

# Causal inference is not just a statistics problem

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**Causal Inference is not a  
statistics problem**

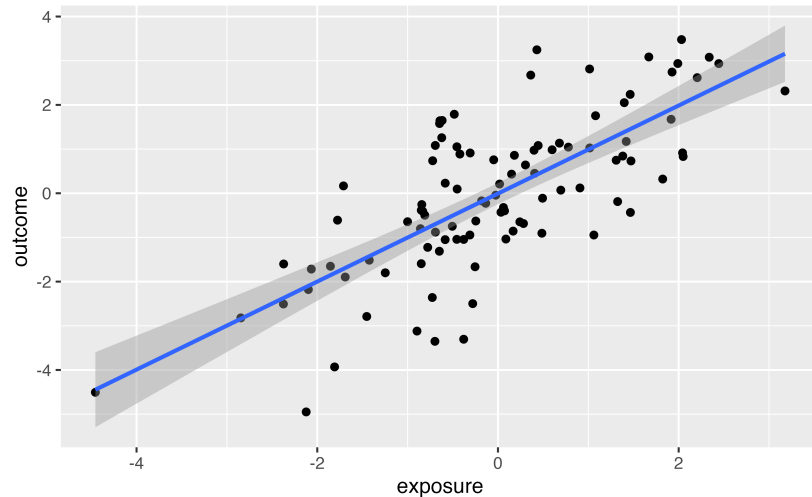
Causal Inference is not  
*just* a statistics problem

# *The problem*

We have measured variables, what should we adjust for?

exposure	outcome	covariate
0.49	1.71	2.24
0.07	0.68	0.92
0.40	-1.60	-0.10
.	.	.
.	.	.
.	.	.
0.55	-1.73	-2.34

# What does the data say?



```
1 cor(exposure, covariate)
```

```
[1] 0.7
```

The exposure and measured factor are positively correlated

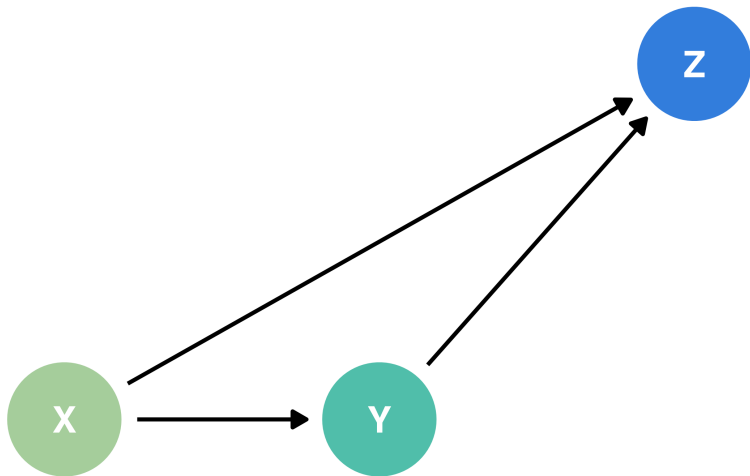
One unit increase in the exposure yields an average increase in the outcome of 1



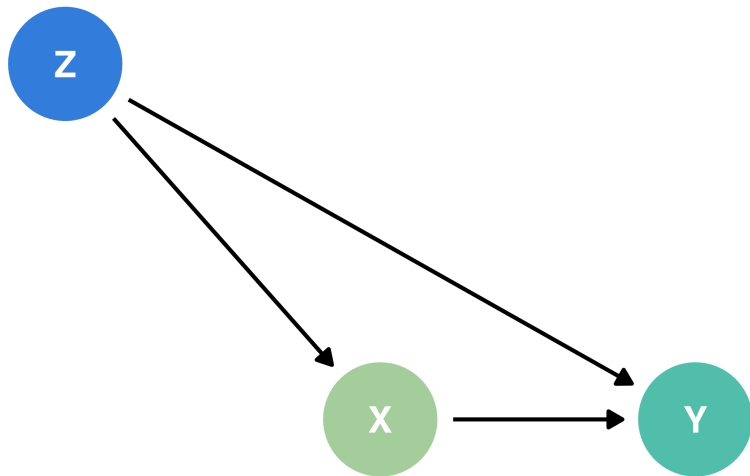
**To adjust or not adjust?  
That is the question.**

