

Stack & Queue

①

Stack: → A stack is a list of elements in which an element may be inserted or deleted only at one end, called the top of the stack.

This means, in particular, that elements are removed from a stack in the reverse order of that in which they were inserted into the stack. Accordingly, stacks are also called Last-in-First-out (LIFO) lists.

Special terminology is used for 2 basic operations associated with stacks.

a) "Push" is the term used to insert an element into a stack.

b) "Pop" is the term used to delete an element from a stack.

Algorithm →

PUSH (STACK, TOP, MAXSTK, ITEM)

S1 → IF $TOP \geq MAXSTK - 1$, then

Print "Overflow" Δ return

S2 → Set $TOP = TOP + 1$

S3 → Set $STACK[TOP] = ITEM$

S4 → Return

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POP (STACK, TOP, ITEM)

S1: \rightarrow If $TOP = -1$, then

Print "Underflow" & Return

S2: \rightarrow Set $ITEM = STACK[TOP]$

S3: \rightarrow Set $TOP = TOP - 1$

S4: \rightarrow Return

Polish Notation \rightarrow The process of writing the operators of an expression either before their operands or after them is called the Polish Notation. The Polish notations are classified into 3 categories.
i) Infix, ii) Prefix iii) Postfix.

i) Infix \rightarrow When the operators exists b/w 2 operands then the expression is called infix expression.

Ex - $(a+b)*c$, $a+(b*c)$.

ii) Prefix \rightarrow When the operators are written before their operands then the resulting expression is called the prefix expression.

Ex: $\rightarrow (A+B)*C = [+AB]*C = *+ABC$

$A+(B*C) = A+[*BC] = +A*BC$

$(A+B)/(C-D) = (+AB)/(-CD) = /+AB-CD$

ii) Postfix \rightarrow When the operators come after their operands the resulting expression is called the reverse Polish notation or Postfix expression.

Ex $A + (B * C) = A + (BC*) = ABC*+$

Evaluation of a Postfix Expression \rightarrow

Suppose P is an arithmetic expression written in postfix notation.

Algorithm \rightarrow

S1 \rightarrow Add ')' at the end of P.

S2 \rightarrow Scan P from left to right & repeat S3 & S4 for each element of P until ')' is encountered.

S3 \rightarrow If an operand is encountered, push it on stack.

S4 \rightarrow If an operator \otimes is encountered, then
(a) Remove the 2 top element of stack, where A is top & B is next top element
(b) Evaluate $B \otimes A$
(c) Push the result of (b) back on stack

end of if
end of loop
S5 Exit.

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Ex → Consider the following arithmetic exp P written in postfix notation:

P: 5, 6, 2, +, *, 12, 4, /, -

Symbol	STACK
1) 5	5
2) 6	5, 6
3) 2	5, 6, 2
4) +	5, 8
5) *	40
6) 12	40, 12
7) 4	40, 12, 4
8) /	40, 3
9) -	37
10))	

Ex → Consider the following arithmetic exp P written in postfix notation:

P: 12, 7, 3, -, /, 2, 1, 5, +, *, +

Evaluate P using algo.

P: 12, 7, 3, -, /, 2, 1, 5, +, *, +

Symbol	STACK
1) 12	12
2) 7	12, 7
3) 3	12, 7, 3
4) -	12, 4
5) /	3
6) 2	3, 2
7) 1	3, 2, 1
8) 5	3, 2, 1, 5
9) +	3, 2, 6
10) *	3, 12
11) +	15
12))	

Transforming Infix Expression into Postfix Expression:

Suppose Q is an arithmetic expression written in infix notation. This algorithm finds the equivalent Postfix expression P .

S1: Push "(" onto STACK & add ")" to the end of Q .

S2: Scan Q from left to right & repeat steps 3 to step 6 for each element of Q until STACK is empty.

S3: IF an operand is encountered, add it to P .

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S4 \rightarrow If a left parenthesis is encountered, push it onto STACK.

S5 \rightarrow If an operator \odot is encountered, then

(a) Repeatedly Pop from STACK & add to P each operator which has the same precedence as or higher precedence than \odot

(b) Add \odot to STACK.

end of if

S6 \rightarrow If a "]" is encountered, then

(a) Repeatedly Pop from STACK & add to P each operator until a left parenthesis is encountered.

