Algorythm:

1.1372

Foreward kinematics, for random joint and links valuees calculate the foreward kinematics:

```
for i = 1:10
algo_lab3
end
```

```
-----New System!-----
d1 val =
0.7920
a1 val =
0.2004
th2_val =
1.1372
a2_val =
0.6939
th3_val =
0.0453
d3_val =
0.2769
th4_val =
0.5531
d4_val =
0.1929
T04 val = 4 \times 4
   0.3222 -0.1989 -0.9256
                               0.0572
   0.7876
           -0.4862
                     0.3786
                                 0.8075
                     0
   -0.5253 -0.8509
                                 0.7920
                0
                            0 1.0000
       0
T03 = 4 \times 4
             0
0
                     -0.9256
   0.3786
                                 0.2357
   0.9256
                     0.3786
                                 0.7345
        0
            -1.0000
                          0
                                 0.7920
        0
                 0
                            0
                                 1.0000
P = 3 \times 1
   0.0572
   0.8075
   0.7920
pw = 3 \times 1
   -0.1785
   0.0730
pa = 3 \times 1
   0.2357
   0.7345
   0.7920
ans_s = struct with fields:
   q1: [2×1 sym]
   q2: [2×1 sym]
   q3: [2×1 sym]
q1_ik =
0.7920
d1_val =
0.7920
q2_ik =
1.1372
th2 val =
```

```
q3_ik =
0.0453
th3_val =
0.0453
ans_2 = 2 \times 1
  0.5531
  -0.5531
th4_val =
0.5531
-----New System!-----
d1_val =
0.2799
a1_val =
0.3442
th2 val =
0.7813
a2 val =
0.5954
th3_val =
0.9109
d3_val =
0.1637
th4_val =
0.2140
d4 val =
0.1540
T04_val = 4 \times 4
                    -0.9926
  -0.1184 0.0257
                               0.4515
   0.9700
           -0.2108 -0.1212 0.3808
                      0 0.2799
  -0.2124
           -0.9772
    0
             0
                            0
                                1.0000
T03 = 4 \times 4
                    -0.9926
  -0.1212
                                 0.6044
                 0
                 0 -0.1212
   0.9926
                                 0.3994
           -1.0000 0
                                0.2799
       0
                 0
                                 1.0000
P = 3 \times 1
   0.4515
   0.3808
   0.2799
pw = 3 \times 1
  -0.1528
  -0.0187
pa = 3 \times 1
   0.6044
   0.3994
   0.2799
ans_s = struct with fields:
   q1: [2×1 sym]
   q2: [2×1 sym]
   q3: [2×1 sym]
q1_ik =
0.2799
d1 val =
0.2799
q2 ik =
0.7813
th2_val =
```

```
0.7813
q3_ik =
0.9109
th3 val =
0.9109
ans_2 = 2 \times 1
 0.2140
  -0.2140
th4_val =
0.2140
-----New System!-----
d1_val =
0.2005
a1 val =
0.1818
th2 val =
0.5613
a2 val =
0.3971
th3_val =
-0.9748
d3_val =
0.1990
th4 val =
-2.2141
d4 val =
0.1330
T04_val = 4 \times 4
  -0.5493 0.7326 0.4019
                                0.6514
   0.2411 -0.3215 0.9157
                              0.5154
   0.8001 0.5999
                    0 0.2005
             0
                          0 1.0000
    0
T03 = 4 \times 4
   0.9157
                0 0.4019
                                0.5979
                0 0.9157
   -0.4019
                                0.3936
            -1.0000
                                0.2005
        0
                         0
        0
                0
                           0
                                1.0000
P = 3 \times 1
   0.6514
   0.5154
   0.2005
pw = 3 \times 1
   0.0534
   0.1218
pa = 3 \times 1
   0.5979
   0.3936
   0.2005