# Causal Quartet

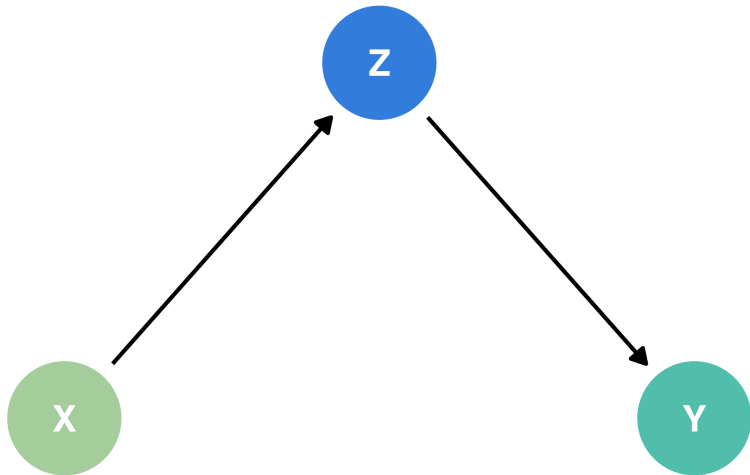
(1) Collider



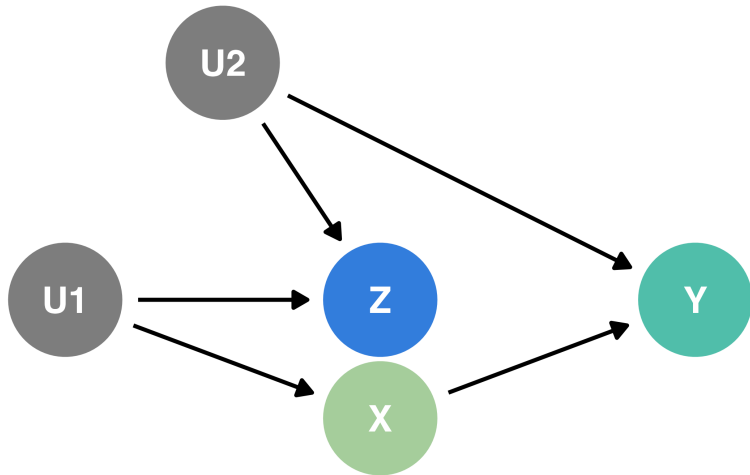
(2) Confounder



(3) Mediator



(4) M-bias







## Your turn 1

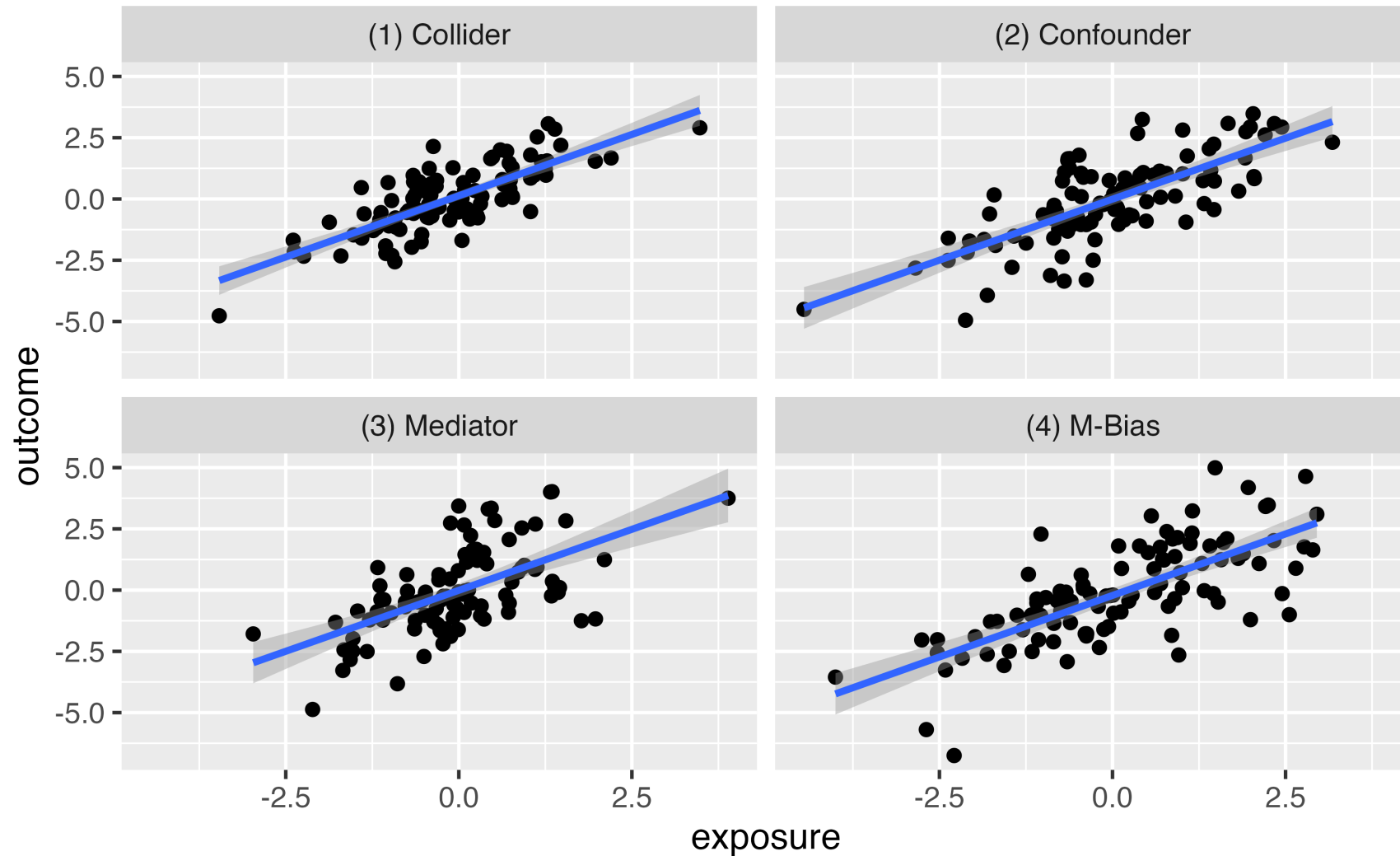
Load the **quartets** package

For each of the following 4 datasets, create a scatterplot looking at the relationship between **exposure** and **outcome**: **causal\_collider**, **causal\_confounding**, **causal\_mediator**, **causal\_m\_bias**

For each of the above 4 datasets, look at the correlation between **exposure** and **covariate**

**Stretch goal:** For each of the above 4 datasets, fit a linear model to examine the relationship between the **exposure** and the **outcome**

# Relationship between exposure and outcome



# Relationship between exposure and covariate

```
1 causal_quartet |>  
2   group_by(dataset) |>  
3   summarise(corr = cor(exposure, covariate))
```

```
# A tibble: 4 × 2
```

	dataset	corr
	<chr>	<dbl>
1	(1) Collider	0.700
2	(2) Confounder	0.696
3	(3) Mediator	0.696
4	(4) M-Bias	0.696