(b) Remove the "C". [Do not add 'C' to P].

end of if.

end of loop.

S7 \rightarrow Exit.

Ex \rightarrow Consider the following arithmetic expression Q:

Q: $A + (B * C - (D / E + F) * G) * H$

Using the algorithm transform Q into its equivalent postfix expression P.

soln:→	Symbol	STACK	Expression P
1)	A	C	A
2)	+	C+	A
3)	C	C+C	A
4)	B	C+C	AB
5)	*	C+C*	AB
6)	C	C+C*	AB C
7)	-	C+C-	ABC*
8)	C	C+C-C	ABC*
9)	D	C+C-C	ABC*D
10)	/	C+C-C/	ABC*D
11)	E	C+C-C/	ABC*DE
12)	↑	C+C-C/↑	ABC*DE
13)	F	C+C-C/↑	ABC*DEF
14))	C+C-	ABC*DEF↑/
15)	*	C+C-*	ABC*DEF↑/
16)	∩	C+C*	ABC*DEF↑/∩
17))	C+	ABC*DEF↑/∩*-
18)	*	C+*	ABC*DEF↑/∩*-
19)	H	C+*	ABC*DEF↑/∩*-H
20))	-	ABC*DEF↑/∩*-H*+

⑧ Ex → Consider the following infix expression $Q: (A+B)*D \uparrow (E-F)$

Soln →

Symbol	STACK	Expression P
1) (((
2) (((((
3) A	((((A	A
4) +	((((A+	A
5) B	((((A+B	AB
6))	((((A+B	AB+
7) *	((((A+B*	AB+
8) D	((((A+B*D	AB+D
9))	((((A+B*D	AB+D*
10) ↑	((((A+B*D↑	AB+D*
11) (((((A+B*D↑(AB+D*
12) E	((((A+B*D↑(E	AB+D*E
13) -	((((A+B*D↑(E-	AB+D*E
14) F	((((A+B*D↑(E-F	AB+D*EF
15))	((((A+B*D↑(E-F	AB+D*EF-
16))	((((A+B*D↑(E-F↑	AB+D*EF-↑

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Queue \rightarrow A queue is a linear list of elements in which deletions can take place only at one end called the front & insertion can take place only at other end called rear.

Queue are also called First-in-first-out (FIFO) list, since the first element in a queue will be the first element out of the queue.

Linear Queue Insertion \rightarrow

LQInsert(Queue, Element, Size)

S1 \rightarrow If front = 0 & rear = Size - 1 then
Print "Overflow" & exit.

S2 \rightarrow If front = -1 then
front = 0, rear = 0

S3 \rightarrow else
rear = rear + 1

S4 \rightarrow Queue[rear] = element

S5 Return.

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Deletion \rightarrow

QDelete(Queue, Element)

S1 \rightarrow If front = -1 then
print "Underflow" & exit

S2 \rightarrow Element = Queue[front]

S3 \rightarrow If front = rear then
front = -1 & rear = -1

S4 \rightarrow else

front = front + 1

S5 \rightarrow Return (Element).

Circular Queue \rightarrow Let we have an array Q that contains n elements in which Q[0] comes after Q[n-1] in the array. When this technique is used to construct a queue then the queue is called circular queue.

Insertion \rightarrow

QInsert(Queue, Size, Item)

S1 \rightarrow If front = 0 & rear = size - 1 or front = rear + 1
then Print "Overflow" & exit

S2 \rightarrow If front = -1 then
front = 0 & rear = 0

S3 else if rear = size - 1 then
rear = 0

S4 else

rear = rear + 1

S5 Queue[rear] = element

S6 Return.

Deletion:

CQ Delete (Queue, size, Element)

S1: \rightarrow If $\text{front} = -1$ then
print "Underflow" & exit

S2: \rightarrow $\text{Element} = \text{Queue}[\text{front}]$

S3: \rightarrow If $\text{front} = \text{rear}$ then
 $\text{front} = -1$ & $\text{rear} = -1$

S4: \rightarrow else if $\text{front} = \text{size} - 1$ then
 $\text{front} = 0$

S5: \rightarrow else
 $\text{front} = \text{front} + 1$

S6: \rightarrow Return (Element)

Deque: \rightarrow A deque is a linear list in which elements can be added or removed at either end but not in the middle. The term deque is a contraction of the name double-ended queue.