ans_s = struct with fields:
   q1: [2×1 sym]
   q2: [2×1 sym]
   q3: [2×1 sym]
q1 ik =
0.2005
d1_val =
0.2005
q2_ik =
0.5613
```

```
th2_val =
0.5613
q3_ik =
-0.9748
th3 val =
-0.9748
ans_2 = 2 \times 1
   2.2141
   4.0690
th4_val =
-2.2141
-----New System!-----
d1_val =
0.8656
a1 val =
0.4363
th2 val =
1.3497
a2_val =
0.5180
th3_val =
0.2601
d3_val =
0.2631
th4 val =
2.3814
d4 val =
0.6933
T04_val = 4 \times 4
   0.0282 0.0268 -0.9992
                               -0.4057
   -0.7242
           -0.6885
                     -0.0389 0.4681
   -0.6891
           0.7247
                          0 0.8656
                            0
                               1.0000
      0
              0
T03 = 4 \times 4
                     -0.9992
   -0.0389
                                 0.2871
   0.9992
                 0 -0.0389
                                 0.4951
       0
            -1.0000
                       0
                                 0.8656
        0
                  0
                                 1.0000
P = 3 \times 1
  -0.4057
   0.4681
   0.8656
pw = 3 \times 1
   -0.6928
   -0.0270
pa = 3 \times 1
   0.2871
   0.4951
   0.8656
ans_s = struct with fields:
   q1: [2×1 sym]
   q2: [2×1 sym]
   q3: [2×1 sym]
q1 ik =
0.8656
d1 val =
0.8656
q2_ik =
```

```
1.3497
th2_val =
1.3497
q3 ik =
0.2601
th3_val =
0.2601
ans_2 = 2 \times 1
   3.9018
   2.3814
th4_val =
2.3814
-----New System!-----
d1 val =
0.1005
a1 val =
0.6193
th2_val =
0.3536
a2_val =
0.6940
th3_val =
0.0870
d3 val =
0.1959
th4 val =
1.8934
d4 val =
0.2367
T04_val = 4 \times 4
   -0.2868 -0.8578 -0.4265
                                 1.0858
   -0.1352 -0.4045 0.9045
                                 0.6316
   -0.9484
           0.3171
                       0 0.1005
                            0 1.0000
      0
                0
T03 = 4 \times 4
   0.9045
                     -0.4265
                 0
                                 1.1867
   0.4265
                 0 0.9045
                                 0.4175
        0
             -1.0000
                          0
                                 0.1005
                 0
                            0
                                 1.0000
        0
P = 3 \times 1
   1.0858
   0.6316
   0.1005
pw = 3 \times 1
  -0.1010
   0.2141
pa = 3 \times 1
   1.1867
   0.4175
   0.1005
ans_s = struct with fields:
   q1: [2×1 sym]
   q2: [2×1 sym]
   q3: [2×1 sym]
q1_ik =
0.1005
d1_val =
0.1005
```

```
q2_ik =
0.3536
th2_val =
0.3536
q3 ik =
0.0870
th3 val =
0.0870
ans_2 = 2 \times 1
   4.3898
   1.8934
th4_val =
1.8934
-----New System!-----
d1_val =
0.5483
a1 val =
0.6405
th2_val =
0.2346
a2_val =
0.6071
th3_val =
0.7497
d3 val =
0.2172
th4 val =
-1.5913
d4 val =
0.4998
T04_val = 4 \times 4
   -0.0114 0.5534
                     -0.8329
                                  0.6338
                     0.5535
   -0.0171
                                  0.5380
           0.8327
   0.9998
           0.0205
                           0
                                  0.5483
                0
                                  1.0000
T03 = 4 \times 4
   0.5535
                     -0.8329
                                  1.0501
   0.8329
                 0 0.5535
                                  0.2613
        0
            -1.0000
                        0
                                  0.5483
                  0
                            0
