

**(\*Matrix and Vector Operations\*)**

*In[ ]:=* **u = {a, b, c}**

*Out[ ]:=* {a, b, c}

*In[ ]:=* **u1 = {2, 5, 7};**

**u2 = {2, 3, 6};**

**u1 + u2**

*Out[ ]:=* {4, 8, 13}

*In[ ]:=* **u2 + u1**

*Out[ ]:=* {4, 8, 13}

*In[ ]:=* **u1 + u2 == u2 + u1**

*Out[ ]:=* True

*In[ ]:=* **u1 - u2**

*Out[ ]:=* {0, 2, 1}

*In[ ]:=* **u2 - u1**

*Out[ ]:=* {0, -2, -1}

*In[ ]:=* **u1 - u2 == u2 - u1**

*Out[ ]:=* False

*In[ ]:=* **A = {7, 3, 9};**

**5 A**

*Out[ ]:=* {35, 15, 45}

*In[ ]:=* **Norm[A]**

*Out[ ]:=*  $\sqrt{139}$

*In[ ]:=* **Norm[{1, 0, 0}]**

*Out[ ]:=* 1

*In[ ]:=* **Norm[{9, 2, -4}] // N**

*Out[ ]:=* 10.0499

*In[ ]:=* **Sqrt[A]**

*Out[ ]:=*  $\{\sqrt{7}, \sqrt{3}, 3\}$

In[ ]:= ? Dot

Out[ ]:=

Symbol



$a.b.c$  or `Dot[a, b, c]` gives products of vectors, matrices, and tensors.



In[ ]:= Dot[u1, u2]

Out[ ]:= 61

In[ ]:= u = {2, 4, 9}; v = {7, 5, 8};

Dot[u, v]

Out[ ]:= 106

In[ ]:= u.v

Out[ ]:= 106

In[ ]:= ? Norm

Out[ ]:=

Symbol



`Norm[expr]` gives the norm of a number, vector, or matrix.

`Norm[expr, p]` gives the  $p$ -norm.



In[ ]:= m1 = {{2, 5}, {7, 8}}; m2 = {{1, 2}, {3, 9}}; v = {2, 5};  
m1 + m2

Out[ ]:= {{3, 7}, {10, 17}}

In[ ]:= m2 + m1

Out[ ]:= {{3, 7}, {10, 17}}

In[ ]:= m1 + m2 == m2 + m1

Out[ ]:= True

(\*scalar multiplication of matrix\*)

In[ ]:= c = 0;

c \* m1

Out[ ]:= {{0, 0}, {0, 0}}

In[ ]:= (\*power of matrix\*)

m1

m1^2

Out[ ]:= {{2, 5}, {7, 8}}

Out[ ]:= {{4, 25}, {49, 64}}

```
In[*]:= v
      m1
```

```
Out[*]:= {2, 5}
```

```
Out[*]:= {{2, 5}, {7, 8}}
```

```
In[*]:= (*column vector with matrix*)
      m1.v
```

```
Out[*]:= {29, 54}
```

```
(*row vector with matrix*)
```

```
In[*]:= v.m1
```

```
Out[*]:= {39, 50}
```

```
In[*]:= x = {2, 4, 6}; y = {7, 5, 3};
      rv = x + y
```

```
Out[*]:= {9, 9, 9}
```

```
In[*]:= mx = Norm[x]; my = Norm[y];
      dotxy = x.y;
      mxmy = mx * my;
      th = ArcCos[dotxy / mxmy]
      th = ArcCos[dotxy / mxmy] // N
      th = ArcCos[dotxy / mxmy] / Degree // N
```

```
Out[*]:= ArcCos[13  $\sqrt{\frac{2}{581}}$ ]
```

```
Out[*]:= 0.703274
```

```
Out[*]:= 40.2946
```

```
In[*]:= (*Direction Vector and Angle*)
      l = {3, 5, 6};
      unitvector = uv = directionvector = dv = l / Norm[l]
      da = ArcCos[dv] / Degree // N
```

```
Out[*]:= {  $\frac{3}{\sqrt{70}}$ ,  $\sqrt{\frac{5}{14}}$ ,  $3\sqrt{\frac{2}{35}}$  }
```

```
Out[*]:= {68.9877, 53.3008, 44.1814}
```