

The Variable Mass Theory and Gravitational Paradoxes

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ABSTRACT

Essential reading is the first article in the series, which is about Atomic Time, Orbital Time and the Variable Mass Theory. It has been shown in this article that General Relativity (GR) can be effectively replaced by Variable Mass (VM) in a Static Euclidean Universe (SEU), which is eternal in Atomic time and has moments of creation (i.e. one or more beginnings) in Orbital time.

The cosmological redshift is intrinsic: it only depends on variable (elementary particle rest) mass. Because that is where the VM theory has been designed for.

A convenient consequence is that Newton's theory is good enough for describing gravity at a cosmic scale. It is demonstrated that the latter, when combined with the Variable Mass hypothesis, solves for Gravitational Paradoxes.

CONTENTS

1. Static Euclidean Universe
 2. Infinite and Eternal
 3. NO curved Space-Time
 4. The Big Bang never happened
 5. The Cosmological Redshift
 6. A Paradox of Gravitation
 7. Solution by Simeon Albert
 8. Seeliger's Paradox
 9. References
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1. Static Euclidean Universe

The "observed" universe, so much celebrated by certain empiricists, has an obvious drawback: it changes every year with the advent of a new telescope. It is hardly possible to build a sensible, let it be predictive, theory upon such a wildly varying concept. So let us make a fresh start with **theory**, apart from being "observed" or not.

Essential reading is the first article in this series, which is called *Atomic Time, Orbital Time and the Variable Mass Theory* [1] The Variable Mass Theory (VM) is compatible with a *static Euclidean universe*, which is *eternal* in Atomic time and has moments of creation (i.e. one or more beginnings) in Orbital time. Moreover it turns out that - in order to arrive at very much the same results as obtained by [Arp and Narlikar](#) in [32] - *General Relativity is not needed*. GR has not become invalid, but it's rather irrelevant at a cosmic scale. More systematically:

- The *universe*, as something that contains everything, does not exist.
Way of speaking: it's *infinite*.
- There is space, there is time, but there is NO space-time.
Space is infinite, (atomic) time is eternal.
- There does not exist another geometry in nature than common *Euclidean geometry*.
There is NO curved space-time.
- Consequently, a Static Euclidean Universe (SEU), as advocated by [Eric Lerner](#) [2], shall be adopted.
- Mainstream Big Bang theory is challenged by proposing that the universe is not expanding.
With other words: *The Big Bang never happened* [3].

- For the purpose of cosmology, GR is effectively replaced by VM.
A convenient consequence is that Newton's theory of gravity is sufficient at a cosmic scale.
- It will be assumed that the *mass density distribution* in SEU cosmos is *uniform*.

Some of the above will need additional explanation.

2. Infinite and Eternal

Our theory starts with the assumption that the universe is infinite in space and time. Because of [Russell's Paradox](#) [5] and *Infinitum Actum Non Datur* [6] this effectively means that "[There is no Universe](#)" [7] at all; in the sense that there would exist something that contains everything. Our infinite universe, according to Gauss' dictum below, is just a way of speaking:

[Was nun aber Ihren Beweis für (1) betrifft,] so protestiere ich zuvörderst gegen den Gebrauch einer unendlichen Größe als einer Vollendeten, welcher in der Mathematik niemals erlaubt ist. Das Unendliche ist nur eine façon de parler, indem man eigentlich von Grenzen spricht, denen gewisse Verhältnisse so nahe kommen als man will, während andern ohne Einschränkung zu wachsen verstattet ist. (C.F. Gauss [in a letter to Schumacher, 12 July 1831])

I protest against the use of infinite magnitude as something completed, which is never permissible in mathematics. Infinity is merely a way of speaking, the true meaning being a limit which certain ratios approach indefinitely close, while others are permitted to increase without restriction.

[Carl Friedrich Gauss](#) [8] (30 April 1777 - 23 February 1855) was a German mathematician and physical scientist who contributed significantly to many fields, including number theory, statistics, analysis, differential geometry, geodesy, geophysics, electrostatics, astronomy and optics. Gauss referred to **mathematics** as "*the queen of sciences*", hence as a **science**.