                                  1.0000
        0
P = 3 \times 1
   0.6338
   0.5380
   0.5483
pw = 3 \times 1
   -0.4163
   0.2767
pa = 3 \times 1
   1.0501
   0.2613
   0.5483
ans_s = struct with fields:
   q1: [2×1 sym]
   q2: [2×1 sym]
   q3: [2×1 sym]
q1 ik =
0.5483
d1_val =
```

```
0.5483
q2_ik =
0.2346
th2 val =
0.2346
q3_ik =
0.7497
th3_val =
0.7497
ans_2 = 2 \times 1
   1.5913
   4.6919
th4_val =
-1.5913
-----New System!-----
d1 val =
0.1751
a1 val =
0.4756
th2_val =
0.5056
a2_val =
0.5379
th3 val =
1.2276
d3 val =
0.2965
th4_val =
1.6904
d4_val =
0.4489
T04_val = 4 \times 4
   0.0193 0.1605 -0.9868
                                   0.2106
            -0.9798
                      -0.1617
   -0.1177
                                   0.1400
   -0.9929
            0.1193
                           0
                                   0.1751
                  0
                                   1.0000
T03 = 4 \times 4
   -0.1617
                  0
                      -0.9868
                                   0.6536
    0.9868
                      -0.1617
                                   0.2126
                  0
         0
             -1.0000
                           0
                                   0.1751
         0
                  0
                              0
                                   1.0000
P = 3 \times 1
   0.2106
    0.1400
    0.1751
pw = 3 \times 1
   -0.4430
   -0.0726
pa = 3 \times 1
   0.6536
    0.2126
    0.1751
ans s = struct with fields:
    q1: [2×1 sym]
    q2: [2×1 sym]
    q3: [2×1 sym]
q1_ik =
0.1751
```

```
d1_val =
0.1751
q2_ik =
0.5056
th2 val =
0.5056
q3 ik =
1.2276
th3 val =
1.2276
ans_2 = 2 \times 1
   1.6904
   4.5928
th4_val =
1.6904
-----New System!-----
d1 val =
0.9355
a1_val =
0.4481
th2_val =
-1.5174
a2_val =
0.1725
th3 val =
1.1395
d3 val =
0.1969
th4_val =
2.1668
d4 val =
0.2256
T04_val = 4 \times 4
  -0.5217 -0.7692 0.3690
                                 0.6132
   0.2071
           0.3054 0.9294 0.2204
           0.5613
  -0.8276
                          0
                                 0.9355
                0
                                 1.0000
T03 = 4 \times 4
  0.9294
                 0 0.3690 0.5299
  -0.3690
                0 0.9294
                                 0.0107
                       0
      0
           -1.0000
                                 0.9355
        0
                 0
                           0
                                 1.0000
P = 3 \times 1
   0.6132
   0.2204
   0.9355
pw = 3 \times 1
   0.0833
   0.2097
pa = 3 \times 1
   0.5299
   0.0107
   0.9355
ans_s = struct with fields:
   q1: [2×1 sym]
   q2: [2×1 sym]
   q3: [2×1 sym]
q1_ik =
```

```
0.9355
d1_val =
0.9355
q2 ik =
-1.5174
th2_val =
-1.5174
q3_ik =
1.1395
th3_val =
1.1395
ans_2 = 2 \times 1
  4.1164
    2.1668
th4_val =
2.1668
-----New System!-----
d1 val =
0.5971
a1_val =
0.4779
th2_val =
-1.4703
a2 val =
0.4688
th3 val =
-0.4322
d3 val =
0.1099
th4_val =
-0.0655
d4_val =
0.2155
T04_val = 4 \times 4
   -0.3250 -0.0213 0.9455
                                0.8326
   -0.9434
           -0.0619 -0.3257 -0.5724
    0.0655
           -0.9979
                          0 0.5971
                  0
                             0
                                1.0000
T03 = 4 \times 4
  -0.3257
                  0
                      0.9455
                                 0.6289
