



Homework 3 Solutions:

1. Thermal noise, Shot noise, Flicker noise,
Explained in details at noise ppt's.

$$2. V_{\text{thermal}} = \sqrt{4KTRB} = \sqrt{4 \times 1.38 \times 10^{-23} \times 300 \times 1000 \times 1000} = 1.287 \times 10^{-7} \text{ V}$$

3. Thermal noise from Resistor

shot noise from photocurrent, Dark current noise

$$b) V_{\text{thermal}} = \sqrt{4KTR\Delta f} = \sqrt{4 \times 1.38 \times 10^{-23} \times 300 \times 10000 \times 100000} = 4.07 \mu\text{V}$$

$$I_{\text{shot}} = \sqrt{2qI\Delta f} = \sqrt{2 \times 1.6 \times 10^{-19} \times 100000} = 5.56 \times 10^{-9}$$

$$V_{\text{shot}} = I_{\text{shot}} \times R = 56.57 \mu\text{V}$$

$$V_{\text{total}} = \sqrt{V_{\text{thermal}}^2 + V_{\text{shot}}^2} = 56.71 \mu\text{V}$$

Shot noise dominates

4. since our signal is from 25 kHz to 35 kHz, but noise span from 0-100 kHz we can use a bandpass filter to pass only 25-35 kHz and reject noise elsewhere. In this case the central frequency is 30 kHz and BW is 10 kHz.

$$V_{\text{thermal}} = \sqrt{4KTR\Delta f} = \sqrt{4 \times 1.38 \times 10^{-23} \times 10000 \times 10000} = 1.28 \mu\text{V}$$

$$I_{\text{shot}} = \sqrt{2qI\Delta f} = \sqrt{2 \times 1.6 \times 10^{-19} \times 10^{-3} \times 10000} = 1.78 \times 10^{-9}$$

$$v_{\text{shot}} = I_{\text{shot}} \times R = 17.89 \mu\text{V}$$

$$v_{\text{total}} = \sqrt{v_{\text{thermal}}^2 + v_{\text{shot}}^2} = 17.93 \mu\text{V}$$

or we could simply say:

$$v_{\text{total, new}} = v_{\text{total, old}} \times \sqrt{\frac{10^{\text{K}}}{100\text{K}}} = 17.93 \mu\text{V}$$

5. Quantization noise, Thermal noise, clock noise, Power supply noise

6.

a) output voltage: $V = RI = 50 \times 10^3 \times 2 \times 10^{-6} = 0.1 \text{V}$

b) Thermal noise: $\sqrt{4kTRB} = \sqrt{4 \times 1.38 \times 10^{-23} \times 300 \times 50 \times 10^3 \times 10^6} = 2.87 \times 10^{-5} \text{V}$

Shot noise: $I_{\text{shot}} = \sqrt{2qIB} = \sqrt{2 \times 1.6 \times 10^{-19} \times 2 \times 10^{-6} \times 10^6} = 8 \times 10^{-10} \text{A}$

$$v_{\text{shot}} = 8 \times 10^{-10} \times 50 \times 10^3 = 4 \times 10^{-5} \text{V}$$

shot noise from dark current:

$$I_{\text{shot}} = \sqrt{2qIB} = \sqrt{2 \times 1.6 \times 10^{-19} \times 1 \times 10^{-9} \times 10^6} = 1.78 \times 10^{-11} \text{A}$$

$$v_{\text{shot}} = 1.78 \times 10^{-11} \times 50 \times 10^3 = 8.94 \times 10^{-7} \text{V}$$

total noise: $v_{\text{total}} = \sqrt{v_{\text{thermal}}^2 + v_{\text{shot, dark}}^2 + v_{\text{shot}}^2} = 4.93 \times 10^{-5} \text{V}$

c) SNR: $\frac{v_{\text{sig}}^2}{v_{\text{noise}}^2} = \frac{(0.1)^2}{(4.93 \times 10^{-5})^2} = \frac{1 \times 10^{-2}}{24.30 \times 10^{-10}} = 4.11 \times 10^6$