

计算铝棒的电阻率

$$\begin{aligned}\overline{R_3} &= \frac{1}{4}(R_{3\text{上}} + R_{3\text{下}} + R'_{3\text{上}} + R'_{3\text{下}}) \\ &= \frac{1}{4}(11.45 + 12.46 + 12.42 + 11.47) \\ &= 11.95\Omega,\end{aligned}$$

$$\begin{aligned}\overline{d} &= \frac{1}{5}\sum d \\ &= \frac{1}{5}(4.035 + 4.031 + 4.043 + 4.038 + 4.033) \\ &= 4.036\text{mm},\end{aligned}$$

$$\begin{aligned}\overline{R_x} &= \frac{R_N}{R_1}\overline{R_3} \\ &= \frac{0.01}{10^2}11.95 \\ &= 1.195 * 10^{-3}\Omega,\end{aligned}$$

$$\begin{aligned}\overline{\rho} &= \frac{\pi \overline{d}^2}{4l}\overline{R_x} \\ &= \frac{3.1416 * 4.036^2}{4 * 400.0}1.195 * 10^{-3} \\ &= 3.822 * 10^{-5}\Omega \cdot \text{mm}.\end{aligned}$$

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$$\begin{aligned}
\overline{R_3} &= \frac{1}{4}(R_{3\text{上}} + R_{3\text{下}} + R'_{3\text{上}} + R'_{3\text{下}}) \\
&= \frac{1}{4}(22.43 + 23.44 + 23.45 + 22.48) \\
&= 22.95\Omega, \\
\overline{d} &= \frac{1}{5} \sum d \\
&= \frac{1}{5}(3.973 + 3.978 + 3.976 + 3.975 + 3.978) \\
&= 3.976\text{mm}, \\
\overline{R_x} &= \frac{R_N}{R_1} \overline{R_3} \\
&= \frac{0.01}{10^2} 22.95 \\
&= 2.295 * 10^{-3} \Omega, \\
\overline{\rho} &= \frac{\pi \overline{d}^2}{4l} \overline{R_x} \\
&= \frac{3.1416 * 3.976^2}{4 * 400.0} 2.295 * 10^{-3} \\
&= 8.513 * 10^{-5} \Omega \cdot \text{mm}.
\end{aligned}$$

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$$\begin{aligned}
\overline{R_3} &= \frac{1}{4}(R_{3上} + R_{3下} + R'_{3上} + R'_{3下}) \\
&= \frac{1}{4}(42.77 + 43.83 + 44.11 + 42.85) \\
&= 43.39\Omega, \\
\overline{d} &= \frac{1}{5} \sum d \\
&= \frac{1}{5}(3.995 + 3.996 + 3.989 + 3.994 + 3.991) \\
&= 3.993\text{mm}, \\
\overline{R_x} &= \frac{R_N}{R_1} \overline{R_3} \\
&= \frac{0.01}{10^2} 43.39 \\
&= 4.339 * 10^{-3} \Omega, \\
\overline{\rho} &= \frac{\pi \overline{d}^2}{4l} \overline{R_x} \\
&= \frac{3.1416 * 3.993^2}{4 * 400.0} 4.339 * 10^{-3} \\
&= 1.623 * 10^{-4} \Omega \cdot \text{mm}.
\end{aligned}$$

计算铝棒电阻率的不确定度

$$\begin{aligned}
U_{\overline{R_3}} &= \frac{1}{4}(|R_{3上} - R_{3下}| + |R'_{3上} - R'_{3下}|) \\
&= \frac{1}{4}(|11.45 - 12.46| + |12.42 - 11.47|) \\
&= 1.96\Omega,
\end{aligned}$$

$$\begin{aligned}
U_{\overline{R_x}} &= \frac{R_N}{R_1} U_{\overline{R_3}} \\
&= \frac{0.01}{10^2} 1.96 \\
&= 1.96 * 10^{-4} \Omega.
\end{aligned}$$

$$\begin{aligned}
U_{\overline{d}} &= \sqrt{U_{dA}^2 + U_{dB}^2} \\
&= \sqrt{\frac{t_p^2}{4 * 5} \sum (\overline{d} - d)^2 + \left(\frac{0.01}{2 * 3}\right)^2} \\
&= \sqrt{1.14^2 + \left(\frac{0.01}{6}\right)^2}
\end{aligned}$$

$$= \sqrt{\frac{1}{4 * 5}(0.001^2 + 0.005^2 + 0.007^2 + 0.002^2 + 0.003^2) + \left(\frac{1}{2 * 3}\right)}$$

$$= 3 * 10^{-3} \text{mm.}$$

$$U_l = U_{lB}$$

$$= \frac{1}{2 * 3}$$

$$= 0.2 \text{mm.}$$

$$\ln \bar{\rho} = \ln \frac{\pi \bar{d}^2}{4l} \bar{R}_x$$

$$= 2 \ln \bar{d} + \ln \bar{R}_x - \ln l + \ln \pi - \ln 4,$$

$$\frac{U_{\bar{\rho}}}{\bar{\rho}} = \sqrt{\left(\frac{\partial \ln \bar{\rho}}{\partial \bar{d}} U_{\bar{d}}\right)^2 + \left(\frac{\partial \ln \bar{\rho}}{\partial \bar{R}_x} U_{\bar{R}_x}\right)^2 + \left(\frac{\partial \ln \bar{\rho}}{\partial l} U_l\right)^2}$$

$$\sqrt{4 \left(\frac{U_{\bar{d}}}{\bar{d}}\right)^2 + \left(\frac{U_{\bar{R}_x}}{\bar{R}_x}\right)^2 + \left(\frac{U_l}{l}\right)^2}$$

$$\sqrt{4 \left(\frac{3 * 10^{-3}}{4.036}\right)^2 + \left(\frac{1.96 * 10^{-4}}{1.195 * 10^{-3}}\right)^2 + \left(\frac{0.2}{400.0}\right)^2}$$

$$= 0.2,$$

$$U_{\bar{\rho}} = \frac{U_{\bar{\rho}}}{\bar{\rho}} \bar{\rho}$$

$$= 0.2 * 3.822 * 10^{-5}$$

$$= 8 * 10^{-6} \Omega \cdot \text{mm.}$$

$$\rho = \bar{\rho} \pm U_{\bar{\rho}}$$

$$= 3.822 * 10^{-5} \pm 8 * 10^{-6}$$

$$= (38 \pm 8) * 10^{-6} \Omega \cdot \text{mm.}$$