3. NO curved Space-Time

A first consequence of the hypothesis that our universe is "infinite" is the nature of **geometry**, which is simply Euclidean and flat. There is no need at all for the curved **Spacetime** geometries [9] of General Relativity. An infinite Euclidean universe readily solves the [Flatness problem](#) [10] and the [Horizon problem](#) [11] in the first place. It does - of course - not solve the [Magnetic monopole](#) [12] problem, which is just another artefact, arising from distorting Maxwell's classical laws of electromagnetism.

In Einstein's General Relativity theory, a four-dimensional space-time [manifold](#) [13] is employed, which is curved into nothingness. The latter may be regarded as a distortion too. By the way, nothing is special about the mathematics of *tensor calculus* in GR : **Solid Mechanics** [14] *extensively uses tensors to describe stresses, strains, and the relationship between them* (Wikipedia). A surface may be bent in a space with a higher dimension. But nowhere in Solid Mechanics - or elsewhere in classical physics - there exist [Applications of Manifolds not embedded in Euclidean Space](#) [15].

Apart from physics, the whole idea of [Minkowski space-time](#) [16] is doubtful in another respect. Let us quote from an article by Norman (N J) Wildberger, titled [Evolution versus Intelligent Design: a mathematician's view](#) [17]. *Going more out on a limb, I will call on modern neuro-psychology and Einstein's theories of relativity to destabilize the familiar view of the universe as a dynamic place which is unfolding as we watch, along lines that we can potentially understand. I will suggest that the world has already been created in its historical entirety. We are just too low dimensional and internal to it to witness it across both space and time. This is consistent with the idea of an omniscient deity, whose existence probably implies that everything is already known, and so any idea of **free will must be an illusion**. Alright, so humanity is guilty of nothing. Because we couldn't have done otherwise, even if we wanted to.*

Or, as formulated by Doug Marett (2013) in his [Spacetime- Right or Wrong?](#) [18]: *What space-time implies is that all events, past, present and future, are already written in the fabric of space. Such a conclusion relegates all human activity to simply being automata acting out the frames of a preordained film strip. If we were to believe Einstein we would have to believe that there is **no free will** at all. That in and of itself should be reason enough to reject the space-time concept without further consideration!*

From [Relativity Reexamined](#) [19] at page 29: *Einstein wanted to reduce all physics to pure geometry; he thought that a conveniently curved space-time universe would provide an explanation for all physical laws from electromagnetism to gravitation. This was his avowed aim and he worked toward this goal for half of*

his life. [..] But the goal was never reached. Einstein managed to interconnect curved geometry and gravitation in a brilliant way, but his **unitary theory**, as he called it, was **never achieved**.

A chain reference in our key article [1] is the [1993 publication](#) [32] by [Jayant Narlikar](#) [4] and [Halton Arp](#) [33]. From that publication we quote: *Finally, the **Euclidean, flat spacetime** becomes a natural, primary reference frame in which cosmological processes are most simply described.* Actually Narlikar has proved herewith that **General Relativity is redundant** on a cosmic scale.

The geometries in Einstein's General Relativity theory have been made "possible" by the discovery of [Non-Euclidean geometry](#) [20] (Wikipedia) in the beginning of the 19th century. This has led to the (mis)understanding that non-Euclidean geometries might possibly be relevant to physics. However, the only thing it shows is that Euclid's Fifth's Postulate - the one of the parallel lines - cannot be deduced from the other postulates; it's an independent axiom. Which as such is an important result indeed. Non-Euclidean geometries can always be embedded in Euclidean geometry - there are many [models of non-Euclidean geometry](#) [21] in common geometry.

