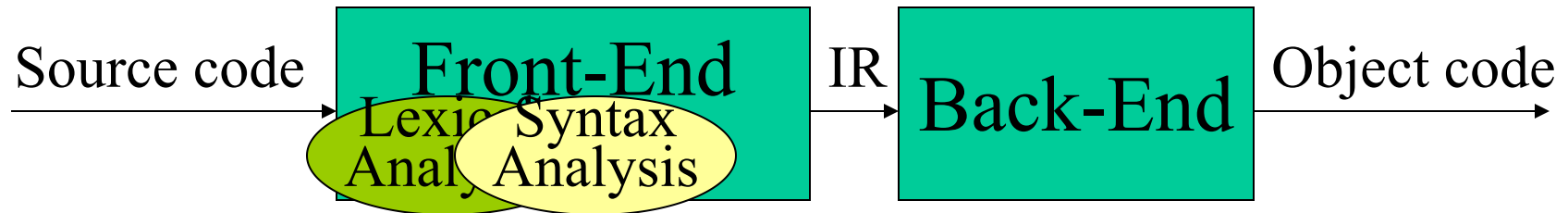


# Lecture 9: Bottom-Up Parsing



(from last lecture) Top-Down Parsing:

- Start at the root of the tree and grow towards leaves.
- Pick a production and try to match the input.
- We may need to backtrack if a bad choice is made.
- Some grammars are backtrack-free (predictive parsing).

Today's lecture:

Bottom-Up parsing

# Bottom-Up Parsing: What is it all about?

**Goal**: Given a grammar,  $G$ , construct a parse tree for a string (i.e., sentence) by starting at the leaves and working to the root (i.e., by working from the input sentence back toward the start symbol  $S$ ).

**Recall**: the point of parsing is to construct a derivation:

$$S \Rightarrow \delta_0 \Rightarrow \delta_1 \Rightarrow \delta_2 \Rightarrow \dots \Rightarrow \delta_{n-1} \Rightarrow \text{sentence}$$

To derive  $\delta_{i-1}$  from  $\delta_i$ , we match some *rhs*  $b$  in  $\delta_i$ , then replace  $b$  with its corresponding *lhs*,  $A$ . This is called a **reduction** (it assumes  $A \rightarrow b$ ).

The **parse tree** is the result of the **tokens** and the **reductions**.

**Example**: Consider the grammar below and the input string **abbcd**e.

1.     **Goal**  $\rightarrow$  **aABe**
2.             **A**  $\rightarrow$  **Abc**
3.                 **|b**
4.             **B**  $\rightarrow$  **d**

Sentential Form	Production	Position
abbcd	3	2
a A bcde	2	4
a A de	4	3
a A B e	1	4
Goal	-	-

# Finding Reductions

- What are we trying to find?
  - A substring  $b$  that matches the right-side of a production that occurs as one step in the rightmost derivation. Informally, this substring is called a **handle**.
- Formally, a handle of a right-sentential form  $\delta$  is a pair  $\langle A \rightarrow b, k \rangle$  where  $A \rightarrow b \in P$  and  $k$  is the position in  $\delta$  of  $b$ 's rightmost symbol.  
*(right-sentential form: a sentential form that occurs in some rightmost derivation).*
  - Because  $\delta$  is a right-sentential form, the substring to the right of a handle contains only terminal symbols. Therefore, the parser doesn't need to scan past the handle.
  - If a grammar is unambiguous, then every right-sentential form has a unique handle (sketch of proof by definition: if unambiguous then rightmost derivation is unique; then there is unique production at each step to produce a sentential form; then there is a unique position at which the rule is applied; hence, unique handle).

**If we can find those handles, we can build a derivation!**

# Motivating Example

Given the grammar of the left-hand side below, find a rightmost derivation for  $x - 2*y$  (starting from Goal there is only one, the grammar is not ambiguous!). In each step, identify the handle.

1.  $Goal \rightarrow Expr$
2.  $Expr \rightarrow Expr + Term$
3.     |  $Expr - Term$
4.     |  $Term$
5.  $Term \rightarrow Term * Factor$
6.     |  $Term / Factor$
7.     |  $Factor$
8.  $Factor \rightarrow number$
9.     |  $id$

Production	Sentential Form	Handle
-	<i>Goal</i>	-
1	<i>Expr</i>	1,1
3	<i>Expr - Term</i>	3,3

Problem: given the sentence  $x - 2*y$ , find the handles!

