

dte_adj: A Python Package for Estimating Distributional Treatment Effects in Randomized Experiments

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DOI: [10.xxxxxx/draft](https://doi.org/10.xxxxxx/draft)

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Submitted: 01 January 1970

Published: unpublished

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Summary

dte_adj is a Python package for estimating distributional treatment effects (DTEs) in randomized experiments (RCTs, also known as A/B tests). Unlike traditional approaches that focus on average treatment effects, dte_adj enables researchers to analyze the full distributional impact of interventions across different outcome levels. The package implements machine learning-enhanced regression adjustment methods for variance reduction, supports multiple experimental designs including simple randomization, covariate-adaptive randomization, and settings with imperfect compliance, and provides a scikit-learn compatible API with comprehensive functionality for computing distribution functions, probability treatment effects, and quantile treatment effects with confidence intervals.

Statement of Need

Randomized experiments have been fundamental to scientific inquiry since Fisher (1935), providing the gold standard for causal inference. While most experimental analyses focus on average treatment effects (ATEs), many research questions require understanding how treatments affect the entire distribution of outcomes. Distributional treatment effects (DTEs) capture these richer patterns, revealing heterogeneous impacts across different outcome levels that averages can mask. For example, a policy intervention might have no effect on average income while substantially reducing poverty rates at lower quantiles, or a medical treatment might benefit patients at the tails of the distribution differently than those near the median.

Despite the growing importance of distributional analysis in economics, medicine, and technology, the Python ecosystem lacks comprehensive tools for DTE estimation with modern variance reduction techniques. Researchers often resort to basic empirical CDFs or manual implementations that lack statistical rigor. dte_adj fills this gap by providing a unified framework for distributional treatment effect analysis that integrates state-of-the-art machine learning methods for improved precision, rigorous confidence interval construction, and support for complex experimental designs.

State of the Field

Several Python packages address causal inference, but none focus on distributional treatment effects with machine learning-based variance reduction:

- **SciPy** (Virtanen et al., 2020): Provides basic empirical cumulative distribution functions but offers no functionality for treatment effect estimation or confidence interval

- 38 construction in experimental settings.
- 39 ■ **DoWhy** (Sharma & Kiciman, 2020): Focuses on causal graph-based inference and
40 average treatment effects, without distributional analysis capabilities.
- 41 ■ **EconML** (Battocchi et al., 2021): Incorporates machine learning for heterogeneous
42 treatment effect estimation (CATE) but does not address distributional effects.
- 43 ■ **causal-curve** (Kobrosly, 2020): Estimates dose-response curves but targets continuous
44 treatments rather than distributional outcomes.

45 In the R ecosystem, packages like `qte` provide quantile treatment effect estimation but
46 lack machine learning integration for variance reduction. `dte_adj` uniquely combines: (1)
47 distributional treatment effect estimation across the full outcome distribution, (2) machine
48 learning-enhanced regression adjustment for precision gains, and (3) support for multiple
49 experimental designs including covariate-adaptive randomization and imperfect compliance
50 settings.

51 Software Design

52 `dte_adj` follows a class-based architecture with a template method pattern, where a base class
53 defines the algorithm structure and subclasses implement design-specific computations:

- 54 ■ **SimpleDistributionEstimator** and **AdjustedDistributionEstimator**: For simple
55 randomized experiments, implementing methods from Byambadalai et al. (2024).
- 56 ■ **SimpleStratifiedDistributionEstimator** and **AdjustedStratifiedDistributionEstimator**:
57 For covariate-adaptive randomization designs, implementing methods from Byambadalai
58 et al. (2025b).
- 59 ■ **SimpleLocalDistributionEstimator** and **AdjustedLocalDistributionEstimator**: For
60 settings with imperfect compliance, implementing methods from Byambadalai et al.
61 (2025a).

62 All estimators implement a consistent API with three primary methods: `predict_dte()` for
63 distributional treatment effects, `predict_pte()` for probability treatment effects over intervals,
64 and `predict_qte()` for quantile treatment effects. The adjusted estimators use K-fold cross-
65 fitting to prevent overfitting and support both single-task and multi-task learning modes (Hirata
66 et al., 2025) for computational efficiency. Bootstrap methods provide confidence intervals with
67 multiple variance estimation approaches.