In a posting at Mathematics Stack Exchange, titled [Non-Euclidean Geometrical Algebra for Real times Real?](#) [22], it is argued that Euclid's Fifth's Postulate is not only essential for Euclidean geometry, but it's also essential for elementary algebra. I have yet to see any decent example contradicting this evidence: *without the axiom of parallel lines elementary algebra cannot even exist.* However, Einstein's tensor calculus eventually rests on elementary algebra. How then can space-time of General Relativity be non-Euclidean?

4. The Big Bang never happened

Let's proceed with another quote from the above mentioned article [17] by N J Wildberger:

Scientific types ought to be a bit more open-minded about things which border on the unknowable. Dramatic denials of God or any kind of cosmic intelligence by biologists, esteemed as they may be in their own communities, seem to me to be almost as unjustifiable as the emphatic assertions of religious extremists, or the overly confident descriptions of the first trillionth of a second by Big-Bangers. Namely according to the standard [Chronology of the universe](#) [23] (Wikipedia).

Another quote comes from the book by Hans Jörg Fahr - *Mit oder ohne Urknall* [24] - and is copied / translated from page 33 without permission. It is noticed that page 314 contains literally the same piece of text, unless there is something wrong with my memory. Or the message is so important that it cannot be repeated often enough. [Starts with a Bang](#) [25]:

Warum also drängt sich das Bild des Urknalls dennoch dem menschlichen Verstand mit so starker Suggestivität auf, förmlich wie eine unvermeidliche Vision? Natürlich haben Bilder einer Atombombenexplosion hierbei ihre ungeheuerliche Suggestivkraft entfaltet. Doch fragt man sich dann aber angesichts solcher Bilder: Entsteht hier eine Welt? Oder vergeht hier eher eine? Auch bei Bildern einer Supernova Explosion geht es einem kaum anders; auch hier glaubt man so etwas wie einen lokalen Weltbeginn wahrzunehmen, und man fragt sich: Könnte nicht vielleicht die Welt als ganze in Form einer globalen Meganova-Explosion, sozusagen wie aus einer gigantischen Wasserstoffbombe hervorgegangen sein?

So why is the image of the Big Bang so pressing upon the human mind with such strong suggestiveness, punctiliously like an inevitable vision? Of course images of an atomic bomb explosion have meanwhile unfold their tremendous suggestive power. Yet one is asking in the face of such images: is a world emerging here? Or does one rather perish? Also with images of a supernova explosion things go hardly different; here also one believes to perceive something like a local world beginning, and one wonders: Couldn't the world as a whole have been born in the form of a global meganova explosion, so to speak as if it had emerged from a gigantic hydrogen bomb?

The glorification of **violence** is indeed *Bankrupting Physics*. Think about particle accelerators for example, especially the [Large Hadron Collider](#) [26]. As if Depth of Truth is proportional to Heaviness of Bombardment. As if all this smashing of matter can reveal anything else than space debris. [The Embarrassing Nonsense of Particle Physicists - No, we do not need a New Collider](#) [27]. It is clear, however, that modern physics is herewith just following a common trend in our nowadays "civilized" society, where you can hardly watch a movie without a murder in it. Death seems to be more interesting than life. Standard (cosmological) models of nowadays physics say more about us humans than they reveal about the outside world.

But okay, let's forget about all this and go back to business. Is it true that no other than [Censored Papers Demolish the Big Bang Hypothesis](#) [28]? According to the Big Bang model, any Static Euclidean Universe is

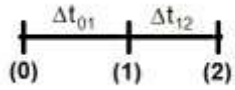
out of the question indeed. One of the most frequently employed arguments to defend this stand is [Olbers' Paradox](#) (Wikipedia) [29] which is also known as the "dark night sky paradox". We certainly have to deal with Olbers' Paradox in a SEU. However, it's not impossible that *observational evidence* is in favour of the latter. Particularly relevant in this respect is the information that has recently reached us via the [James Webb Telescope](#) [31].

