

Agenda

- Max consecutive 1's caused by
 - Atmost 1 swap
 - Atmost 1 replace
- Count triplets
- Josephus problem
- Comparator

Qul Given binary arr[n], we can atmost replace a
contains 0 and 1

single 0 with 1. find max consecutive 1's in array.

Ex: $arr[] = [1, 1, 0, 1, 1, 0, 1, 1]$ [Amazon
Adobe
Walmart]

case1: $[1, 1, 0, 1, 1, 0, 1, 1]$

case2: $[1, 1, 0, 1, 1, 0, 1, 1]$ ans = 5

Ex: $arr[] = [0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0]$

case1: $[0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0]$ 4

case2: $[0, 1, 1, 1, 0, 1, 1, 0, 1, 1, 0]$ 6

Ex: $arr[] = [1, 1, 1, 1, 1]$ ans = 5

Ex: $arr[] = [1, 1, 1, 0, 1, 1, 0, 1, 1, 1, 1, 0, 0, 1, 1, 0]$

↓
consecutive 1's on left [3]

+

consecutive 1's on right [2]

+

1 [1]

[6]

Observation

consecutive 1s on left — $\text{prefix}[]$

consecutive 1s on right — $\text{suffix}[]$

$\text{arr}[] = [\overset{0}{1} \ \overset{1}{1} \ \overset{2}{1} \ \overset{3}{0} \ \overset{4}{1} \ \overset{5}{1} \ \overset{6}{0} \ \overset{7}{1} \ \overset{8}{1} \ \overset{9}{1} \ \overset{10}{1} \ \overset{11}{0} \ \overset{12}{0} \ \overset{13}{1} \ \overset{14}{1} \ \overset{15}{0}]$

$\text{pfx}[] = [1 \ 2 \ 3 \ 0 \ 1 \ 2 \ 0 \ 1 \ 2 \ 3 \ 4 \ 0 \ 0 \ 1 \ 2 \ 0]$

$\text{sfx}[] = [3 \ 2 \ 1 \ 0 \ 2 \ 1 \ 0 \ 4 \ 3 \ 2 \ 1 \ 0 \ 0 \ 2 \ 1 \ 0]$

$\text{pfx}[0] = \text{consecutive 1's from 0th idx to 0th idx.}$

$\text{pfx}[1] = \text{consecutive 1's } [0, 1] \text{ idx}$

$= \text{pfx}[0] + \text{if arr}[1] == 1 \ [1]$

$\text{pfx}[3] = \text{consecutive 1's from } [0, 3] \text{ idx}$

$\text{sfx}[i] = \text{consecutive 1's from } i\text{th idx to } n-1 \text{ idx}$

$\text{pfx}[i] = \text{" " " 0th " " } i\text{th idx}$

} This statement
?

arr[] = [0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15]
 [1 1 1 0 1 1 0 1 1 1 1 0 0 1 1 0]

pf[] = [1 2 3 0 1 2 0 1 2 3 4 0 0 1 2 0]

sf[] = [3 2 1 0 2 1 0 4 3 2 1 0 0 2 1 0]

↓
 pf[2] + 1 + sf[4]

pf[i-1] + 1 + sf[i+1]

Edge case:

1) 0th idx = pf[0-1] + 1 + sf[0+1]
 ↓
 0 + 1 + sf[1]

2) n-1 idx = pf[n-1-1] + 1 + sf[n-1+1]
 pf[n-2] + 1 + 0

int maxConsecutive1s(int[] arr) {

int[] pf = consecutivePrefixes(arr);

int[] sf = consecutiveSuffixes(arr);

h/w.

int ans = -1;

// edge cases.

1. 0th idx

if (arr[0] == 0) {

ones = 1 + sf[1];

ans = Math.max(ans, ones);

}

2. $n-1$ idx.

```
if (arr[n-1] == 0) {  
    ones = pf[n-2] + 1;  
    ans = Math.max(ans, ones);  
}
```

```
for (i=1; i < n-1; i++) {  
    if (arr[i] == 0) {  
        ones = pf[i-1] + 1 + sf[i+1];  
        ans = Math.max(ans, ones);  
    }  
}
```

```
if (ans == -1) {  
    return arr.length;  
}
```

I have an array with
all 1's.

```
return ans;
```

```
}
```

TC : $O(n)$

SC : $O(n)$

Assignment:- SC : $O(1)$?? [Is it possible]

└ carry forward

nu2 follow up.