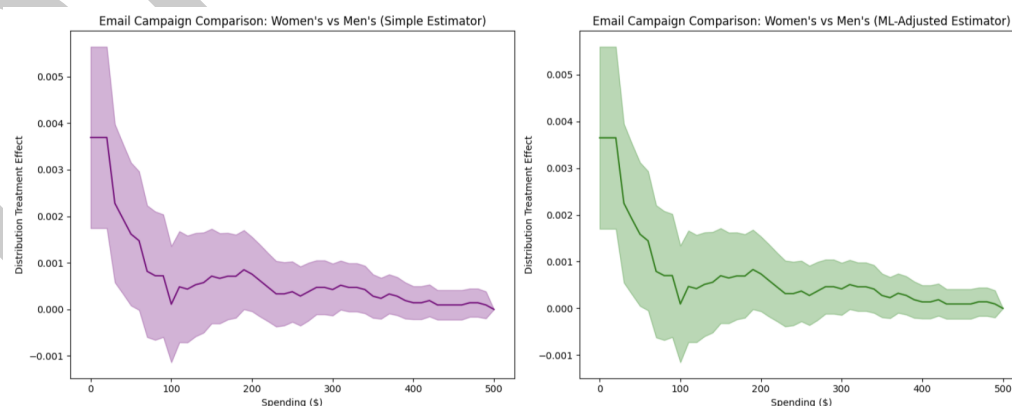


Figure 1: Distributional treatment effects for the Hillstrom email marketing dataset (Hillstrom, 2008), comparing Women's vs Men's email campaigns. The simple estimator (left, purple) and ML-adjusted estimator (right, green) show that adjustment substantially tightens confidence bands, demonstrating the variance reduction benefit of regression adjustment.

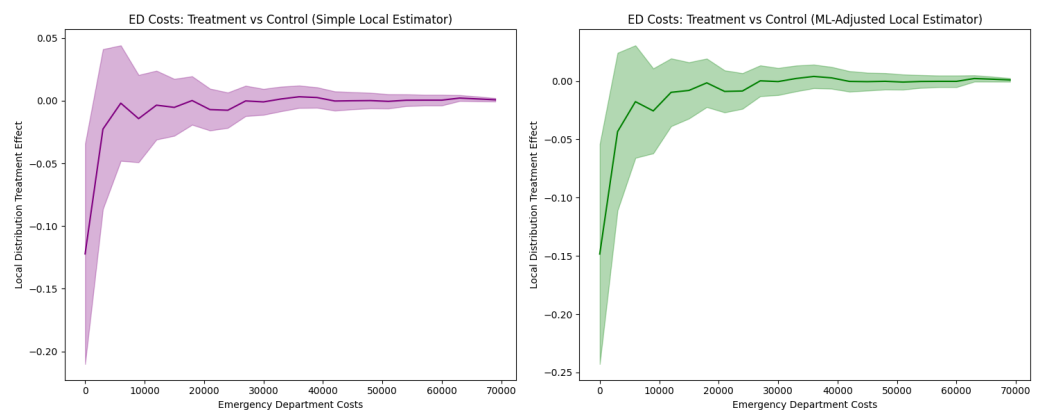


Figure 2: Local distributional treatment effects for emergency department costs in the Oregon Health Insurance Experiment (Finkelstein et al., 2012), estimated using SimpleLocalDistributionEstimator (left) and AdjustedLocalDistributionEstimator (right). Health insurance coverage shifts the distribution of ED costs, with ML adjustment again yielding narrower confidence intervals.

68 Research Impact Statement

69 The methods implemented in `dte_adj` have been published at top machine learning venues:
 70 ICML 2024 (Byambadalai et al., 2024) and ICML 2025 (Byambadalai et al., 2025b).
 71 The package has been used internally at CyberAgent, Inc. for analyzing A/B tests where
 72 distributional impacts are critical, such as evaluating interventions on user engagement
 73 metrics where tail behavior matters more than averages. The documentation includes tutorials
 74 demonstrating applications to the Hillstrom email marketing dataset (Figure 1) and the Oregon
 75 Health Insurance Experiment (Figure 2), facilitating adoption by researchers in economics,
 76 marketing, and healthcare.

77 AI Usage Disclosure

78 Generative AI tools (Claude) were used to assist with documentation writing and code review
 79 during development. All AI-generated content was reviewed and validated by the human
 80 authors.

81 Acknowledgements

82 We thank CyberAgent, Inc. for supporting this research and the open-source community for
 83 valuable feedback during development.

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