5. The Cosmological Redshift

Cosmological Redshift [34] is the phenomenon that *all* wavelengths λ as received from cosmic objects - in the past - are *larger* than corresponding wavelengths λ_0 here and now on earth. Expressed into common $z =$ redshift notation that is:

$$z = \frac{\lambda - \lambda_0}{\lambda_0} = \frac{\lambda}{\lambda_0} - 1 > 0$$

Take a look at the picture below, depicting a timeline *running backwards* (= forward distance) in cosmos. Let (0) be our position on earth, (1) is the position of a far away civilization like ours, (2) is the position of a galaxy observed by observers on both habitable planets (0) and (1).



Let $\lambda =$ wavelength of light. Then it is mathematically obvious that:

$$\frac{\lambda_1}{\lambda_0} \frac{\lambda_2}{\lambda_1} = \frac{\lambda_2}{\lambda_0}$$

And therefore, by definition of any redshift as $z_{ab} = (\lambda_b - \lambda_a)/\lambda_a$:

$$1 + z_{02} = (1 + z_{01})(1 + z_{12})$$

It is reasonable to assume that the whole Δt_{02} is the sum of the parts Δt_{01} and Δt_{12} and so

$$1 + z = F(\Delta t) \quad \text{where} \quad F(\Delta t_{02}) = F(\Delta t_{01}) \cdot F(\Delta t_{12}) = F(\Delta t_{01} + \Delta t_{12})$$

This makes the function F a special one, because it is seen now that the following property must hold for all time intervals (t, τ) .

$$\ln(F(t + \tau)) = \ln(F(t)) + \ln(F(\tau))$$

We need additional mathematics, namely: *Additive functions and measure theory* [35]. From that reference it is inferred that the logarithm of our function F is *linear*. And so the redshift itself (plus one) is an exponential function.

$$\ln(F(t)) = \kappa \cdot t \quad \implies \quad F(t) = 1 + z = e^{\kappa \cdot t}$$

where κ is a constant that has to be determined from physics.

Essential reference is *Atomic Time, Orbital Time and the Variable Mass Theory* [1], which is to be considered as Part I of the current series on VM. In there an alternative derivation of the above is found, namely in the section 6. *Mass in Atomic Time*. Taking a further look at the content of the paper, we have respectively the formulas (5), (9) and (11):

$$1 + z = \frac{m_0}{m} \quad ; \quad \frac{m}{m_0} = e^{H \cdot t} \quad ; \quad A = \frac{2}{H} \quad \text{or} \quad \frac{1}{2}H = \frac{1}{A}$$

where $z =$ **intrinsic redshift** [30], which is typical for the Variable Mass Theory. Furthermore $t =$ time, $A =$ age (as measured in Orbital time), $m =$ (elementary particle rest) mass, $_0 =$ here and now.

From the previous it is easily concluded that our constant kappa is minus the familiar Hubble parameter:

$$1 + z = e^{\kappa \cdot t} = \frac{m_0}{m} = e^{-H \cdot t} \quad (1)$$

A further consequence is the *logarithmic distance formula*, which is formula (12) in our key reference [1]:

$$d = \frac{c}{H} \ln(1 + z) \quad (2)$$

where d = distance, c = lightspeed in empty space. It should be noticed that there are Hubble tensions in H , making it possible that there are different intrinsic redshifts z at the same distance d .

6. A Paradox of Gravitation

Key reference for this section is *A Paradox of Newtonian Gravitation and Laplace's Solution* [36] by [Amitabha Ghosh](#) [37] and Ujjal Dey.

Consider a test mass m at position (x, y, z) inside an infinitely large medium (ipse est Cosmos) with mean density ρ_c and calculate the gravitational force $\vec{F}$ upon that test mass with Newton's third law, where G is the [Gravitational constant](#) [38].

$$\vec{F}(x, y, z) = G \cdot m \iiint \begin{bmatrix} x - \xi \\ y - \eta \\ z - \zeta \end{bmatrix} \frac{\rho_c d\xi d\eta d\zeta}{[(x - \xi)^2 + (y - \eta)^2 + (z - \zeta)^2]^{3/2}}$$