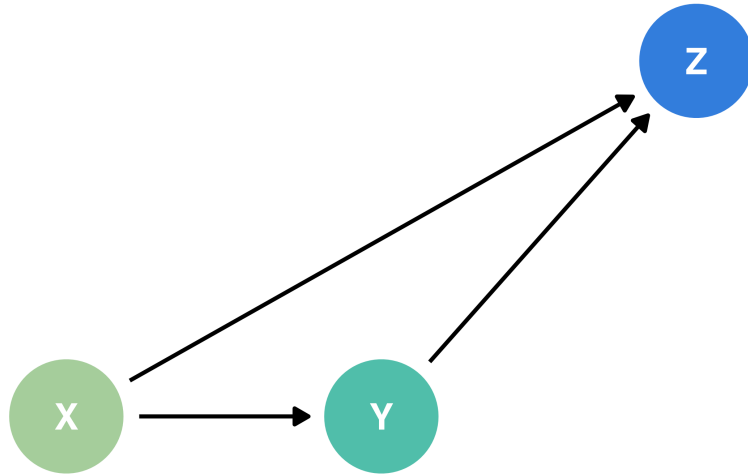
# Observed effects

Data generating mechanism	ATE		
	ATE not adjusting for Z	adjusting for Z	Correlation of X and Z
(1) Collider	1.00	0.55	0.70
(2) Confounder	1.00	0.50	0.70
(3) Mediator	1.00	0.00	0.70
(4) M-Bias	1.00	0.88	0.70

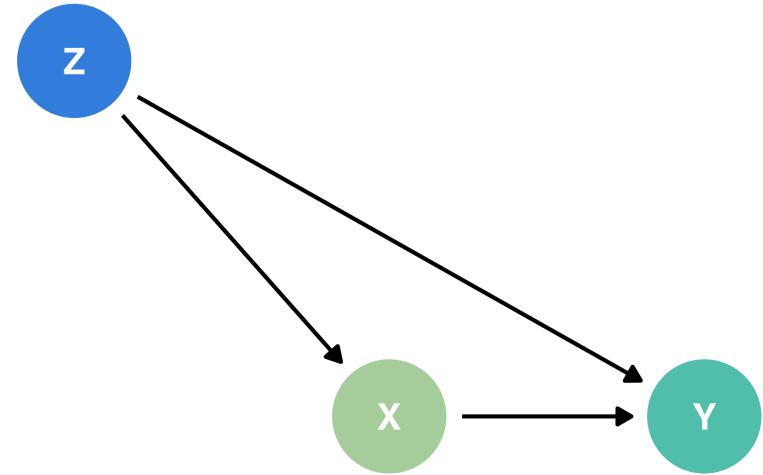
D’Agostino McGowan L, Gerke T, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

