

#### **Testing a One Population Proportion**

Reed Coots
Statistics Course Developer





## Hypotheses

 $H_0: p = 0.52$ 

 $H_a: p > 0.52$ 

Best Estimate of p is  $\hat{s} = 0.56$ 

Where p is the population proportion of parents with a teenager who believe that electronics and social media is the cause of their teenager's lack of sleep

$$\alpha = 0.05$$



#### **Test Statistic**

# Best estimate - Hypothesized estimate Standard error of estimate

$$\frac{\hat{p}-p_o}{s.e.}$$

$$s.\,e.\,(\hat{p})=\sqrt{rac{p\cdot(1-p)}{n}}$$
  $\Longrightarrow$   $s.\,e.\,(\hat{p})=\sqrt{rac{p_0\cdot(1-p_o)}{n}}$ 



### **Test Statistic**

$$\hat{p}-p_o$$
 $s.e.$ 

Null 
$$s.e.(\hat{p}) = \sqrt{\frac{p_0\cdot(1-p_o)}{n}}$$

$$Z = 0.56 - 0.52$$
 $0.0157$ 

$$Z = 2.555$$



## Test Statistic Interpretation

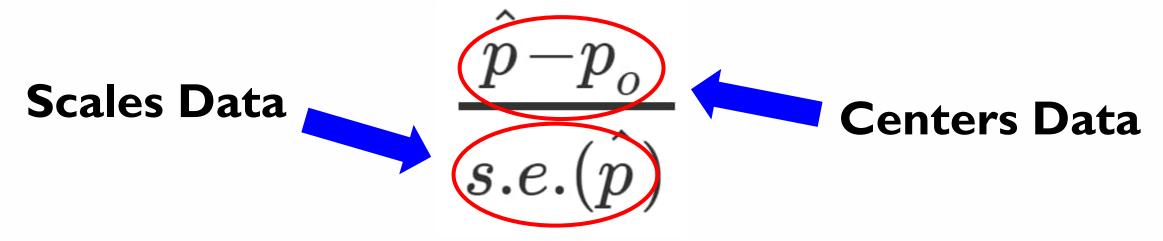
$$Z = 2.555$$

That means that our observed sample proportion is 2.555 null standard errors above our hypothesized population proportion



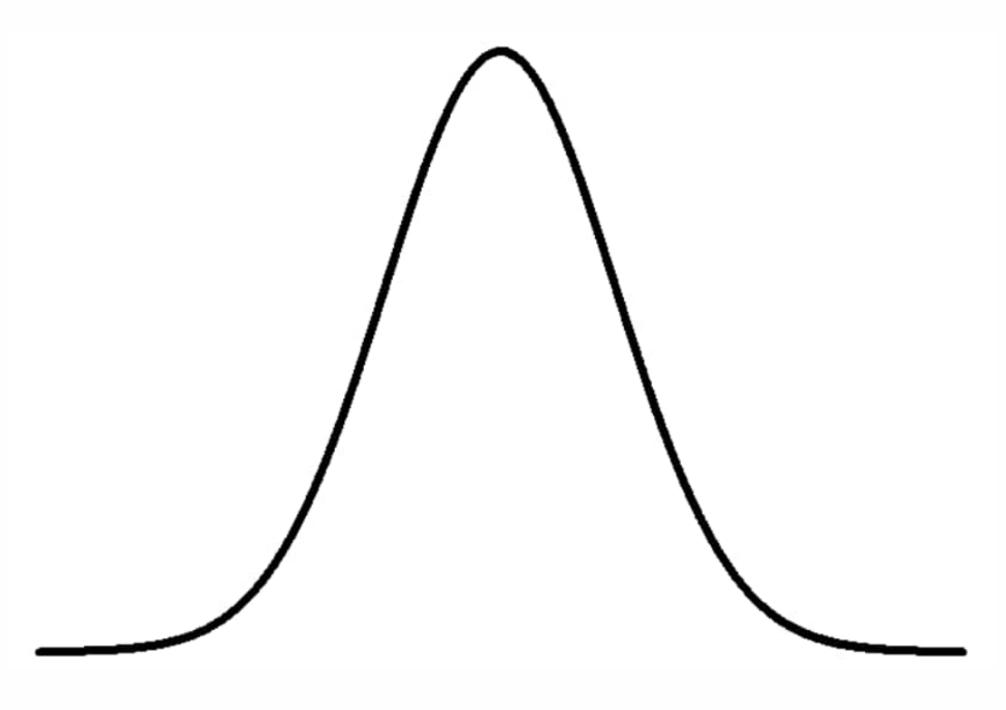
### Test Statistic Distribution

- A Z test statistic is another random variable! It has a distribution.
- The Z test statistic will always follow a N(0, I)
- This is due to us centering and scaling our original data





## The P-Value





#### Conclusions

p-value =  $0.0053 < \alpha = 0.05$ 

Reject the null hypothesis ( $H_0$ : p = 0.52)

There is sufficient evidence to conclude that the population proportion of parents with a teenager who believe that electronics and social media is the cause for lack of sleep is greater than 52%.



## Summary

- 4 main steps to a hypothesis test
  - Stating hypothesis & select significance level  $(\alpha)$
  - Checking assumptions
  - Calculating a test statistic and getting a p-value from the test statistic
  - Drawing a conclusions from the p-value
- The Z test statistic distribution is N(0,1)