Introducing a [Spherical coordinate system](#) [39]:

$$\begin{cases} \xi = r \sin(\theta) \cos(\phi) \\ \eta = r \sin(\theta) \sin(\phi) \\ \zeta = r \cos(\theta) \end{cases} \quad \text{where } 0 \leq \theta \leq \pi \quad \text{and} \quad 0 \leq \phi \leq 2\pi$$

Because of the expected spherical symmetry of the problem, we only have to consider a ray in the z direction, which means that $x = 0$, $y = 0$. Also put $z = R$, then we have:

$$d\xi d\eta d\zeta = r^2 dr \sin(\theta) d\theta d\phi$$

$$(x - \xi)^2 + (y - \eta)^2 + (z - \zeta)^2 = \xi^2 + \eta^2 + \zeta^2 - 2z\zeta + z^2 = r^2 - 2rR \cos(\theta) + R^2$$

The integral then becomes, after suitable rearrangement:

$$F(R) = G \cdot m \cdot \rho_c \int_0^{2\pi} d\phi \int_0^\infty r^2 dr \int_0^\pi \frac{[R - r \cos(\theta)] \sin(\theta) d\theta}{[r^2 - 2rR \cos(\theta) + R^2]^{3/2}}$$

Substitute $y = \cos(\theta)$ and find that $dy = -\sin(\theta) d\theta$. Replace y by $(-y)$.

$$F(R) = -G \cdot m \cdot \rho_c \cdot 2\pi \int_0^\infty r^2 dr \int_{+1}^{-1} \frac{R - ry}{(r^2 - 2ryR + R^2)^{3/2}} dy$$

$$F(R) = G \cdot m \cdot \rho_c \cdot 2\pi \int_0^\infty r^2 \left[\int_{-1}^{+1} \frac{R + ry}{(R^2 + r^2 + 2ryR)^{3/2}} dy \right] dr$$

At last, substitute $x = r/R$ to get

$$F(R) = 2\pi G \rho_c R m \int_0^\infty x^2 \left[\int_{-1}^{+1} \frac{xy + 1}{(1 + x^2 + 2xy)^{3/2}} dy \right] dx \quad (3)$$

It should be noticed for later use that the *distance* between the test mass and an infinitesimal element in space $= R\sqrt{1+x^2+2xy}$. Now calculate the inner integral, the one between square brackets.

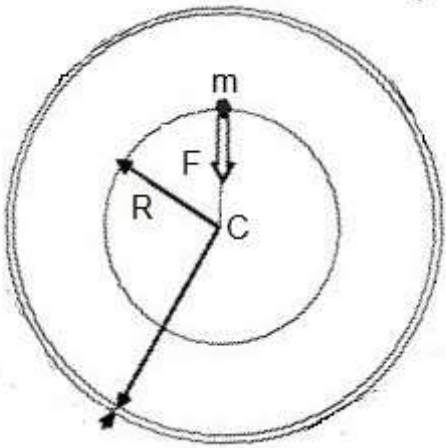
```
int((x*y+1)/(1+x^2+2*x*y)^(3/2),y=-1..1);
latex(%);
```

The first line by [MAPLE](#) [40], the rest by hand. The outcome is a (Heaviside) step function.

$$\begin{aligned}
& - \frac{-\sqrt{(x-1)^2}x - \sqrt{(x-1)^2} + \sqrt{(x+1)^2}x - \sqrt{(x+1)^2}}{\sqrt{(x+1)^2}\sqrt{(x-1)^2}} \\
& = - \left[-\frac{x}{|x+1|} - \frac{1}{|x+1|} + \frac{x}{|x-1|} - \frac{1}{|x-1|} \right] = \frac{x+1}{|x+1|} - \frac{x-1}{|x-1|} = 1 - \frac{x-1}{|x-1|} \\
& \Rightarrow \int_{-1}^{+1} \frac{xy+1}{(1+x^2+2xy)^{3/2}} dy = \begin{cases} 2 & \text{for } x \leq 1 \\ 0 & \text{for } x \geq 1 \end{cases}
\end{aligned}$$