# A basic bottom-up parser

- The process of discovering a handle is called handle pruning.
- To construct a rightmost derivation, apply the simple algorithm:
  - for**  $i=n$  to  $1$ , step  $-1$ 
    - find** the handle  $\langle A \rightarrow b, k \rangle_i$  in  $\delta_i$
    - replace**  $b$  with  $A$  to generate  $\delta_{i-1}$
  - (needs  $2n$  steps, where  $n$  is the length of the derivation)*
- One implementation is based on using a stack to hold grammar symbols and an input buffer to hold the string to be parsed. Four operations apply:
  - **shift**: next input is shifted (pushed) onto the top of the stack
  - **reduce**: right-end of the handle is on the top of the stack; locate left-end of the handle within the stack; pop handle off stack and push appropriate non-terminal left-hand-side symbol.
  - **accept**: terminate parsing and signal success.
  - **error**: call an error recovery routine.

# Implementing a shift-reduce parser

**push** \$ onto the stack

token = next\_token()

**repeat**

**if** the top of the stack is a handle  $A \rightarrow b$

**then** /\* reduce  $b$  to  $A$  \*/

            pop the symbols of  $b$  off the stack

            push  $A$  onto the stack

**elseif** (token != eof) /\* eof: end-of-file = end-of-input \*/

**then** /\* shift \*/

            push token

            token=next\_token()

**else** /\* error \*/

        call error\_handling()

**until** (top\_of\_stack == *Goal* && token==eof)

*Errors show up: a) when we fail to find a handle, or b) when we hit EOF and we need to shift. The parser needs to recognise syntax errors.*

# Example: $x-2*y$

Stack	Input	Handle	Action	
\$	id – num * id	None	Shift	
\$ id	– num * id	9,1	Reduce 9	
\$ Factor	– num * id	7,1	Reduce 7	
\$ Term	– num * id	4,1	Reduce 4	
<b>\$ Expr</b>	<b>– num * id</b>	<b>None</b>	<b>Shift</b>	<b>!!</b>
\$ Expr –	num * id	None	Shift	
\$ Expr – num	* id	8,3	Reduce 8	
\$ Expr – Factor	* id	7,3	Reduce 7	
<b>\$ Expr – Term</b>	<b>* id</b>	<b>None</b>	<b>Shift</b>	<b>!!</b>
\$ Expr – Term *	id	None	Shift	
\$ Expr – Term * id		9,5	Reduce 9	
\$ Expr – Term * Factor		5,5	Reduce 5	
\$ Expr – Term		3,3	Reduce 3	
\$ Expr		1,1	Reduce 1	
\$ Goal		none	Accept	

- 1. Shift until top of stack is the right end of the handle
  - 2. Find the left end of the handle and reduce
- (5 shifts, 9 reduces, 1 accept)

# What can go wrong?

(think about the steps with an exclamation mark in the previous slide)

- **Shift/reduce conflicts**: the parser cannot decide whether to shift or to reduce.

Example: the dangling-else grammar; usually due to ambiguous grammars.

Solution: a) modify the grammar; b) resolve in favour of a shift.

- **Reduce/reduce conflicts**: the parser cannot decide which of several reductions to make.

Example: `id(id, id);` reduction is dependent on whether the first `id` refers to array or function.

May be difficult to tackle.

*Key to efficient bottom-up parsing: the handle-finding mechanism.*



# LR(1) grammars

*(a beautiful example of applying theory to solve a complex problem in practice)*

A grammar is LR(1) if, given a rightmost derivation, we can (I) isolate the handle of each right-sentential form, and (II) determine the production by which to reduce, by scanning the sentential form from left-to-right, going at most 1 symbol beyond the right-end of the handle.

- LR(1) grammars are widely used to construct (automatically) efficient and flexible parsers:
  - Virtually all context-free programming language constructs can be expressed in an LR(1) form.
  - LR grammars are the most general grammars parsable by a non-backtracking, shift-reduce parser (deterministic CFGs).
  - Parsers can be implemented in time proportional to tokens+reductions.
  - LR parsers detect an error as soon as possible in a left-to-right scan of the input.