# The solution

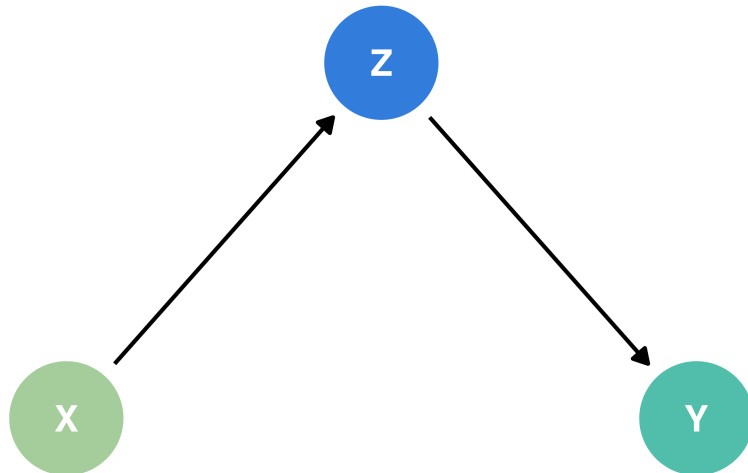
(1) Collider



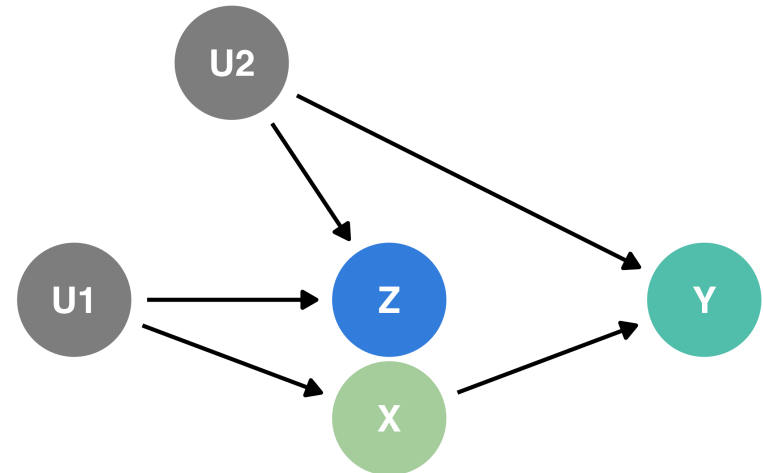
(2) Confounder



(3) Mediator



(4) M-bias



# Correct effects

Data generating mechanism	Correct causal model	Correct causal effect
(1) Collider	$Y \sim X$	1.0
(2) Confounder	$Y \sim X ; Z$	0.5
(3) Mediator	Direct effect: $Y \sim X ; Z$ Total Effect: $Y \sim X$	Direct effect: 0.0 Total effect: 1.0
(4) M-Bias	$Y \sim X$	1.0