It follows that

$$F(R) = 2\pi G \rho_c R m \left[\int_0^1 2x^2 dx + \int_1^\infty 0x^2 dx \right] = \frac{4}{3} \pi G \rho_c R m$$



The *Paradox of Newtonian Gravitation* is in the fact that, according to the above calculations, any test mass m anywhere in the universe is being attracted (with a force F) towards the center C of a (spherical) coordinate system, which is also an arbitrary point in the universe. The paradox can be derived in a much simpler way by employing two well known results in gravity theory. Both are a consequence of Newton's [Shell theorem](#) [41]. The first result is that the force upon a test mass *inside* a hollow sphere is *exactly zero*. The second result is that the force upon a test mass *outside* a massive sphere is the same as the force towards a point at the center of the sphere with the total mass of the sphere concentrated in it. Therefore the total force is simply $F = G m(\rho_c \cdot 4/3\pi R^3)/R^2 = 4/3 \pi G \rho_c R m$, quite in concordance with the more elaborate theory.

7. Solution by Simeon Albert

How can the *Paradox of Newtonian Gravitation* be resolved? The approach as has been employed by [Pierre-Simon Laplace](#) [42] is to modify Newton's third law according to formula (2) in [reference](#) [36].

$$F = G \frac{m_1 m_2}{r^2} \exp(-\Gamma r) \quad (4)$$

Let us translate this into our integral (3). Remember that $r = R\sqrt{1+x^2+2xy}$ in there and abbreviate $\Gamma R = \alpha$.

$$F(R) = 2\pi G \rho_c R m \int_0^\infty x^2 \left[\int_{-1}^{+1} \frac{e^{-\alpha\sqrt{1+x^2+2xy}}(xy+1)}{(1+x^2+2xy)^{3/2}} dy \right] dx$$

Where $\alpha = \Gamma R$ is a dimensionless quantity, still dependent on the place of the test mass in the universe with respect to some origin.

In order to resolve for the paradox, the integral must be zero. The authors of the key reference have presented

numerical evidence, but they have not been able to prove this analytically. However, by employing the power of our favorite computer algebra system [8] - *Brain off, computer on!* - we find a straightforward shortcut to the proof that $F(R) = 0$.

```
g(x,alpha) := int(exp(-alpha*sqrt(1+x^2+2*x*y))*(x*y+1)/(1+x^2+2*x*y)^(3/2),y=-1..1);
F := int(g(x,alpha)*x^2,x=0..infinity);
simplify(%,assume=positive);
```

0

The problem has become the subject of a posting at the Mathematics Stack Exchange forum (MSE for short): [Prove or disprove the equality of these two integrals](#) [43]. And indeed there is an analytical solution. Even better, it's entirely by hand: *Brain on, computer off!* The gravitational force on a test mass in a universe with uniform density is zero everywhere. However, this is only the case with "assume=positive". The paradox pops up again as soon as α is exactly zero. We can see that, at a positive infinitesimal distance from $\alpha = 0$, the integral suddenly changes from $2/3$ to 0. *Thus $\alpha = 0$ or $\alpha > 0$ makes a hell of a difference !!*

Why are we so motivated by this problem? Once more, take a look at equation (2) in the key [paper](#) [36]. Our version of the Variable Mass Theory comes in with a twist on Laplace's modification of the law of gravitation. It's reasonable to assume that the test mass m is located near us, here and now. If the other infinitesimal masses $dM = \rho_c dV$ (V = volume) in the universe are present at large distances r from us, as is usually the case with cosmology, then we are looking backwards in the past ($-t > 0$) and the corresponding variable masses have been smaller at that time, according to the formulas (1) and (2) in our above section 5. ($d \rightarrow r$ renamed):

$$r = \frac{c}{H} \ln(1+z) = \frac{c}{H} \ln\left(\frac{dM_0}{dM}\right) \iff dM = dM_0 e^{-H/c \cdot r} \quad (5)$$

where H = (intrinsic) Hubble parameter and c = speed of light in empty space. Variable Mass leads to an equivalent of Laplace's modification (4) of the law of gravitation:

$$dF = G \frac{m dM}{r^2} = G \frac{m dM_0}{r^2} e^{-H/c \cdot r} \quad (6)$$

It is easily seen now that Laplace's factor must be

$$\exp(-\Gamma \cdot r) = \exp(-H/c \cdot r) \implies \Gamma = \frac{H}{c} \quad (7)$$