L stands for left-to-right scanning of the input; R for constructing a rightmost derivation in reverse; 1 for the number of input symbols for lookahead.

# LR Parsing: Background

- Read tokens from an input buffer (same as with shift-reduce parsers)
- Add an extra state information after each symbol in the stack. The state summarises the information contained in the stack below it. The stack would look like:

$\$ S_0 \textit{Expr} S_1 - S_2 \textit{num} S_3$

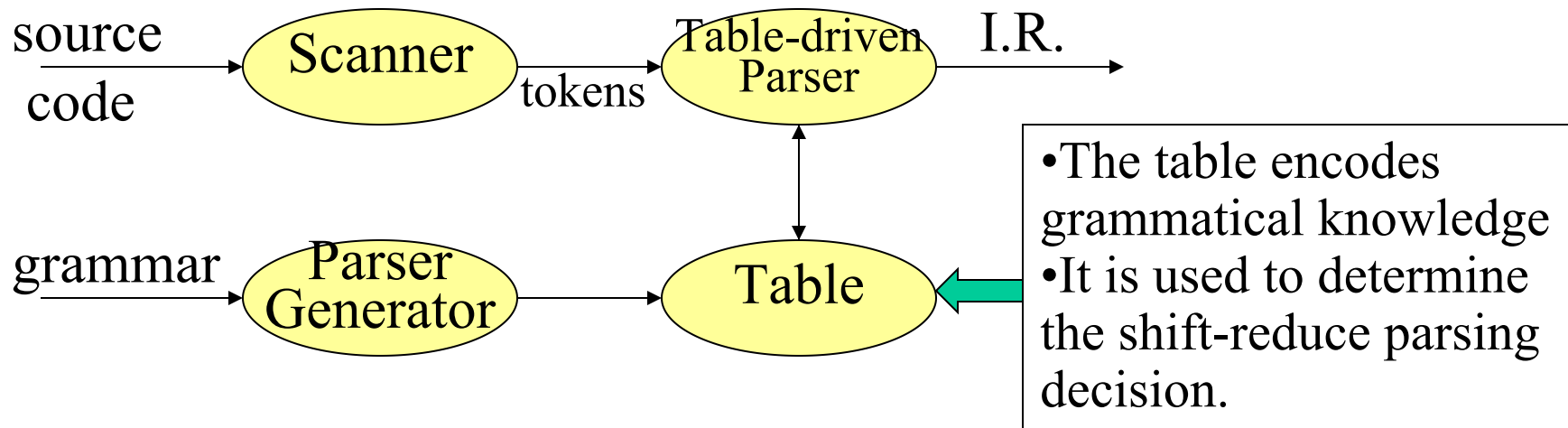
- Use a table that consists of two parts:
  - **action**[state\_on\_top\_of\_stack, input\_symbol]: returns one of: shift s (push a symbol and a state); reduce by a rule; accept; error.
  - **goto**[state\_on\_top\_of\_stack, non\_terminal\_symbol]: returns a new state to push onto the stack after a reduction.

# Skeleton code for an LR Parser

```
Push $ onto the stack
push s0
token=next_token()
repeat
    s=top_of_the_stack /* not pop! */
    if ACTION[s,token]==`reduce A→b'
        then pop 2*(symbols_of b) off the stack
            s=top_of_the_stack /* not pop! */
            push A; push GOTO[s,A]
    elseif ACTION[s,token]==`shift sx'
        then push token; push sx
            token=next_token()
    elseif ACTION[s,token]==`accept'
        then break
    else report_error
end repeat
report_success
```

# The Big Picture: Prelude to what follows

- LR(1) parsers are table-driven, shift-reduce parsers that use a limited right context for handle recognition.
- They can be built by hand; perfect to automate too!
- Summary: Bottom-up parsing is more powerful!



Next: we will automate table construction!

