5 Cos[t] + Sin[t]
Cos[t] - 5 Sin[t]

```
DSolve[eqn, y, x] solves a differential equation for the function y, with independent variable x.
  \mathsf{DSolve}[\{\mathit{eqn}_1, \mathit{eqn}_2, \ldots\}, \{y_1, y_2, \ldots\}, x] \; \mathsf{solves} \; \mathsf{a} \; \mathsf{list} \; \mathsf{of} \; \mathsf{differential} \; \mathsf{equations}.
  DSolve[eqn, y, \{x_1, x_2, ...\}] solves a partial differential equation. \gg
 (*Solve the differential eq d^2x/dt^2=-kx*)
deq = x''[t] + k * x[t] == 0;
sol = DSolve[deq, x[t], t]
\left\{\left\{x[t] \to C[1] \; \text{Cos}\!\left[\sqrt{k} \; t\right] + C[2] \; \text{Sin}\!\left[\sqrt{k} \; t\right]\right\}\right\}
xt = x[t] /. sol[[1]]
C[1] \cos \left[ \sqrt{k} t \right] + C[2] \sin \left[ \sqrt{k} t \right]
vt = D[xt, t]
\sqrt{k} \ \texttt{C[2]} \ \texttt{Cos} \Big[ \sqrt{k} \ \texttt{t} \Big] - \sqrt{k} \ \texttt{C[1]} \ \texttt{Sin} \Big[ \sqrt{k} \ \texttt{t} \Big]
xt = xt /. k \rightarrow 1
vt = vt /. k \rightarrow 1
C[1] Cos[t] + C[2] Sin[t]
C[2] Cos[t] - C[1] Sin[t]
eq1 = (xt/.t \rightarrow 0) = 5
eq2 = (vt /. t \rightarrow 0) = 1
C[1] = 5
C[2] = 1
constant = Solve[{eq1, eq2}, {C[1], C[2]}]
\{\,\{\text{C[1]}\,\rightarrow\,5\,\text{, C[2]}\,\rightarrow\,1\}\,\}
xt = xt /. constant[[1]]
vt = vt /. constant[[1]]
```

Plot[{xt, vt}, {t, 0, 10}]

