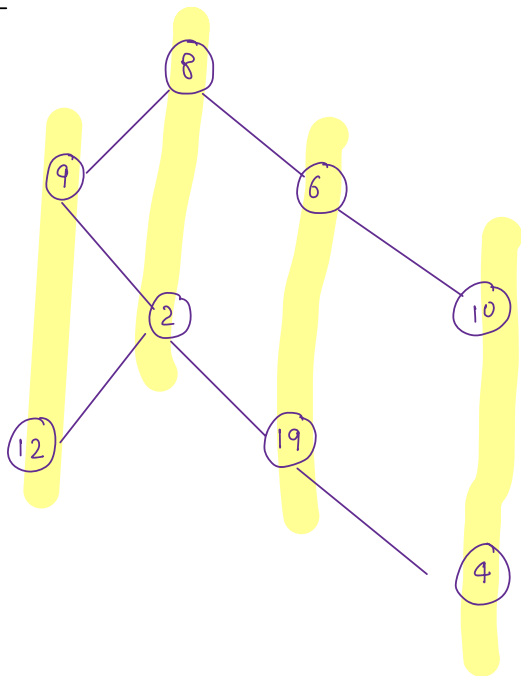
Level order:



0 : 8, 2
-1 : 9,
1 : 6, 19

✓

Logic



9 12

8 2

6 19

10 4

Map:

0 : 8, 2

-1 : 9, 12

1 : 6, 19

2 : 10, 4

Queue: | (~~8, 0~~) (~~9, -1~~) (~~6, 1~~) (~~2, 0~~) (~~10, 2~~) (~~12, -1~~) (~~19, 1~~)
 | (~~4, 2~~)

minLevel = \emptyset -1

maxLevel = \emptyset 2

class Pair {

Node node;

int lvl;

Pair (x, y) {

node = x;

lvl = y;

}

}

Code:

```
void verticalorder(Node root) {
    Queue<Pair> q;
    Map<Integer, List<Integer>> map;
    minL=0, maxL=0;
    q.add(root, 0);
    while(!q.isEmpty()) {
        Pair f = q.poll();
        Node curr = f.node;
        int lvl = f.lvl;
        minL = min(lvl, minL);
        maxL = max(lvl, maxL);
        addToMap(map, curr.data, lvl);
        if (curr.left != null) {
            q.add(new Pair(curr.left, lvl-1));
        }
        if (curr.right != null) {
            q.add(new Pair(curr.right, lvl+1));
        }
    }
}
```

```
for (i = minL; i <= maxL; i++) {
    List<Integer> list = map.get(i);
    for (int el : list) {
        cout << el;
    }
    cout << "\n";
}
```

TC: $O(n)$

SC: $O(n)$

Break: 8:53

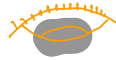
Map:

0	:	8, 2
-1	:	9, 12
1	:	6, 19
2	:	10, 4

// minL = -1
// maxL = 2

9	12
8	2
6	19
10	4

Qu Top order of B.T.

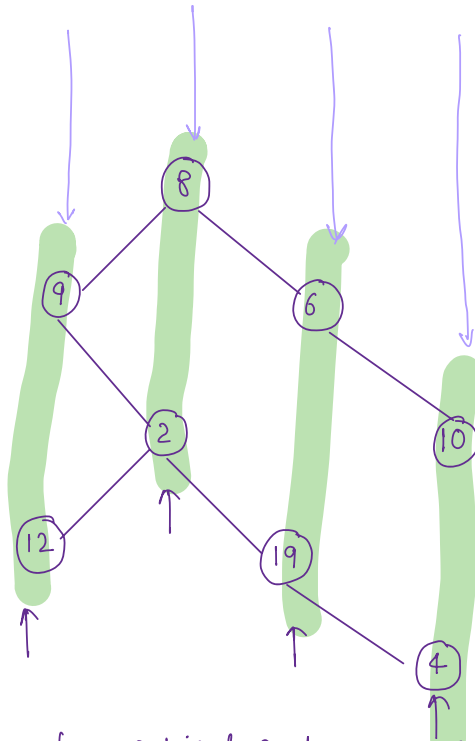


Op

9
8
6
10

Map:

0	:	8, 2
-1	:	9, 12
1	:	6, 19
2	:	10, 4



BV = 12 2 19 4
 print(list.get(n-1));
 ,

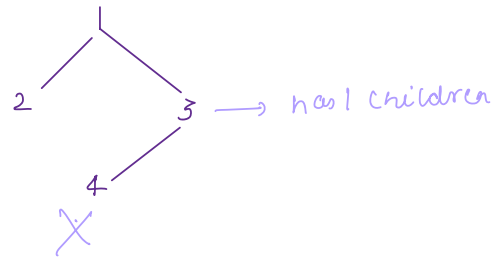
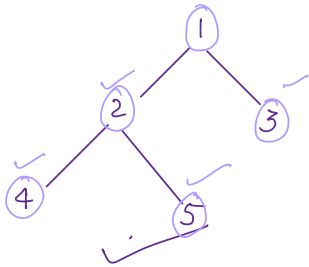
Code: Same code as of vertical order except

```
for( i=minL; i(<= maxL; i++) {
    List<Integer> list = map.get(i);
    print(list.get(0));
}
```