Reading: Aho2 Section 4.5; Aho1 pp.195-202; Hunter pp.100-103;  
Grune pp.150-152

# Example

Consider the following grammar and tables:

1.  $Goal \rightarrow CatNoise$
2.  $CatNoise \rightarrow CatNoise\ miau$
3.  $\quad\quad\quad | \quad miau$

STATE	ACTION		GOTO
	eof	miau	CatNoise
0	-	Shift 2	1
1	accept	Shift 3	
2	Reduce 3	Reduce 3	
3	Reduce 2	Reduce 2	

**Example 1:** (input string miau)

Stack	Input	Action
\$ s0	miau eof	Shift 2
\$ s0 miau s2	eof	Reduce 3
\$ s0 CatNoise s1	eof	Accept

*Note that there cannot be a syntax error with CatNoise, because it has only 1 terminal symbol. “miau woof” is a lexical problem, not a syntax error!*

**Example 2:** (input string miau miau)

Stack	Input	Action
\$ s0	miau miau eof	Shift 2
\$ s0 miau s2	miau eof	Reduce 3
\$ s0 CatNoise s1	miau eof	Shift 3
\$ s0 CatNoise s1 miau s3	eof	Reduce 2
\$ s0 CatNoise s1	eof	accept

eof is a convention for end-of-file (=end of input)

# Example: the expression grammar (slide 4)

1.  $Goal \rightarrow Expr$
2.  $Expr \rightarrow Expr + Term$
3.       |  $Expr - Term$
4.       |  $Term$
5.  $Term \rightarrow Term * Factor$
6.       |  $Term / Factor$
7.       |  $Factor$
8.  $Factor \rightarrow number$
9.       |  $id$

STATE	ACTION							GOTO		
	eof	+	-	*	/	num	id	Expr	Term	Factor
0						S 4	S 5	1	2	3
1	Acc	S 6	S 7							
2	R 4	R 4	R 4	S 8	S 9					
3	R 7	R 7	R 7	R 7	R 7					
4	R 8	R 8	R 8	R 8	R 8					
5	R 9	R 9	R 9	R 9	R 9					
6						S 4	S 5		10	3
7						S 4	S 5		11	3
8						S 4	S 5			12
9						S 4	S 5			13
10	R 2	R 2	R 2	S 8	S 9					
11	R 3	R 3	R 3	S 8	S 9					
12	R 5	R 5	R 5	R 5	R 5					
13	R 6	R 6	R 6	R 6	R 6					

*Apply the algorithm in slide 3 to the expression  $x-2*y$*   
*The result is the rightmost derivation (as in Lect.8, slide 7), but ...*  
*... no conflicts now: state information makes it fully deterministic!*

1. <i>Goal</i> $\rightarrow$ <i>Expr</i> 2. <i>Expr</i> $\rightarrow$ <i>Expr</i> + <i>Term</i> 3.             <i>Expr</i> − <i>Term</i> 4.             <i>Term</i> 5. <i>Term</i> $\rightarrow$ <i>Term</i> * <i>Factor</i> 6.             <i>Term</i> / <i>Factor</i> 7.             <i>Factor</i> 8. <i>Factor</i> $\rightarrow$ <i>number</i> 9.             <i>id</i>	STA TE	ACTION						GOTO			
		eof	+	−	*	/	num	id	Expr	Term	Factor
	0						S 4	S 5	1	2	3
	1	Acc	S 6	S 7							
	2	R 4	R 4	R 4	S 8	S 9					
	3	R 7	R 7	R 7	R 7	R 7					
	4	R 8	R 8	R 8	R 8	R 8					
	5	R 9	R 9	R 9	R 9	R 9					
	6						S 4	S 5		10	3
	7						S 4	S 5		11	3
	8						S 4	S 5			12
	9						S 4	S 5			13
	10	R 2	R 2	R 2	S 8	S 9					
	11	R 3	R 3	R 3	S 8	S 9					
	12	R 5	R 5	R 5	R 5	R 5					
	13	R 6	R 6	R 6	R 6	R 6					

Stack	Input	Action
\$s0	x-2*y	Shift 5
\$s0 x s5	- 2*y	Reduce 9
\$s0 Factor s3	- 2*y	Reduce 7
\$s0 Term s2	- 2*y	Reduce 4
\$s0 Expr s1	- 2*y	Shift 7
\$s0 Expr s1 - s7	2*y	Shift 4
\$s0 Expr s1 - s7 2 s4	*y	Reduce 8
\$s0 Expr s1 - s7 Factor s3	*y	Reduce 7
\$s0 Expr s1 - s7 Term s11	*y	Shift 8
\$s0 Expr s1 - s7 Term s11 * s8	y	Shift 5
\$s0 Expr s1 - s7 Term s11 * s8 y s5	EOF	Reduce 9
\$s0 Expr s1 - s7 Term s11 * s8 Factor s12	EOF	Reduce 5
\$s0 Expr s1 - s7 Term s11	EOF	Reduce 3
\$s0 Expr s1	EOF	accept