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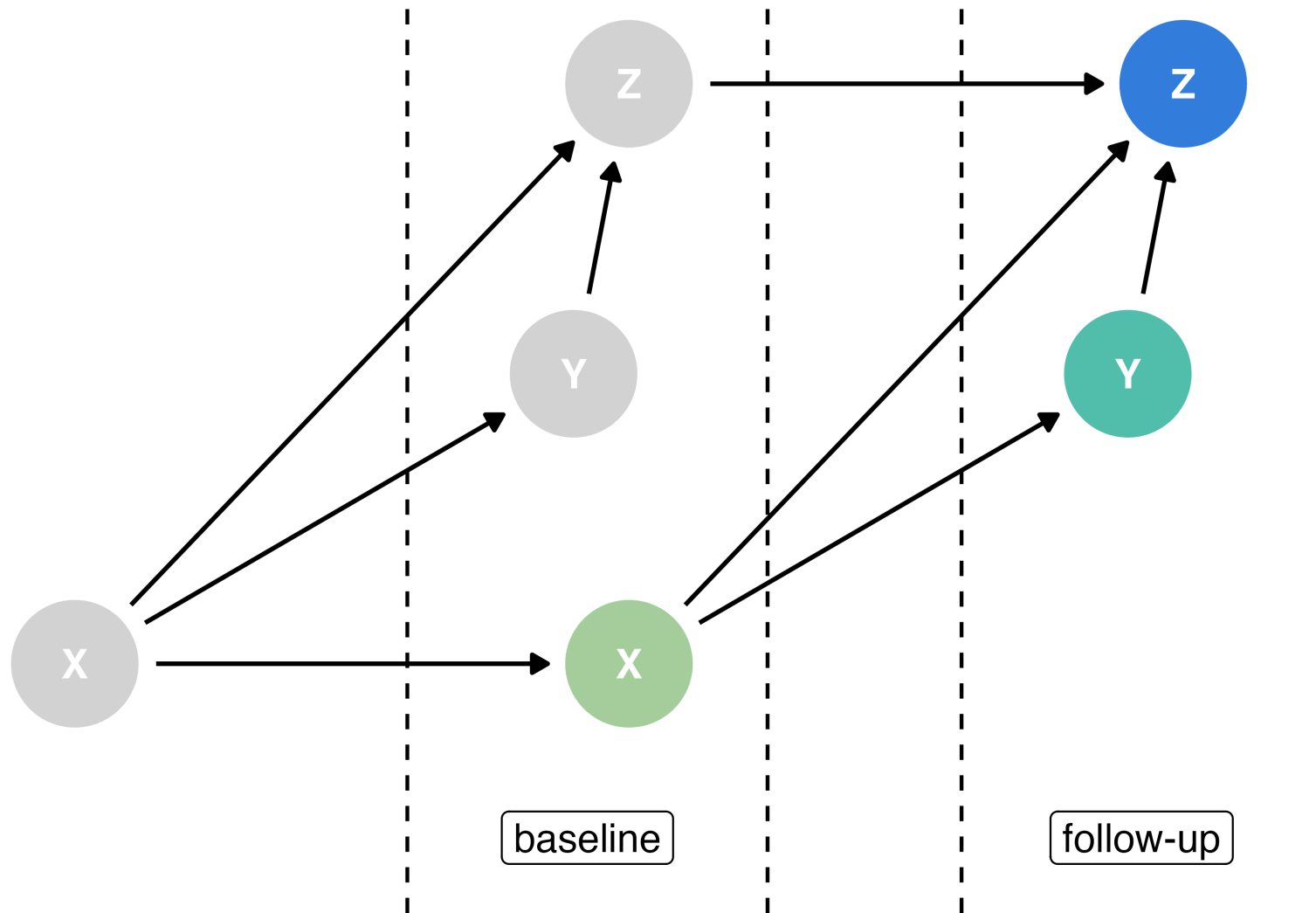
# The *partial* solution

```
1 causal_collider_time
```

```
# A tibble: 100 × 6
  exposure_baseline outcome_baseline covariate_baseline
      <dbl>          <dbl>          <dbl>
1      -1.43         0.287        -0.0963
2       0.0593       -0.978        -1.11
3       0.370        0.348         0.647
4      0.00471      0.851         0.755
5       0.340        1.94         1.19
6      -3.61       -0.235       -0.588
7       1.44       -0.827       -1.13
8       1.02      -0.0410        0.689
9      -2.43       -2.10       -1.49
10     -1.26      -2.41       -2.78
# i 90 more rows
# i 3 more variables: exposure_followup <dbl>,
#   outcome_followup <dbl>, covariate_followup <dbl>
```