If we take $H = H_0$ equal to a common value for the "cosmic" Hubble parameter for Cepheids, then Pierre-Simon's constant can be calculated.

```
# 1 megaParsec
Mpc := 3.08567758*10^22;
# Hubble parameter (2022-02-08)
H := 73.4*1000/Mpc;
# Speed of light
c := 299792458;
# Gamma
H/c;
```

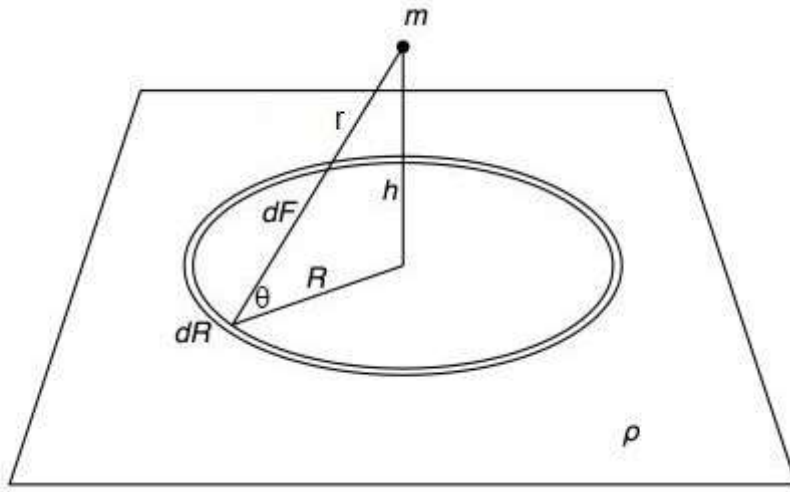
-26
0.7934595873 10

It turns out to be very small indeed, approximately $8 \times 10^{-27} m^{-1}$. Compare with Laplace's own estimate as mentioned in [36]: $\Gamma < 7 \times 10^{-18} m^{-1}$.

Note. The initials L.M. in the name of the author of the awarded answer in [43] stand for [Louis Marmet](#) [44].

8. Seeliger's Paradox

Key reference for this section is [Seeliger's Gravitational Paradox and the Infinite Universe](#) [45] by Leonardo Sarasúa. Fig. 1 is copied from the paper as it is.



F = force, G = [gravitational constant](#), m = test mass, R = radius, h = height, $r = \sqrt{R^2 + h^2}$ = distance. The 2-D treatment in the paper will be used as a template for generalization to 3-D. The surface mass density ρ = will be replaced by ρ_c = volumetric mass density of cosmos. The 2-D plane in the above picture has thickness zero. For our generalization to 3-D it must be dh instead. Giving a slightly but essentially different expression for the infinitesimal vertical component dF of the force on the particle with mass m as it is attracted by the plane, which has become a plate now.

$$dF = \frac{G m (\rho_c 2\pi R dR dh)}{(\sqrt{R^2 + h^2})^2} \frac{h}{\sqrt{R^2 + h^2}} = 2\pi G m \rho_c h dh \frac{R dR}{(R^2 + h^2)^{3/2}}$$

The total force experienced by the test mass from all of the mass *below* it is

$$F = 2\pi G m \rho_c \int_0^\infty h \left[\int_0^\infty \frac{R dR}{(R^2 + h^2)^{3/2}} \right] dh$$