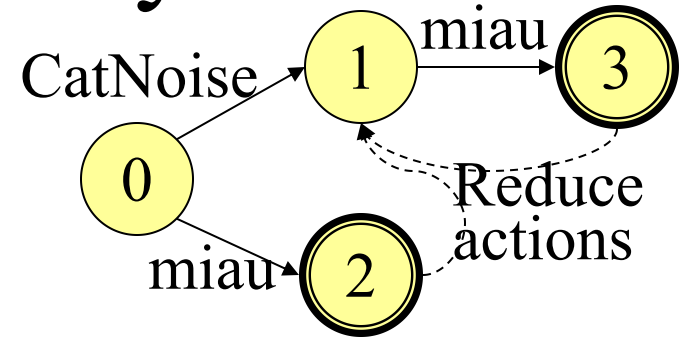
# Summary

- **Top-Down Recursive Descent**: Pros: Fast, Good locality, Simple, good error-handling. Cons: Hand-coded, high-maintenance.
- **LR(1)**: Pros: Fast, deterministic languages, automatable. Cons: large working sets, poor error messages.
- **What is left to study?**
  - Checking for context-sensitive properties
  - Laying out the abstractions for programs & procedures.
  - Generating code for the target machine.
  - Generating good code for the target machine.
- **Reading**: Aho2 Sections 4.7, 4.10; Aho1 pp.215-220 & 230-236; Cooper 3.4, 3.5; Grune pp.165-170; Hunter 5.1-5.5 (too general).



# LR(1) – Table Generation

# LR Parsers: How do they work?



- Key: language of handles is regular
  - build a handle-recognising DFA
  - Action and Goto tables encode the DFA
- How do we generate the Action and Goto tables?
  - Use the grammar to build a model of the DFA
  - Use the model to build Action and Goto tables
  - If construction succeeds, the grammar is LR(1).
- Three commonly used algorithms to build tables:
  - LR(1): full set of LR(1) grammars; large tables; slow, large construction.
  - SLR(1): smallest class of grammars; smallest tables; simple, fast construction.
  - LALR(1): intermediate sized set of grammars; smallest tables; very common.  
(Space used to be an obsession; now it is only a concern)

# LR(1) Items

- An LR(1) item is a pair  $[A, B]$ , where:
  - $A$  is a production  $\alpha \rightarrow \beta \gamma \delta$  with a  $\bullet$  at some position in the *rhs*.
  - $B$  is a lookahead symbol.
- The  $\bullet$  indicates the position of the top of the stack:
  - $[\alpha \rightarrow \beta \gamma \bullet \delta, a]$ : the input seen so far (ie, what is in the stack) is consistent with the use of  $\alpha \rightarrow \beta \gamma \delta$ , and the parser has recognised  $\beta \gamma$ .
  - $[\alpha \rightarrow \beta \gamma \delta \bullet, a]$ : the parser has seen  $\beta \gamma \delta$ , and a lookahead symbol of  $a$  is consistent with reducing to  $\alpha$ .
- The production  $\alpha \rightarrow \beta \gamma \delta$  with lookahead  $a$ , generates:
  - $[\alpha \rightarrow \bullet \beta \gamma \delta, a]$ ,  $[\alpha \rightarrow \beta \bullet \gamma \delta, a]$ ,  $[\alpha \rightarrow \beta \gamma \bullet \delta, a]$ ,  $[\alpha \rightarrow \beta \gamma \delta \bullet, a]$
- ***The set of LR(1) items is finite.***
  - *Sets of LR(1) items represent LR(1) parser states.*

# The Table Construction Algorithm

- Table construction:
  - 1. Build the canonical collection of sets of LR(1) items,  $S$ :
    - I) Begin in  $S_0$  with  $[\text{Goal} \rightarrow \bullet \alpha, \text{eof}]$  and find all equivalent items as **closure**( $S_0$ ).
    - II) Repeatedly compute, for each  $S_k$  and each symbol  $\alpha$  (both terminal and non-terminal), **goto**( $S_k, \alpha$ ). If the set is not in the collection add it. This eventually reaches a fixed point.
  - 2. Fill in the table from the collection of sets of LR(1) items.
- The canonical collection completely encodes the transition diagram for the handle-finding DFA.
- The lookahead is the key in choosing an action:

*Remember Expr-Term from Lecture 8 slide 7, when we chose to shift rather than reduce to Expr?*

# Closure(state)

**Closure(s)**      // s is the state  
  **while** (s is still changing)  
    **for each** item  $[\alpha \rightarrow \beta \bullet \gamma \delta, a]$  in s  
      **for each** production  $\gamma \rightarrow \tau$   
        **for each** terminal b in FIRST( $\delta a$ )  
          **if**  $[\gamma \rightarrow \bullet \tau, b]$  is not in s, then add it.

**Recall** (Lecture 7, Slide 7): *FIRST(A)* is defined as the set of terminal symbols that appear as the first symbol in strings derived from A.

E.g.: FIRST(Goal) = FIRST(CatNoise) = FIRST(miau) = miau

**Example:** (using the CatNoise Grammar) S0: {[Goal  $\rightarrow \bullet$  CatNoise, eof],  
[CatNoise  $\rightarrow \bullet$  CatNoise miau, eof], [CatNoise  $\rightarrow \bullet$  miau, eof],  
[CatNoise  $\rightarrow \bullet$  CatNoise miau, miau], [CatNoise  $\rightarrow \bullet$  miau, miau]}  
(the 1st item by definition; 2nd,3rd are derived from the 1st; 4th,5th are derived from the 2nd)

# Goto(s,x)

**Goto(s,x)**

new= $\emptyset$

**for each** item  $[\alpha \rightarrow \beta \bullet x \delta, a]$  in s

**add**  $[\alpha \rightarrow \beta x \bullet \delta, a]$  to new

**return closure**(new)

Computes the state that the parser would reach if it recognised an x while in state s.

## Example:

S1 (x=CatNoise):  $[\text{Goal} \rightarrow \text{CatNoise} \bullet, \text{eof}]$ ,  $[\text{CatNoise} \rightarrow \text{CatNoise} \bullet \text{ miau}, \text{eof}]$ ,  
 $[\text{CatNoise} \rightarrow \text{CatNoise} \bullet \text{ miau}, \text{miau}]$

S2 (x=miau):  $[\text{CatNoise} \rightarrow \text{miau} \bullet, \text{eof}]$ ,  $[\text{CatNoise} \rightarrow \text{miau} \bullet, \text{miau}]$

S3 (from S1):  $[\text{CatNoise} \rightarrow \text{CatNoise} \text{ miau} \bullet, \text{eof}]$ ,  $[\text{CatNoise} \rightarrow \text{CatNoise} \text{ miau} \bullet, \text{miau}]$

# Example (slide 1 of 4)

Simplified expression grammar:

$$Goal \rightarrow Expr$$
$$Expr \rightarrow Term - Expr$$
$$Expr \rightarrow Term$$
$$Term \rightarrow Factor * Term$$
$$Term \rightarrow Factor$$
$$Factor \rightarrow id$$
$$FIRST(Goal) = FIRST(Expr) = FIRST(Term) = FIRST(Factor) = FIRST(id) = id$$
$$FIRST(-) = -$$
$$FIRST(*) = *$$

