

2nd

Naive Bayes \Rightarrow classification algorithm
 \hookrightarrow probability-based

KNN \rightarrow neighborhood based classification.

Conditional Probability $= (P(A/B)) = P_c(A=a/B=b)$
 \downarrow \downarrow
value that A takes value that B takes.

Always read equations in english.

$$P(A/B) = \frac{P(A \cap B)}{P(B)}$$

* Independent Events & Mutually Exclusive events

A, B are said to be independent.

$$P(A/B) = P(A)$$

$$P(B/A) = P(B)$$

for ex \Rightarrow

A: getting value of 6 in die 1
throw ($D_1=6$)

B: getting a value of 3 in
die 2's throw ($D_2=3$)

A, B are said to be mutually exclusive if.

$$P(A/B) = P(B/A) = 0$$

$$\frac{P(A \cap B)}{P(B)}$$

$$\frac{P(B \cap A)}{P(A)}$$

\therefore so, $P(A \cap B)$ should be 0

$$\text{as } A \cap B = B \cap A$$

for ex \Rightarrow probability of getting 3 in die 1 is 0 if die 2
is getting 6 in it.

Bayes Theorem \rightarrow (1700s)

$$P(A/B) = \frac{P(B/A) \cdot P(A)}{P(B)} \quad \text{if } P(B) \neq 0.$$

$P(A/B)$ is labeled **posterior probability**
 $P(B/A)$ is labeled **likelihood**
 $P(A)$ is labeled **prior**
 $P(B)$ is labeled **evidence**

Proof of Bayes Theorem \rightarrow

$$P(A/B) = \frac{P(A \cap B)}{P(B)} = \frac{P(A, B)}{P(B)} \quad \text{also means } \cap$$

In set theory $A \cap B = B \cap A \leftarrow$

$$P(A/B) = \frac{P(B \cap A)}{P(B)} = \frac{P(B, A)}{P(B)} \quad \text{--- (1)}$$

$$P(B/A) = \frac{P(B \cap A)}{P(A)}$$

$$P(B \cap A) = P(B/A) \cdot P(A) \quad \text{--- (2)}$$

Put $P(B \cap A)$ in (1) eq

$$P(A/B) = \frac{P(B/A) \cdot P(A)}{P(B)}$$

* Naive Bayes Algorithm

↓
unobtrusive
↓
Simplistic

$$P(C/f_1, f_2, f_3, f_4) = P(f_1/C) * P(f_2/C) * P(f_3/C) * P(f_4/C) * P(C)$$

Naive Bayes is much better in terms of space complexity at runtime

$O(d \times c) \rightarrow$ naive Bayes

$O(n \times d) \rightarrow$ KNN

memory efficient at run-time

* Naive Bayes on text data \rightarrow

first technique used in case of spam filters \rightarrow email \rightarrow spam
↓
not spam

review \rightarrow +ve
↓
 \rightarrow -ve

Text classification \rightarrow Naive Bayes is a simple used method.

← text1 →	0
← text2 →	1
	0
	1

Task

① $P(y_v = 1 / \text{text}_q) \rightarrow$ compute these

② $P(y_q = 0 / \text{text}_q)$

So if ① > ②

then we can say that $y_q = 1$ for given text_q .

preprocessing \rightarrow

text \rightarrow

stopwords

stemming

n-grams

$\rightarrow \{w_1, w_2, w_3, \dots, w_d\}$

\downarrow

Binary Bow

text $\xrightarrow{\text{pre-pro}}$ $\{w_1, w_2, \dots, w_d\}$
set of words.

$$P(y_1 = 1 / \text{text}) = P(y_1 = 1 / \underbrace{w_1, w_2, w_3, \dots, w_d}_{\text{features}})$$

class
prior

likelihoods

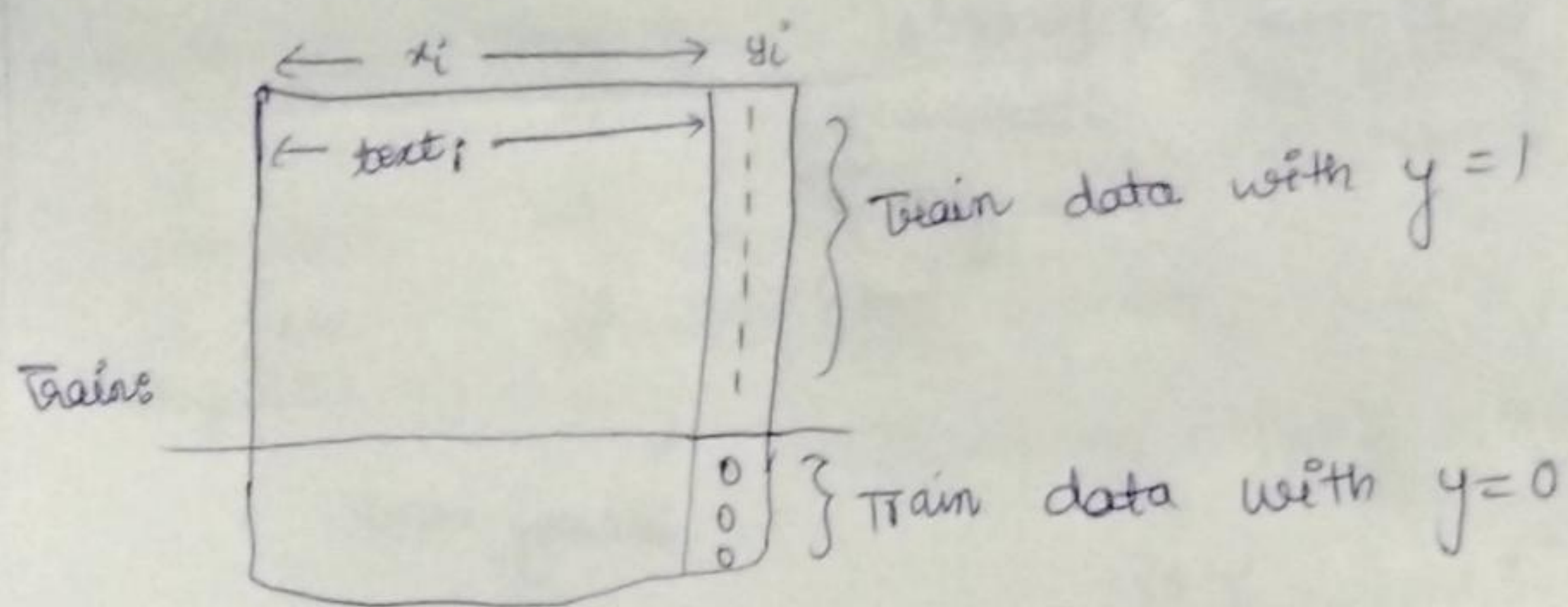
$$= P(y=1) * P(w_1 / y=1) * P(w_2 / y=1) \dots P(w_d / y=1)$$

