$$\sum_{k=1}^{n} \frac{1}{\sqrt{k^3}}$$

$$=1 + \sum_{k=2}^{n} \frac{1}{k\sqrt{k}}$$

$$\leq 1 + \sum_{k=2}^{n} \frac{1}{k\sqrt{k-1}}$$

$$=1 + \sum_{k=2}^{n} (\frac{2}{\sqrt{k-1}} - \frac{k-1+k}{k\sqrt{k-1}})$$

$$\leq 1 + \sum_{k=2}^{n} (\frac{2}{\sqrt{k-1}} - \frac{2\sqrt{(k-1)k}}{k\sqrt{k-1}})$$

$$=1 + \sum_{k=2}^{n} (\frac{2}{\sqrt{k-1}} - \frac{2}{\sqrt{k}})$$

$$\begin{aligned} & = 1 + (2 - \frac{2}{\sqrt{n}}) \\ & < 3 \\ & \pi = \frac{a}{b} \quad a \ b \in \mathbb{N}^* \\ & f(x) = \frac{x^n (a - bx)^n}{n!} = \frac{b^n x^n (\pi - x)^n}{n!} \\ & f(x) = f(\pi - x) \\ & \forall k \in \mathbb{N}^*. f^{(k)}(0) \in \mathbb{Z} \quad f^{(k)}(\pi) = (-1)^k f^{(k)}(0) \in \mathbb{Z} \\ & \int_0^\pi f(x) sin(x) \mathrm{d}x \\ & = -f(x) cos(x) \Big|_0^\pi + \int_0^\pi f(x) cos(x) \mathrm{d}x \\ & = -f(0) + f(\pi) + f^{(1)}(x) sinx \Big|_0^\pi - \int_0^\pi f^{(2)}(x) sinx \mathrm{d}x \\ & = f(0) + f(\pi) - f^{(2)}(0) - f^{(2)}(\pi) + \int_0^\pi f^{(4)}(x) sinx \mathrm{d}x \\ & = f(0) + f(\pi) - f^{(2)}(0) - f^{(2)}(\pi) + \dots + (-1)^n f^{(2n)}(0) + \\ & (-1)^n f^{(2n)}(\pi) \\ & \int_0^\pi f(x) sin(x) \mathrm{d}x \in \mathbb{Z} \\ & \forall x \in [0, \pi]. 0 \le a - bx = b(\pi - x) \le a \\ & 0 \le f(x) = \frac{x^n (a - bx)^n}{n!} \le \frac{\pi^n a^n}{n!} \\ & 0 \le \int_0^\pi f(x) sinx \mathrm{d}x \le \int_0^\pi f(x) \mathrm{d}x \le \int_0^\pi \frac{\pi^n a^n}{n!} \mathrm{d}x = \frac{\pi^{n+1} a^n}{n!} \\ & \lim_{n \to \infty} \frac{\pi^{n+1} a^n}{n!} = 0 \\ & \lim_{n \to \infty} \frac{\pi^{n+1} a^n}{n!} = 0 \end{aligned}$$

$$n \in \mathbb{A} := (n \in \mathbb{N}^*) \wedge ((\neg(\exists t \in \mathbb{N}^*)) \to (t^2 = n))$$

$$n \in \mathbb{A} \to \sqrt{n} \in \mathbb{R} \setminus \mathbb{Q}$$

$$\sqrt{n} \in \mathbb{Q} \to \sqrt{n} = \frac{p}{q} \to p^2 = nq^2 \quad (Bezout's \ theorem)$$

$$\exists a \ b \in \mathbb{Z} \to ap + bq = 1$$

$$p = ap^2 + bpq = anq^2 + bpq = (anq + bp)q \to$$

$$\sqrt{n} = \frac{p}{q} = anq + bp \in \mathbb{N}^*$$

$$\int_0^{114514} \sqrt{x} dx = \frac{2x\sqrt{x}}{3} \Big|_0^{114514} = \frac{229028\sqrt{114514}}{3}$$

$$\int_0^1 \frac{1}{1+x^2} dx = \frac{\pi}{4}$$

 $5756349734494395196560705630345427186932793468472838716428096645500052134940586805698371580218613033\\3624025889014715365627577902394355374303315284508158622522727342918209611955245175385641879880549342\\4427643522361203671329599098374955467430836156332977517026730342006960242381054148188573825706807656\\0061847078270714002631368920793647928160220157729558501176777764256227842068154452922197974697536488\\4230398476795902584183477291343182100904222561750961264546022025338093446438589338145839130891466480\\1870096470791240536332400558490260214426235708942756154183031379649304272706913433012568448875352331\\4167676547034782574962448479779084505179694165756237624013777931642165373213086208644135150782785237\\2395257626676278535128231837032526975023802535714142769361532472697007123419965704780892710518646662\\36634287446807022570656318619451740314610477452732311007/6$