*Time-varying data*

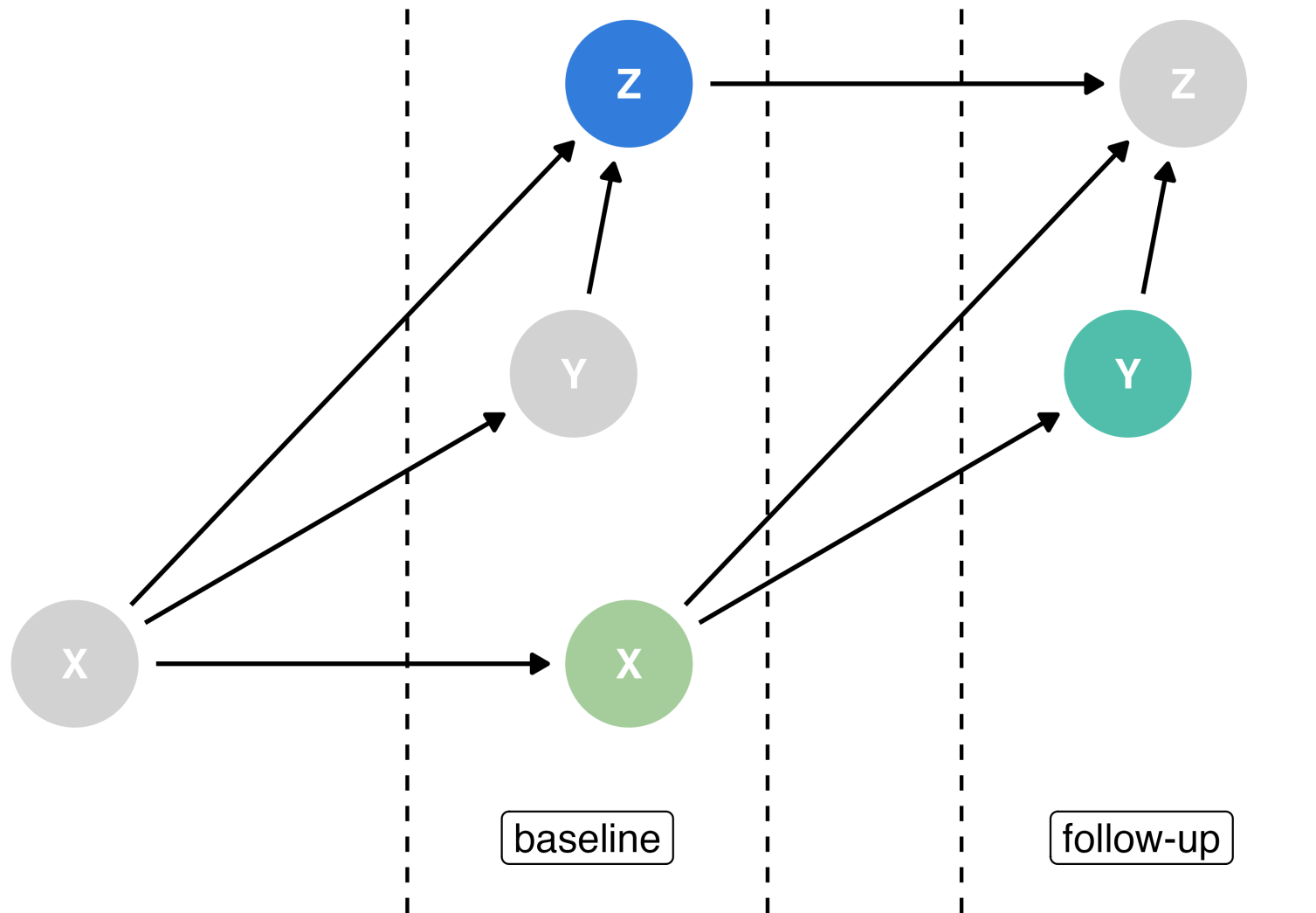
# Time-varying DAG



True causal effect: 1 Estimated causal effect: 0.55



# Time-varying DAG



True causal effect: 1 Estimated causal effect: 1

```
outcome_followup ~ exposure_baseline +  
covariate_baseline
```

## *Your turn 2*

For each of the following 4 datasets, fit a linear model examining the relationship between **outcome\_followup** and **exposure\_baseline** adjusting for **covariate\_baseline**:

- causal\_collider\_time,**
- causal\_confounding\_time,**
- causal\_mediator\_time, causal\_m\_bias\_time**

# The *partial* solution

Data generating mechanism	ATE not adjusting for pre-exposure Z	ATE adjusting for pre-exposure Z	Correct causal effect
(1) Collider	1.00	1.00	1.00
(2) Confounder	1.00	0.50	0.50
(3) Mediator	1.00	1.00	1.00
(4) M-Bias	1.00	0.88	1.00

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# On *M*-Bias

- The relationship between  $Z$  and the unmeasured confounders needs to be really large (Liu et al 2012)
- “To obsess about the possibility of [M-bias] generates bad practical advice in all but the most unusual circumstances” (Rubin 2009)
- There are (almost) no true zeros (Gelman 2011)
- Asymptotic theory shows that induction of M-bias is quite sensitive to various deviations from the exact M-Structure (Ding and Miratrix 2014)