The integral between square brackets is, with $x = R/h$ and $u = x^2 + 1$:

$$\int_0^\infty \frac{R dR}{(R^2 + h^2)^{3/2}} = \frac{h^2}{h^3} \frac{1}{2} \int_{x=0}^\infty \frac{d(x^2 + 1)}{(x^2 + 1)^{3/2}} = \frac{1}{h} \frac{1}{2} (-2) \left[\frac{1}{\sqrt{u}} \right]_1^\infty = \frac{1}{h}$$

Giving for the total force as experienced by our test mass an infinite outcome.

$$F = 2\pi G m \rho_c \int_0^\infty h \cdot \frac{1}{h} dh = \infty$$

Minus another infinite outcome if the mass of the universe at the other side (above it) is taken into account. Therefore *the total force can be anything*. Which is contrary to experience.

However, let's now introduce the panacea as proposed by Laplace and [Seeliger](#) [47] and observe what happens.

$$F = 2\pi G m \rho_c \int_{-\infty}^{+\infty} h \left[\int_0^\infty \frac{e^{-\Gamma \sqrt{R^2 + h^2}} R dR}{(R^2 + h^2)^{3/2}} \right] dh$$

With $\therefore$ -(brainless)-: help of [MAPLE](#) [39] we see that the outcome is zero again, as desired and required. Physical truth should not depend upon the way you look at it.

```
h*int(R*exp(-Gamma*sqrt(R^2+h^2))/(R^2+h^2)^(3/2),R=0..infinity);
f(h) := simplify(%,assume=positive);
int(f(h),h=-infinity..infinity);
```

It must be possible again to do this with *Brain on*, computer off. Define I as the above integral:

$$I = \int_{-\infty}^{+\infty} h \left[\int_0^{\infty} \frac{e^{-\Gamma \sqrt{R^2+h^2}} R dR}{(R^2 + h^2)^{3/2}} \right] dh$$

$$u = \sqrt{R^2 + h^2} \quad ; \quad v = \frac{h}{\sqrt{R^2 + h^2}} \quad ; \quad h = uv \quad ; \quad du dv = \frac{\partial(u, v)}{\partial(R, h)} dR dh = |J| dR dh$$

From the picture we see that $u = r$ and $v = \sin(\theta)$, giving the integration bounds $0 \leq u < \infty$ and $-1 \leq v \leq +1$.

$$|J| = \begin{vmatrix} \partial u / \partial R & \partial u / \partial h \\ \partial v / \partial R & \partial v / \partial h \end{vmatrix} = \begin{vmatrix} R / \sqrt{R^2 + h^2} & h / \sqrt{R^2 + h^2} \\ -Rh / (R^2 + h^2)^{3/2} & 1 / \sqrt{R^2 + h^2} - h^2 / (R^2 + h^2)^{3/2} \end{vmatrix} = \frac{R}{R^2 + h^2}$$

$$u^2 = R^2 + h^2 \implies R^2 = u^2 - h^2 = u^2(1 - v^2) \implies R = u\sqrt{1 - v^2} \implies |J| = \frac{\sqrt{1 - v^2}}{u}$$

$$I = \iint uv \cdot \frac{e^{-\Gamma u} u \sqrt{1 - v^2}}{u^3} \left(\frac{u}{\sqrt{1 - v^2}} \right) du dv = \int_0^{\infty} e^{-\Gamma u} du \cdot \int_{-1}^{+1} v dv$$

$$\implies F = 2\pi G m \rho_c \int_0^{\infty} e^{-\Gamma u} du \cdot \int_{-1}^{+1} v dv = 0 \quad (8)$$

because

$$\int_0^{\infty} e^{-\Gamma u} du = -\frac{1}{\Gamma} [e^{-\Gamma u}]_{u=0}^{\infty} = \frac{1}{\Gamma} \quad \times \quad \int_{-1}^{+1} v dv = \frac{1}{2} \left[\frac{v^2}{2} \right]_{v=-1}^{+1} = 0$$

The physical meaning of $1/\Gamma = c/H$ is the speed of light in vacuum times a Hubble time. Which in some circles is called the *size of the [Observable universe](#)* [46].

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