Given binary arr[], find max consecutive 1's. We can do atmost one swap.

$$\text{var}() = [1 \ 1 \ 0 \ 1 \ 1 \ 1 \ 0 \ 1] \quad \text{ans} = 6$$

case 1:

The diagram shows an array of 8 elements: [1, 1, 0, 1, 1, 1, 0, 1]. The first three elements (1, 1, 0) are highlighted in a yellow box. An arrow labeled 'swap' points from the 3rd element (0) to the 8th element (1). The 8th element is also crossed out with a red line, and a '0' is written below it, indicating a swap with the 3rd element.

case2:

[1 1 0 1 1 1 0 1]

swap

[illegible]

varr[] = [0 1 1 1 0 1 1 0 0] \Rightarrow swapping with leftmost 1

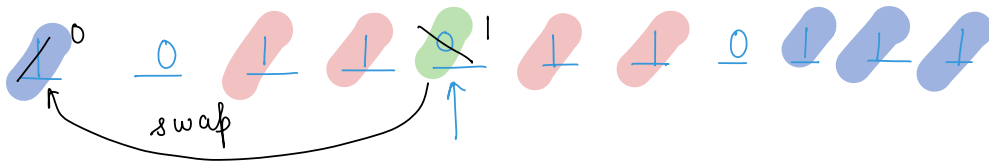
case 1:

[0 1 0 1 1 0 1 1 0 0] right most consecutive 1.

swap

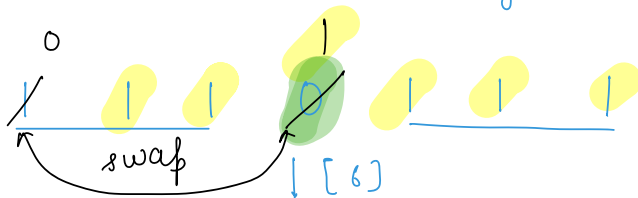
0 1 0 1 1 0 1 1 0 0

swap



$$pf[i-1] + 1 + ofx[i+1]$$

if I have extra's which are not part of left & right consecutive 1's



$$pf[i-1] + \cancel{1} + ofx[i+1]$$

if I have no extra's. $\left[pf[i-1] + ofx[i+1] \right]$

$$arr[] = [1, 0, 0, 1, 1, 1, 0]$$

$$pfx[i-1] + ofx[i+1] + 1 \text{ (if extra's)}$$

$$0 \text{ (if no extra's)}$$

swapping \rightarrow for any 0 -

$$pfx[i-1] + ofx[i+1] + \text{if extra's } [1]$$

$$\text{else } [0]$$

```

int maxConsecutive1s (int[] arr) {
    int onesCount = 0;
    for (int el: arr) {
        if (el == 1) {
            onesCount++;
        }
    }
    int[] pfx = consecutivePrefixones(arr);
    int[] sfx = consecutiveSuffixones(arr);
    int ans = -1;

    // Edge cases.
    1. 0th idx
    if (arr[0] == 0) {
        int consecutives = sfx[1];
        if (onesCount > consecutives) {
            ones = 1 + sfx[1];
            ans = Math.max(ans, ones);
        } else {
            ones = sfx[1];
            ans = Math.max(ans, ones);
        }
    }
    ...
}

```

h/w.

→ differentiating
1st & 2nd problem

Try it out??

Q2

Goldman Sachs

Given $arr[n]$, calculate no of triplets i, j & k such that

$i < j < k$ and $arr[i] < arr[j] < arr[k]$

$arr[5] = \begin{pmatrix} 0 & 1 & 2 & 3 & 4 \\ 2 & 6 & 9 & 4 & 10 \end{pmatrix}$

i	j	k
0	1	2

$2 < 6 < 9$

0	1	3
---	---	---

0	1	4
---	---	---

$2 < 6 < 10$

0	2	3
---	---	---

0	2	4
---	---	---

0	3	4
---	---	---

$2 < 4 < 10$

1	2	3
---	---	---

1	2	4
---	---	---

2	3	4
---	---	---

1	3	4
---	---	---

Expected TC: $O(n^2)$

arr[] = [4, 1, 2, 6, 9, 7]

$j = 3$

$i \quad j \quad k$
 $arr[i] < arr[j] < arr[k]$
 0 3 4
 4 < 6 < 9

0 3 5

1 3 4

1 3 5

2 3 4

2 3 5

$j^{th} \text{ idx} = 3$

No of el less than arr[3] on left *

No of el greater than arr[3] on right

$$3 * 2 = 6$$

Algo: fix $j^{th} \text{ idx}$ [1, n-2 idx]
 middle idx

left - find no of el less than arr[j] in left [0, j-1]

right - find " " " greater " " " right [j+1, n-1]

- cnt = left * right

- ans = ans + cnt;

```
int countTriplets(int[] arr) {
```

```
    int ans = 0;
```

```
    // fix jth idx
```

```
    o(n) — for (j = 1; j <= n-2; j++) {
```

```
        // el lesser on left side
```

```
        int left = 0;
```

```
        for (i = 0; i < j; i++) {
```

```
            if (arr[i] < arr[j]) {
```

```
                left++;
```

```
            }
```

```
        }
```

```
        // el greater on right side
```

```
        int right = 0;
```

```
        for (int k = j+1; k < n; k++) {
```

```
            if (arr[k] > arr[j]) {
```

```
                right++;
```

```
            }
```

```
        }
```

```
        ans = ans + (left * right);
```

```
    }
```

```
    return ans;
```

```
}
```

TC: $O(n^2)$

can prefix

solve this??