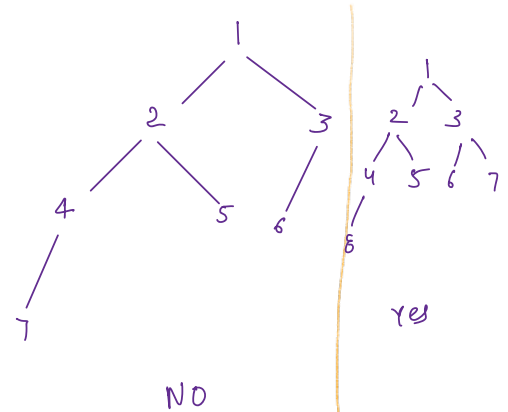
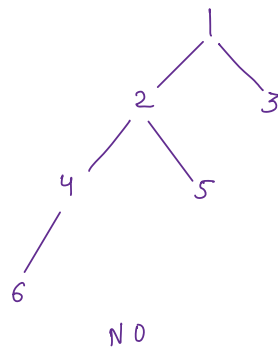
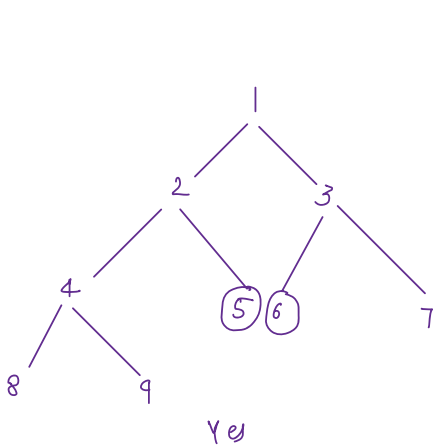
* Bottom view:- TODO

Types of BT [optional]

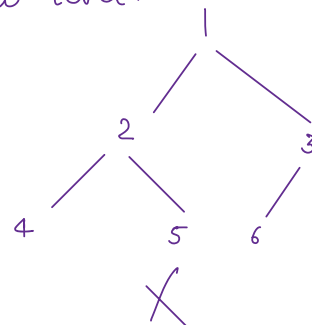
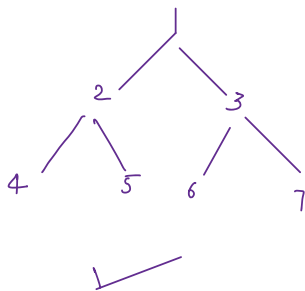
1> Proper BT. : Every node should have either 0 or 2 children



2> Complete BT. : Nodes are arranged from left to right & top to bottom



3> Perfect BT. (h/w) : All nodes are completely filled except for last level, 2 children

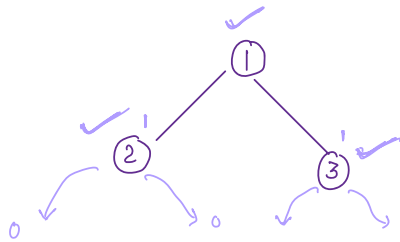


Perfect = X

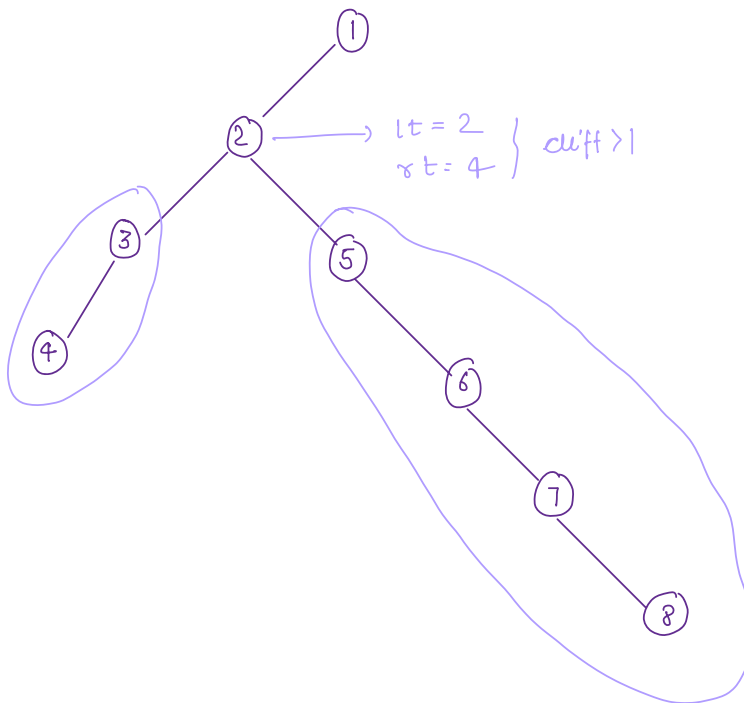
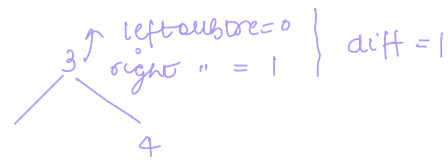
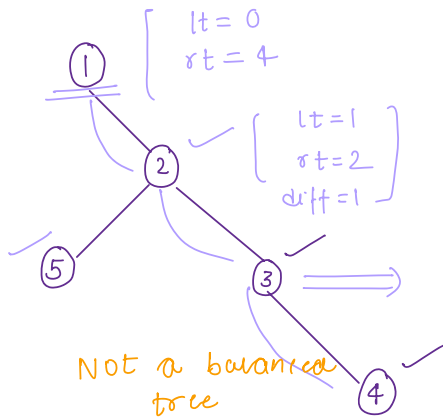
complete = ✓

