What are Marginal Models, and Why Do We Fit Them?

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Now, we shift focus to **marginal models** as alternative tools for capturing *within-cluster* correlations

Key Distinction: In marginal models, we do ***not*** include random effects, because we are not interested in estimating between-cluster variance in coefficients

We still model **within-cluster** correlations

What are Marginal Models?

- General class of statistical models used to model dependent data, where observations within a randomly sampled cluster may be correlated
- We are interested in the estimation of overall, population-averaged relationships between independent variables (IVs) and dependent variables (DVs), across all clusters!

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Goal: Make inference about these overall, marginal relationships, with standard errors that reflect clustering

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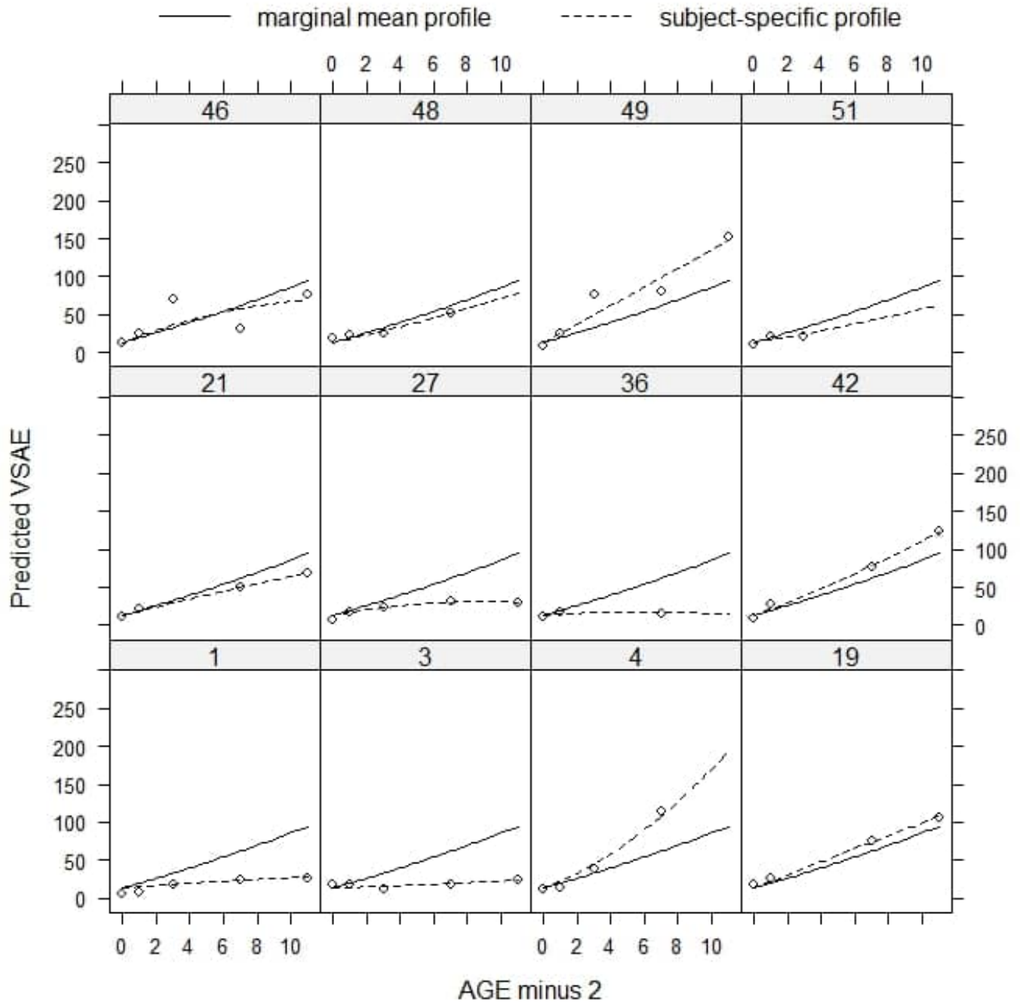