$O(n)$

$O(n)$

Q4:

Squad Game (Josephus problem)

N people standing in a circle, clockwise

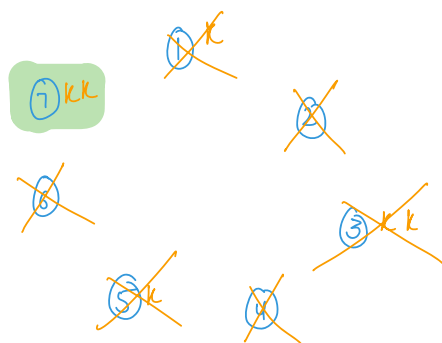
Person 1 has the knife

He kills the next person in clockwise manner
and passes the knife to next alive person

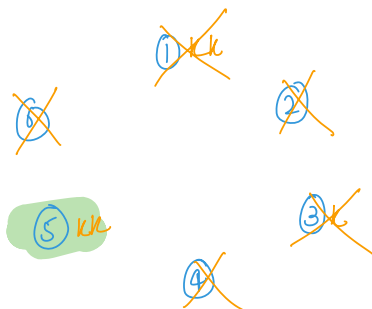
Repeat until one person is alive

find the last man standing

$n=7$



$n=6$



$n=1$

① k

$n=2$

① k

~~②~~

$n=4$

① k k

~~④~~

~~③~~

~~③~~ k

$n=8$

① k k k

~~⑧~~

~~⑦~~

~~⑦~~ k

~~⑤~~ k

~~⑥~~

~~⑤~~ k k

~~④~~

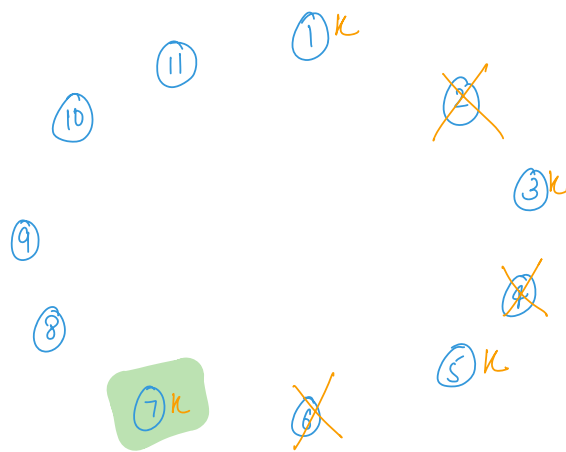
$n=16$

① k k k k
② k k k k
③ k k k k
④ k k k k
⑤ k k k k
⑥ k k k k
⑦ k k k k
⑧ k k k k
⑨ k k k k
⑩ k k k k
⑪ k k k k
⑫ k k k k
⑬ k k k k
⑭ k k k k
⑮ k k k k

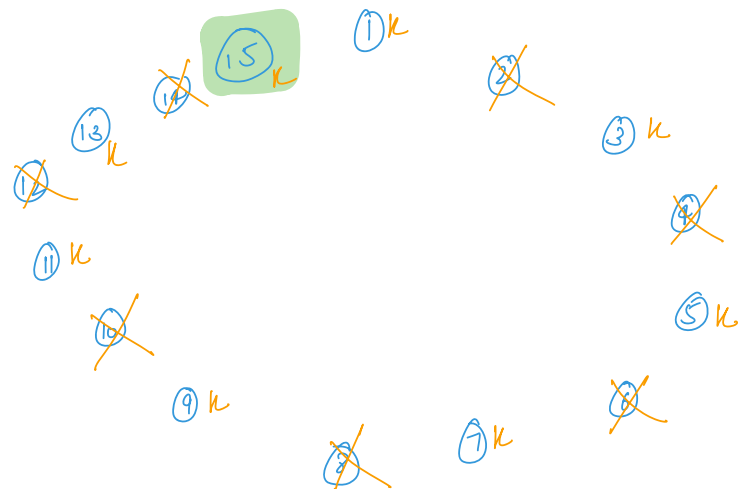
If n is power of 2, whoever has the knife is winner.

[We are killing next person] — a^n .

$n=11 \xrightarrow{3 \text{ kill}} 8$



$n=15 \xrightarrow{7 \text{ kill}} \underline{\underline{8}}$



code it out ??

Doubt 8