Proper : X

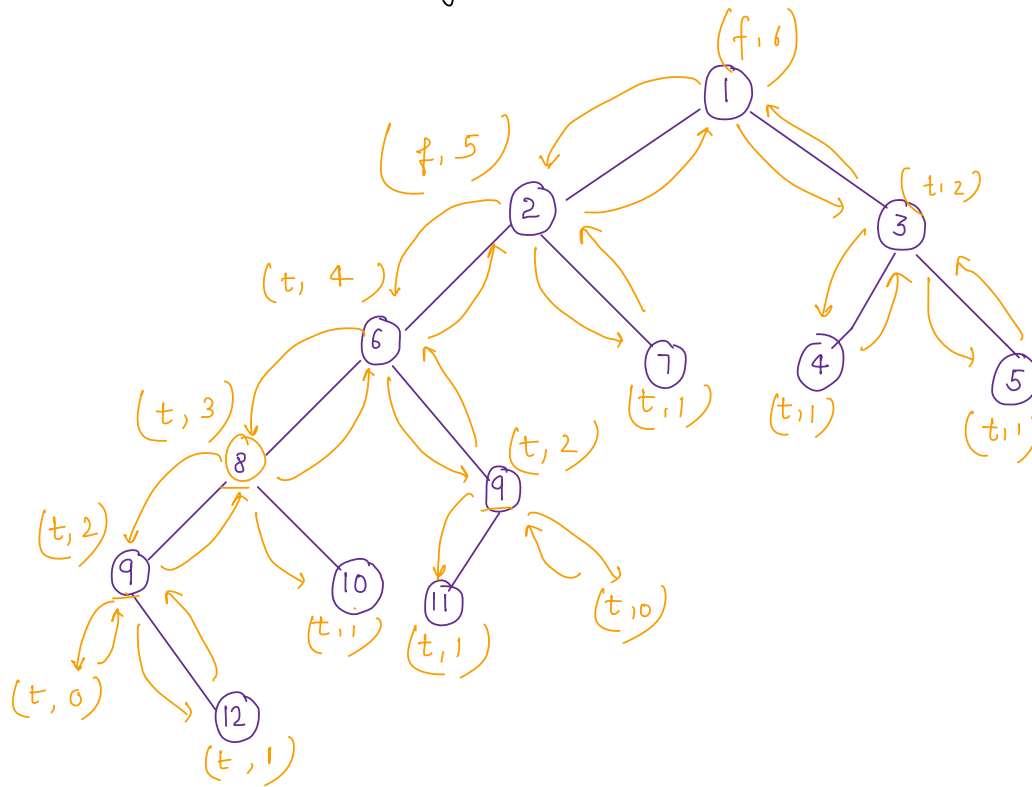
Balanced B.T. : A tree in which height b/w left and right subtree for every node is ≤ 1 .



→ Balanced B.T.



Qn: Check if tree is height balanced?



```

class Pair {
    boolean isBalanced;
    int height;

    Pair(x, y) {
        isBalanced = x;
        height = y;
    }
}

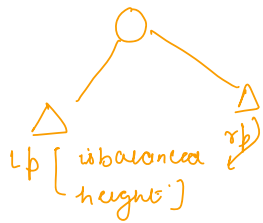
boolean isBalanced(Node root) {
    Pair p = helper(root);
    return p.isBalanced;
}

```

```

Pair helper( Node root) {
    if( root == null) {
        return new Pair (t, 0);
    }
    if( root.left == null && root.right == null) {
        return new Pair (t, 1);
    }
    Pair lp = helper( root.left);
    Pair rp = helper( root.right);
    int height = max( lp.height, rp.height) + 1;
    if( lp.isBalanced == false ||
        rp.isBalanced == false) {
        return new Pair (false, height );
    }
    if( Math.abs( lp.height - rp.height) > 1) {
        return new Pair (false, height );
    }
    return new Pair ( true, height );
}

```



TC: $O(n)$

SC: $O(\text{height})$

Thankyou 😊