   -0.9455
                 0
                     -0.3257
                                 -0.5023
        0
             -1.0000
                        0
                                  0.5971
                             0
                                  1.0000
        0
                  0
P = 3 \times 1
   0.8326
   -0.5724
   0.5971
pw = 3 \times 1
   0.2038
   -0.0702
        0
pa = 3 \times 1
   0.6289
   -0.5023
   0.5971
ans_s = struct with fields:
   q1: [2×1 sym]
    q2: [2×1 sym]
    q3: [2×1 sym]
```

```
q1_ik =
0.5971
d1_val =
0.5971
q2 ik =
-1.4703
th2 val =
-1.4703
q3_ik =
-0.4322
th3_val =
-0.4322
ans_2 = 2 \times 1
   0.0655
   -0.0655
th4 val =
-0.0655
-----New System!-----
d1_val =
0.2108
a1_val =
0.2233
th2_val =
-1.1105
a2_val =
0.2134
th3 val =
-1.4368
d3 val =
0.2270
th4_val =
-1.3706
d4_val =
0.4232
T04_val = 4x4
                      0.5599
   -0.1648
           -0.8120
                                0.6822
   -0.1114
           -0.5487
                     -0.8285 -0.7299
   0.9800
           -0.1989
                            0
                                0.2108
                 0
                             0
                                  1.0000
       0
T03 = 4 \times 4
                      0.5599
   -0.8285
                  0
                                0.4452
   -0.5599
                 0
                     -0.8285 -0.3793
                        0
                                  0.2108
        0
             -1.0000
                                  1.0000
        0
                  0
                             0
P = 3 \times 1
   0.6822
   -0.7299
   0.2108
pw = 3 \times 1
   0.2369
   -0.3506
        0
pa = 3 \times 1
   0.4452
   -0.3793
   0.2108
ans s = struct with fields:
```

```
q1: [2×1 sym]
    q2: [2×1 sym]
    q3: [2×1 sym]
q1 ik =
0.2108
d1 val =
0.2108
q2_ik =
-1.1105
th2_val =
-1.1105
q3_ik =
-1.4368
th3 val =
-1.4368
ans 2 = 2 \times 1
  -1.3706
    1.3706
th4_val =
-1.3706
```

```
function algo_lab3
% this script determines a Homogeneous Transformation matrix
clear
disp(' ')
disp(" ")
disp('----')
d1_val=random('Uniform',0.1,1)
a1 val=random('Uniform',0.1,0.7)
th2_val=random('Uniform',-pi/2,pi/2)
a2_val=random('Uniform',0.1,0.7)
th3_val=random("Uniform",-pi/2,pi/2)
d3_val=random('Uniform',0.1,0.3)
th4_val=random('Uniform',-pi,pi)
d4_val=random('Uniform',0.1,0.7)
disp(" ")
A1=mA(0,d1_val,a1_val,0);
A2=mA(th2_val,0,a2_val,0);
A3=mA(th3_val,0,0,sym(-pi/2));
A32=mA(0,d3_val,0,0);
A4=mA(th4_val,d4_val,0,0);
T04_val=double(A1*A2*A3*A32*A4)
T03=double(A1*A2*A3*A32)
P=T04 \ val(1:3,4)
pw=T04_val(1:3,3)*d4_val
pa=P-pw %same as T03u
```

```
%
% T04n=subs(T04,{d1,a1,th2,a2,th3,d3,th4,d4},{d1_val,a1_val,th2_val,a2_val, ...
      th3_val,d3_val,d4_val,d4_val})
%%
syms d1 a1 th2 a2 th3 th4 d3 d4 q1 q2 q3 q4 real
A1=mA(0,d1,a1,0);
A2=mA(th2,0,a2,0);
A3=mA(th3,0,0,sym(-pi/2));
A32=mA(0,d3,0,0);
A4=mA(th4,d4,0,0);
T03=A1*A2*A3*A32;
T03v=subs(T03,{d1,a1,th2,a2,th3,d3},,q1,a1_val,q2,a2_val,q3,d3_val});
disp(" ")
eq = pa==(T03v(1:3,4));
ans_s=(solve(eq,[q1,q2,q3]))
q1_ik=double(ans_s.q1(1))
d1 val
q2_ik=double(ans_s.q2(1))
th2 val
q3_ik=double(ans_s.q3(1))
th3_val
T04=A1*A2*A3*A32*A4;
T04v=subs(T04,{d1,a1,th2,a2,th3,d3,th4,d4},
{d1_val,a1_val,th2_val,a2_val,th3_val,d3_val,q4,d4_val});
eq2 = T04_val(3,2) == (T04v(3,2));
disp(" ")
ans_2=double(solve(eq2,q4))
th4_val
end
```