

Task 6

A)

Checking the stability of system below.

```
Ag=[0 0 0 1 0 0;0 0 0 0 1 0;0 0 0 0 0 1;...  
    7.3809 0 0 0 2 0;0 -2.1904 0 -2 0 0;0 0 -3.1904 0 0 0]
```

```
Ag = 6x6  
      0      0      0      1.0000      0      0  
      0      0      0      0      1.0000      0  
      0      0      0      0      0      1.0000  
  7.3809      0      0      0      2.0000      0  
      0  -2.1904      0  -2.0000      0      0  
      0      0  -3.1904      0      0      0
```

```
Bg=[ [0 0 0 1 0 0]' [0 0 0 0 1 0]' [0 0 0 0 0 1]']
```

```
Bg = 6x3  
      0      0      0  
      0      0      0  
      0      0      0  
      1      0      0  
      0      1      0  
      0      0      1
```

```
e=eig(Ag)
```

```
e = 6x1 complex  
-2.1587 + 0.0000i  
 2.1587 + 0.0000i  
 0.0000 + 1.8626i  
 0.0000 - 1.8626i  
 0.0000 + 1.7862i  
 0.0000 - 1.7862i
```

The equilibrium point is not a stable position because one pole is on the right side of the complex plane.

B-C)

Controllability:

```
system_order = length(Ag)
```

```
system_order = 6
```

```
M = ctrb(Ag, Bg(:,1));  
rank_of_M = rank(M)
```

```
rank_of_M = 4
```

```
M = ctrb(Ag, Bg(:,2));  
rank_of_M = rank(M)
```

```
rank_of_M = 4
```

```
M = ctrb(Ag, Bg(:,3));
rank_of_M = rank(M)
```

```
rank_of_M = 2
```

From the fact that the controllability matrix for u_1 , u_2 and u_3 is of lower rank than the order of the system we conclude the system is not controllable from any input u .

D)

Determining the transfer function for $y=[0 \ 1 \ 0 \ 0 \ 0 \ 0]x$

```
Cg=[0 1 0 0 0 0];
Dg=0;
```

```
[NUM,DEN]=ss2tf(Ag,Bg(:,2),Cg,Dg)
```

```
NUM = 1x7
      0      0      1.0000      0.0000     -4.1905      0.0000     -23.5480
DEN = 1x7
      1.0000      0.0000      1.9999      0.0000     -19.9653      0.0000     -51.5796
```

```
sys=tf(NUM,DEN)
```

```
sys =
```

$$\frac{s^4 + 4.441e-16 s^3 - 4.191 s^2 + 1.776e-15 s - 23.55}{s^6 + 1.943e-16 s^5 + 2 s^4 + 3.325e-15 s^3 - 19.97 s^2 + 8.629e-15 s - 51.58}$$

Continuous-time transfer function.

E)

Controllability for $y=[0 \ 1 \ 0 \ 0 \ 0 \ 0]x$

```
zeros=zero(sys)
```

```
zeros = 4x1 complex
      -2.7168 + 0.0000i
       2.7168 + 0.0000i
       0.0000 + 1.7862i
       0.0000 - 1.7862i
```

```
poles=pole(sys)
```

```
poles = 6x1 complex
      -2.1587 + 0.0000i
       2.1587 + 0.0000i
       0.0000 + 1.8626i
       0.0000 - 1.8626i
      -0.0000 + 1.7862i
      -0.0000 - 1.7862i
```

```
K=1;
zeros=[zeros(1:2)]
```

```
zeros = 2×1
-2.7168
 2.7168
```

```
poles=[poles(1:4)]
```

```
poles = 4×1 complex
-2.1587 + 0.0000i
 2.1587 + 0.0000i
 0.0000 + 1.8626i
 0.0000 - 1.8626i
```

```
sys=zpk(zeros,poles,K)
```

```
sys =
```

$$\frac{(s+2.717)(s-2.717)}{(s+2.159)(s-2.159)(s^2 + 3.469)}$$

Continuous-time zero/pole/gain model.

```
NUM=conv([1 2.717],[1 -2.717])
```

```
NUM = 1×3
 1.0000      0   -7.3821
```

```
DEN=conv([1 2.159],[1 -2.159]);
DEN=conv(DEN,[1 0 3.469])
```

```
DEN = 1×5
 1.0000      0   -1.1923      0  -16.1700
```

```
[A,B,C,D] = tf2ss(NUM,DEN)
```

```
A = 4×4
      0    1.1923      0   16.1700
 1.0000      0      0      0
      0    1.0000      0      0
      0      0    1.0000      0
```

```
B = 4×1
      1
      0
      0
      0
```

```
C = 1×4
      0    1.0000      0   -7.3821
```

```
D = 0
```

```
system_order = length(A)
```

```
system_order = 4
```

```
M = ctrb(A,B);
rank_of_M = rank(M)
```

```
rank_of_M = 4
```

```
N = obsv(Ag, Cg);
```

```
rank_of_N = rank(N)
```

```
rank_of_N = 4
```

The system is now controllable given the uniformity of the rank of controllability matrix with system order.