$$P(y=1 / \text{text}) \propto P(y=1) * \prod_{i=1}^d P(w_i / y=1)$$

$$P(y=0 / \text{text}) \propto P(y=0) * \prod_{i=1}^d P(w_i / y=0)$$

$$P(y=1) = \frac{\text{no. of train points with } y=1}{\text{Total no. of train points.}}$$

$$P(y=0) = \frac{\text{no. of train points with } y=0}{\text{Total no. of train points.}}$$



$$P(w_i | y=1) = \frac{\text{no. of } \overset{\text{Train}}{\text{data points which contain } w_i \&\&}}{\text{no. of } \overset{\text{Train}}{\text{data points with } y=1}}$$

Text - classification problems.

{ spam - detection
 Reliability of a review } Naive Bayes is a very good Baseline

benchmark

* Laplace - Additive Smoothing \rightarrow ~~not Laplace smoothing~~

After training \rightarrow { $P(y=1); P(y=0) \leftarrow$ class priors }
 all this data is already computed. { $P(w_1/y=1) \quad P(w_1/y=0)$
 $P(w_2/y=1) \quad P(w_2/y=0)$
 \vdots
 $P(w_m/y=1) \quad P(w_m/y=0)$ } \rightarrow likelihoods

Test: $\rightarrow \text{test}_q = (w_1, w_2, w_3, w')$

\nwarrow w' is not present in $\{w_1, w_2, w_3, \dots, w_m\}$ \nearrow training data.
very often

$$P(1/\text{test}_q) = P(y=1/w_1, w_2, w_3, w')$$

$$= P(y=1) * P(w_1/y=1) * P(w_2/y=1) * P(w_3/y=1)$$

$$* P(w'/y=1)$$

ignoring or dropping it will mean

$P(w'/y=1) = 1$
which is not correct.

how do you get ^{this} probability as w' is not present in training data.

we have to get values of $P(w'/y=1)$ and $P(w'/y=0)$

$$P(w'/y=1) = \frac{P(w', y=1)}{P(y=1)}$$

$$= \frac{\text{no. of train points such that } w' \text{ occurs in } y=1}{\text{no. of train points where } y=1}$$

$$= \frac{0}{n_1} = 0 \rightarrow \text{This is also dangerous as it will make whole probability to be 0.}$$

Laplace smoothing or additive smoothing

$$P(f_i = a / y = 1) = \frac{0 + \alpha}{n_i + \alpha k}$$

$\alpha = 1$ typically (not always)

k = no. of distinct values which f_i can take

$f_i \Rightarrow$ feature

$$P(w' / y = 1) = \frac{0 + \alpha}{100 + 2\alpha}$$

\uparrow
 $k = 2 \rightarrow$ because w' is 0 or 1,
present or not.

Let $n_i = 100$

Case 1: $\rightarrow \alpha = 1 \Rightarrow \frac{1}{102} \neq 0$

α small,
we are getting
rid of multiplying
all the
probabilities
with 0.

$$P(w' / y = 1) \neq 0 \quad \Downarrow \text{which implies}$$

$$P(y = 1 | \text{text}_q) \neq 0.$$

So it's not 0 anymore

Case 2: $\rightarrow \alpha = 10000 \rightarrow$ when α is large

$$P(w' / y = 1) = \frac{0 + 10k}{100 + 2 \times 10k} = \frac{10k}{20100} \approx \frac{1}{2}$$

$$P(w' / y = 1) = P(w' / y = 0) = \frac{1}{2}$$

means equal probability of w' to be 0 or 1
because w' have only two possibilities (0 or 1)

Laplace smoothing \Rightarrow find this for all words

$$P(w_i | y=1) = \frac{(\text{no. of data points with } w_i \text{ \& } y=1) + \alpha}{(\text{no. of data points with } y=1) + \alpha k}$$

present in
my training
data

adding something
to numerator &
denominator,
that's why it is
called additive
smoothing

In this formula, as $\alpha \uparrow$,

$P(w_i | y=1) \rightarrow$ likelihood probability
is moving to a uniform distribution.

if n_i is small

num or den is small \rightarrow less confidence in ratio

often times, $\alpha = 1 \rightarrow$ add one smoothing

It is called smoothing because you are moving likelihood probability towards uniform distribution