# Example: first step (slide 2 of 4)

- $S_0$ :  $\text{closure}(\{[\text{Goal} \rightarrow \bullet \text{Expr}, \text{eof}]\})$   
 $\{[\text{Goal} \rightarrow \bullet \text{Expr}, \text{eof}], [\text{Expr} \rightarrow \bullet \text{Term-Expr}, \text{eof}],$   
 $[\text{Expr} \rightarrow \bullet \text{Term}, \text{eof}], [\text{Term} \rightarrow \bullet \text{Factor} * \text{Term}, \text{eof}],$   
 $[\text{Term} \rightarrow \bullet \text{Factor} * \text{Term}, -], [\text{Term} \rightarrow \bullet \text{Factor}, \text{eof}],$   
 $[\text{Term} \rightarrow \bullet \text{Factor}, -], [\text{Factor} \rightarrow \bullet \text{id}, \text{eof}], [\text{Factor} \rightarrow \bullet \text{id}, -],$   
 $[\text{Factor} \rightarrow \bullet \text{id}, *]\}$
- Next states:
  - Iteration 1:
    - $S_1$ :  $\text{goto}(S_0, \text{Expr})$ ,  $S_2$ :  $\text{goto}(S_0, \text{Term})$ ,  $S_3$ :  $\text{goto}(S_0, \text{Factor})$ ,  $S_4$ :  $\text{goto}(S_0, \text{id})$
  - Iteration 2:
    - $S_5$ :  $\text{goto}(S_2, -)$ ,  $S_6$ :  $\text{goto}(S_3, *)$
  - Iteration 3:
    - $S_7$ :  $\text{goto}(S_5, \text{Expr})$ ,  $S_8$ :  $\text{goto}(S_6, \text{Term})$



# Example: the states (slide 3 of 4)

S1: {[Goal→Expr•,eof]}

S2: {[Goal→Term•-Expr,eof], [Expr→Term•,eof]}

S3: {[Term→Factor•\*Term,eof],[Term→Factor•\*Term,-],  
[Term→Factor•,eof], [Term→Factor•,-]}

S4: {[Factor→id•,eof], [Factor→id•,-], [Factor→id•,\*]}

S5: {[Expr→Term-•Expr,eof], [Expr→•Term,eof],  
[Term→•Factor\*Term,eof], [Term→•Factor\*Term,-],  
[Term→•Factor,eof], [Term→•Factor,-], [Factor→•id,eof],  
[Factor→•id,-], [Factor→•id,-]}

S6: {[Term→Factor\*•Term,eof],[Term→Factor\*•Term,-],  
[Term→•Factor\*Term,eof], [Term→•Factor\*Term,-],  
[Term→•Factor,eof], [Term→•Factor,-], [Factor→•id,eof],  
[Factor→•id,-], [Factor→•id,-]}

S7: {[Expr→Term-Expr•,eof]}

S8: {[Term→Factor\*Term•,eof], Term→Factor\*Term•,-]}

# Table Construction

- 1. Construct the collection of sets of LR(1) items.
- 2. State  $i$  of the parser is constructed from state  $j$ .
  - If  $[A \rightarrow \alpha \bullet a \beta, b]$  in state  $i$ , and  $\text{goto}(i, a) = j$ , then set  $\text{action}[i, a]$  to “shift  $j$ ”.
  - If  $[A \rightarrow \alpha \bullet, a]$  in state  $i$ , then set  $\text{action}[i, a]$  to “reduce  $A \rightarrow \alpha$ ”.
  - If  $[\text{Goal} \rightarrow A \bullet, \text{eof}]$  in state  $i$ , then set  $\text{action}[i, \text{eof}]$  to “accept”.
  - If  $\text{goto}[i, A] = j$  then set  $\text{goto}[i, A]$  to  $j$ .
- 3. All other entries in action and goto are set to “error”.

# Example: The Table (slide 4 of 4)

*Goal*  $\rightarrow$  *Expr*

*Expr*  $\rightarrow$  *Term-Expr*

*Expr*  $\rightarrow$  *Term*

*Term*  $\rightarrow$  *Factor*\**Term*

*Term*  $\rightarrow$  *Factor*

*Factor*  $\rightarrow$  *id*

STA TE	ACTION				GOTO		
	id	-	*	eof	Expr	Term	Factor
0	S 4				1	2	3
1				Accept			
2		S 5		R 3			
3		R 5	S 6	R 5			
4		R 6	R 6	R 6			
5	S 4				7	2	3
6	S 4					8	3
7				R 2			
8		R 4		R 4			

# Further remarks

- If the algorithm defines an entry more than once in the ACTION table, then the grammar is not LR(1).
- Other table construction algorithms, such as LALR(1) or SLR(1), produce smaller tables, but at the cost of larger space requirements.
- **yacc** can be used to convert a context-free grammar into a set of tables using LALR(1) (see % **man yacc** )
- **In practice**: “...the compiler-writer does not really want to concern himself with how parsing is done. So long as the parse is done correctly, ..., he can live with almost any reliable technique...” [J.J.Horning from “Compiler Construction: An Advanced Course”, Springer-Verlag, 1976]