There are 2 types of deque.

- i) Input-restricted deque &
- ii) Output-restricted deque.

i) Input-restricted deque: \rightarrow An input restricted deque is a deque which allows insertions at only one end of the list but also allows deletions at both ends of the list.

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i) Output-restricted dequeue → An output-restricted dequeue is a dequeue which allows deletions at only one end of the list but allows insertions at both ends of the list.

Algorithm to insert any element in a dequeue →

Insert-front() algo: →

Ins-f(Dequeue, item, size)

S1: → If $\text{front} = 0 \ \& \ \text{rear} = \text{size} - 1$ or $\text{front} = \text{rear} + 1$ then
print "Overflow" & exit.

S2: → If $\text{front} = -1 \ \& \ \text{rear} = -1$ then
 $\text{front} = 0 \ \& \ \text{rear} = 0$

S3: → Else if $\text{front} = 0$ then
 $\text{front} = \text{size} - 1$

S4: → Else $\text{front} = \text{front} - 1$

S5: → $\text{Dequeue}[\text{front}] = \text{item}$

S6: → Return.

Insert-rear() algo: →

Ins-r(Dequeue, item, size)

S1: → If $\text{front} = 0 \ \& \ \text{rear} = \text{size} - 1$ or $\text{front} = \text{rear} + 1$ then
print "Overflow" & exit

S2: → If $\text{front} = -1 \ \& \ \text{rear} = -1$ then
 $\text{front}, \text{rear} = 0$

S3: → Else if $\text{rear} = \text{size} - 1$ then
 $\text{rear} = 0$

S4: → Else $\text{rear} = \text{rear} + 1$

S5: → $\text{Dequeue}[\text{rear}] = \text{item}$

S6: → Return.

Algorithm to delete an element from the deque: (13)

delet-front() algo:

del-F (Deque, item, size)

S1: \rightarrow If $\text{front} = -1$ & $\text{rear} = -1$ then
print "Underflow" & exit

S2: \rightarrow $\text{item} = \text{Deque}[\text{front}]$

S3: \rightarrow if $\text{front} = \text{rear}$ then
 $\text{front} = -1$ & $\text{rear} = -1$

S4: \rightarrow else if $\text{front} = \text{size} - 1$ then
 $\text{front} = 0$

S5: \rightarrow else $\text{front} = \text{front} + 1$

S6: \rightarrow Return (item)

delet-rear() algo:

del-r (Deque, item, size)

S1: \rightarrow If $\text{front} = -1$ & $\text{rear} = -1$ then
print "Underflow" & Exit.

S2: \rightarrow $\text{item} = \text{Deque}[\text{rear}]$

S3: \rightarrow if $\text{front} = \text{rear}$ then
 $\text{front} = -1$ & $\text{rear} = -1$

S4: \rightarrow else if $\text{rear} = 0$ then
 $\text{rear} = \text{size} - 1$

S5: \rightarrow else
 $\text{rear} = \text{rear} - 1$

S6: \rightarrow Return (item).

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Priority Queue \rightarrow A priority queue is a collection of elements such that each element has been assigned a priority & such that the order in which elements are deleted & processed comes from the following rules:

- ii) An element with the same priority are processed according to order in which they were added to the queue.
- i) An element of higher priority is processed before any element of lower priority.

There are 2 types of priority queue.

i) Ascending Priority Queue \rightarrow An ascending priority queue is a collection of items into which items can be inserted arbitrarily & from which only the smallest item can be removed.

A queue may be viewed as an ascending priority queue whose elements are ordered by time of insertion. The element that was inserted 1st has the lowest insertion time value & is the only item that can be retrieved.

i) Descending Priority Queue \Rightarrow An descending (15)
priority queue is a collection of items into
which item can be inserted arbitrarily &
from which only the largest item can
be removed.

A stack may be viewed as descending
priority queue whose elements are
ordered by time of insertion. The
element that was inserted last has
the greatest insertion time value & is the
only item that can be retrieved.