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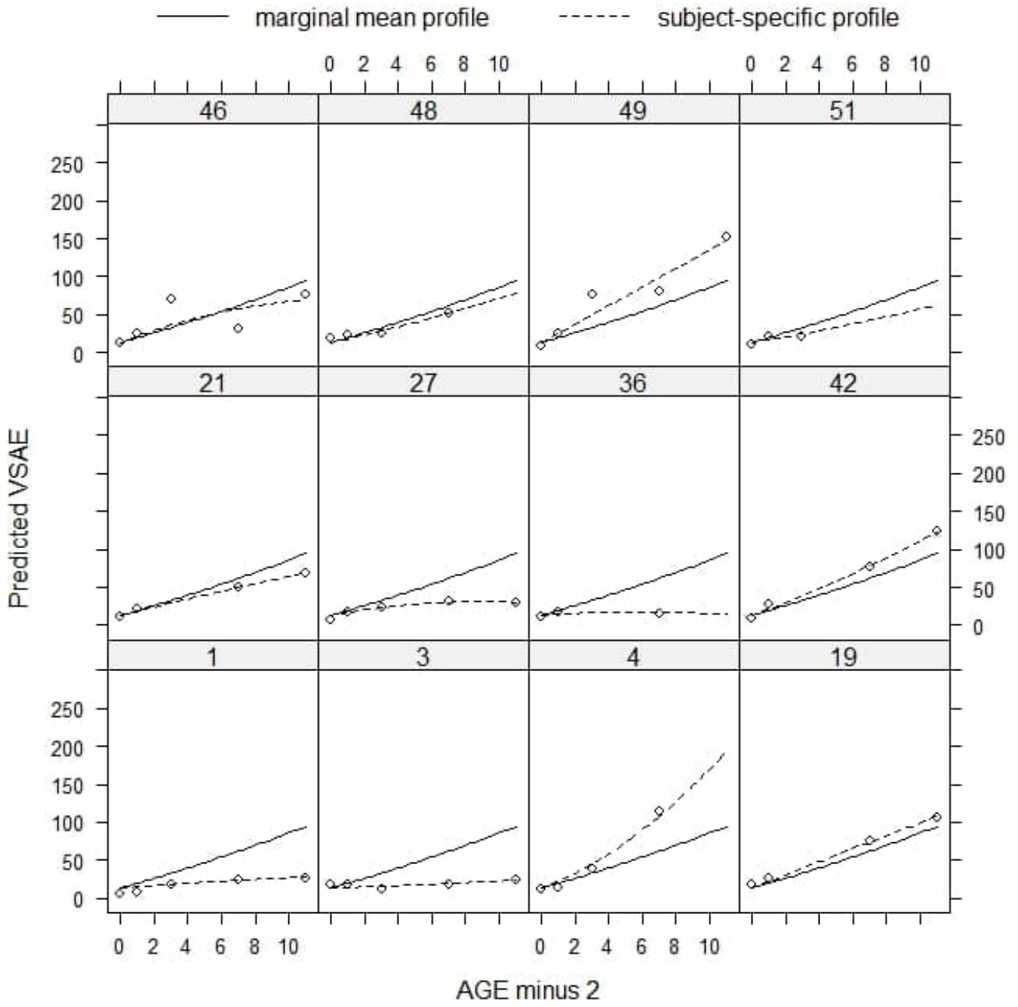
- Multilevel models capture dependencies by allowing coefficients to randomly vary across clusters
- Marginal models simply look at overall relationships, and make sure that standard errors reflect dependencies



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2. Select structure that makes sense for the **variances <u>and</u> <u>covariances</u>** of observations coming from the same cluster that are <u>not explained</u> by the selected predictors

3. Compare the fits of models with different choices for this variance-covariance structure, and choose the best fit

Marginal Models

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- Errors close to each other in time have a stronger correlation than errors farther apart
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For clustered data, we might assume that the errors within a cluster follow an **exchangeable** covariance structure (constant variance and covariance)

When Can We Fit Marginal Models?

Rather than assuming i.i.d. data!)

- ☑ We have data from a longitudinal or clustered study design that **introduces dependencies in the collected data**, and we need to model those dependencies to obtain **accurate inferences** about relationships of interest

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- ☑ We have **no interest** in estimating between-subject or between-cluster variance in the coefficients of interest
- ☑ We wish to make inference about **overall, marginal relationships between IVs and DVs** in the target population; that is, we do not wish to condition on random effects of subjects or clusters in the modeling

Why do we Fit Marginal Models?

- These models offer some advantages over other approaches for **dependent data** (e.g., multilevel modeling):
  - Quicker computational times; faster estimation
  - Robust standard errors that reflect the specified correlation structure
  - Easier accommodation of non-normal outcomes (recall that multilevel models for non-normal outcomes can take a while to estimate!)

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Remember: We can no longer make inference about between-cluster variance in the coefficients of interest!

What's Next?

- We'll revisit earlier examples of multilevel modeling, and consider alternative marginal modeling approaches
- We'll discuss how to estimate these models, and methods for assessing model fit
- Finally, we will present examples, and you'll be able to walk through examples of fitting these models using Python!