

DILLA, KERVIN CLYDE S. CS 201

LOPE OF TANGENT LINE

$$\frac{dy}{dx} = \frac{f(x+h) - f(x)}{(x+h) - x} = \frac{dy}{dx} = \frac{f(x+h) - f(x)}{h} \text{ (as } h \text{ goes to 0)} \quad \frac{d}{dx}(c) = 0$$

$$\begin{aligned} \frac{dy}{dx} &= \frac{f(x+h) - f(x)}{h} \\ \frac{dy}{dx} &= \frac{((x+h)^2) - (x^2)}{h} \\ \frac{dy}{dx} &= \frac{(x^2 + 2xh + h^2) - x^2}{h} \end{aligned}$$

$$\begin{aligned} \frac{dy}{dx} &= \frac{2xh + h^2}{h} \\ \frac{dy}{dx} &= 2x + h \\ \frac{dy}{dx} &= 2x \end{aligned}$$

POWER RULE

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

CONSTANT MULTIPLE

$$\frac{d}{dx}(c \cdot u) = c \frac{du}{dx}$$

SUM RULE

$$\frac{d}{dx}(u+v) = \frac{du}{dx} + \frac{dv}{dx}$$

DIFFERENCE RULE

$$\frac{d}{dx}(u-v) = \frac{du}{dx} - \frac{dv}{dx}$$

CHAIN RULE

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$$

SHORT METHOD

$$y = g(f(x)), \quad \frac{dy}{dx} = g'(f(x)) \times f'(x)$$

$$y = (f(x))^n, \quad \frac{dy}{dx} = n(f(x))^{n-1} \times f'(x)$$

FUNCTIONS OF THE FORM $e^{f(x)}$

$$y = e^x, \quad \frac{dy}{dx} = e^x$$

$$y = ke^x, \quad \frac{dy}{dx} = ke^x$$

$$y = e^{kx}, \quad \frac{dy}{dx} = ke^{kx}$$

$$y = e^{f(x)}, \quad \frac{dy}{dx} = f'(x)e^{f(x)}$$

NOTATIONS

$f'(x)$ > prime
 y'

$\frac{dy}{dx}$ derivative of y with respect to x (NOUN)

$\frac{d}{dx}$ take derivative with respect to x (VERB)

TRIGONOMETRY

$$\frac{d}{dx} \sin x = \cos x$$

$$\frac{d}{dx} \cos x = -\sin x$$

$$\frac{d}{dx} \tan x = \sec^2 x$$

$$\frac{d}{dx} \cot x = -\csc^2 x$$

$$\frac{d}{dx} \sec x = \sec x (\tan x)$$

$$\frac{d}{dx} \csc x = -\csc x (\cot x)$$

PRODUCT RULE

$$\frac{d}{dx}(uv) = u \frac{dv}{dx} + v \frac{du}{dx}$$

QUOTIENT RULE

$$\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

IDENTITIES

$$\tan = \sin / \cos \quad \cot = 1 / \tan = \cos / \sin$$

$$\sec = 1 / \cos \quad \csc = 1 / \sin$$