F)

Designing a controller for system stabilisation.

```
desiredpoles = [-1+1i;-1-1i;-10;-10]
```

```
desiredpoles = 4×1 complex  
-1.0000 + 1.0000i  
-1.0000 - 1.0000i  
-10.0000 + 0.0000i  
-10.0000 + 0.0000i
```

```
K = acker(A,B,desiredpoles)
```

```
K = 1×4  
22.0000 143.1923 240.0000 216.1700
```

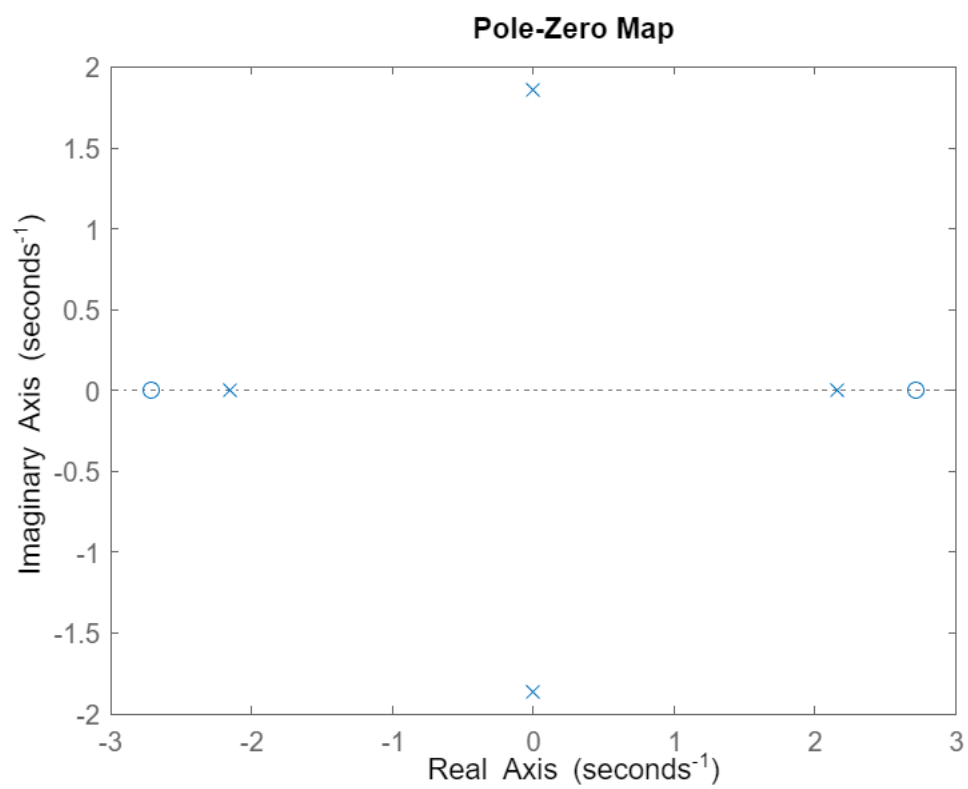
```
[num2,den2] = ss2tf(A - B * K,B,C,D);  
G = tf(num2,den2)
```

G =

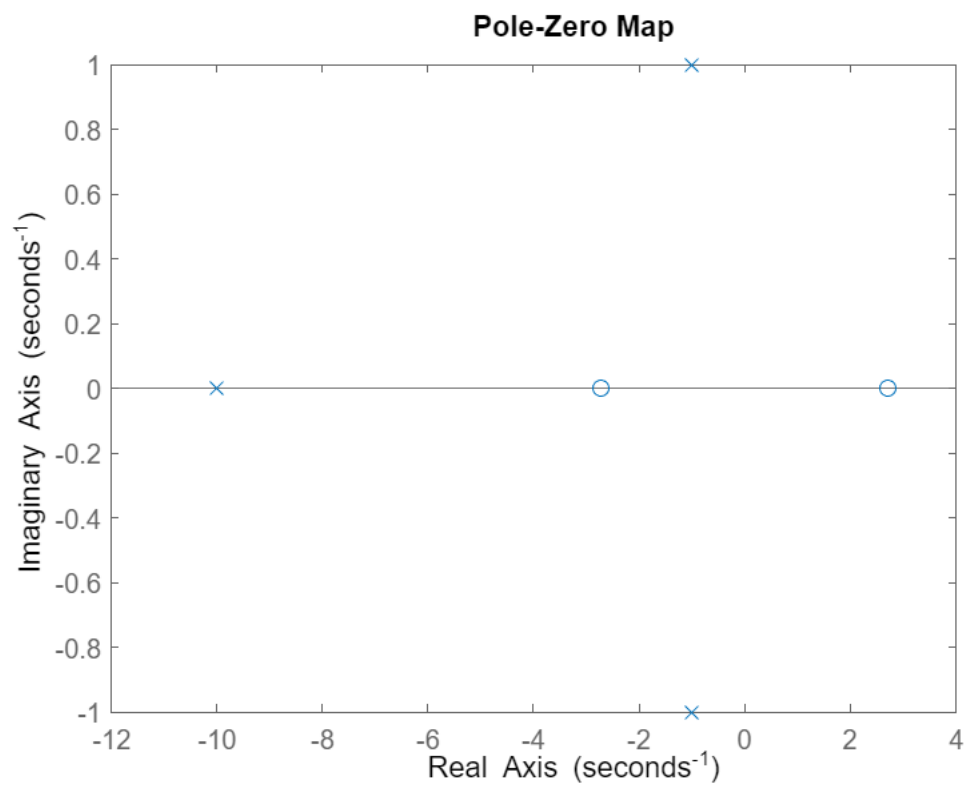
```
          s^2 - 7.382  
-----  
s^4 + 22 s^3 + 142 s^2 + 240 s + 200
```

Continuous-time transfer function.

```
pzmap(sys)
```



pzmap(G)



```
roots(den2)
```

```
ans = 4×1 complex  
-10.0000 + 0.0000i  
-10.0000 - 0.0000i  
-1.0000 + 1.0000i  
-1.0000 - 1.0000i
```

No positive real parts of poles imply stabilized system.