

Bayesian Approaches to Statistics and Modeling Case Study • Part II

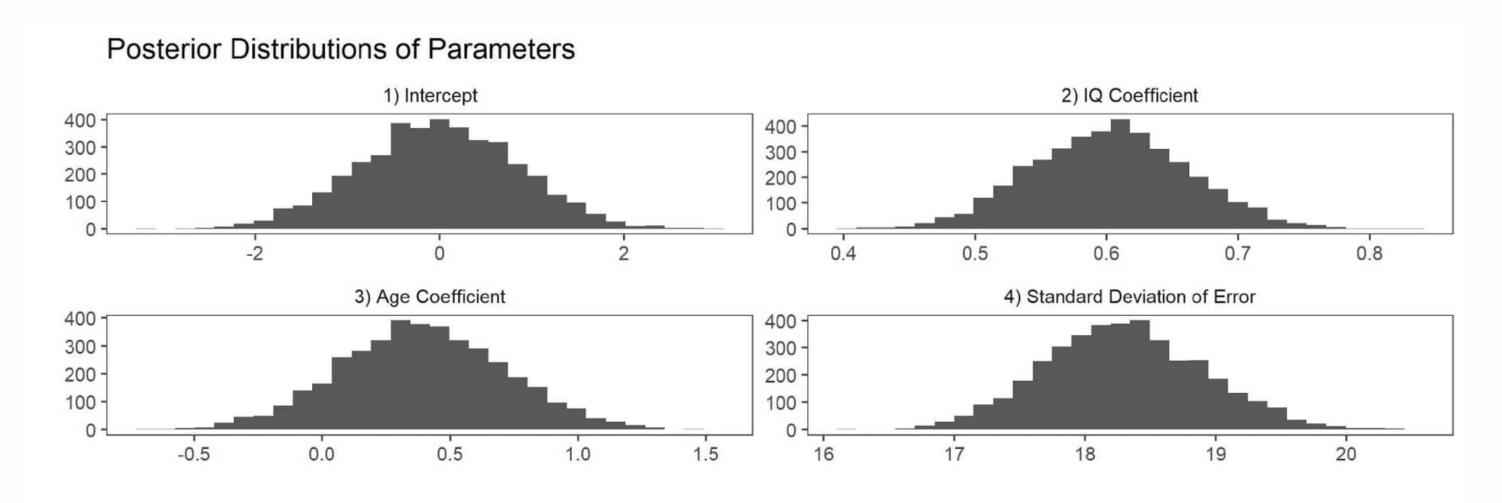
Mark Kurzeja



Case Layout

- We are going to walk through a multi-level regression problem using a Bayesian framework
- Bayesian frameworks are be flexible enough to do variable selection, regularization, modeling of dependence, fit models where the number of parameters exceed the number of observations, and model dependence all within the same model
- We will barely scratch the surface of these methods in this case, but we will explore the Bayesian workflow for modeling



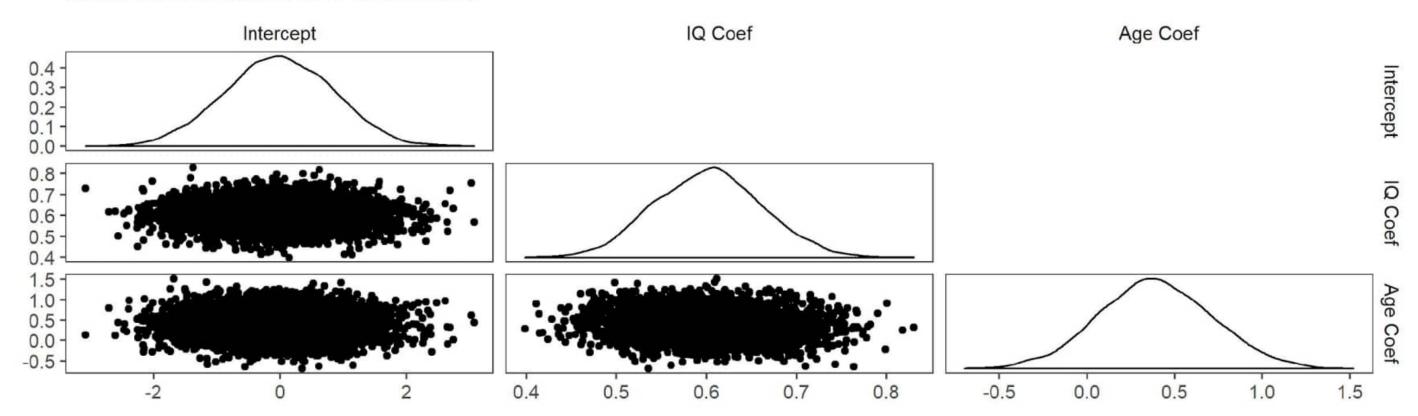


Belief about the World

Collect Data







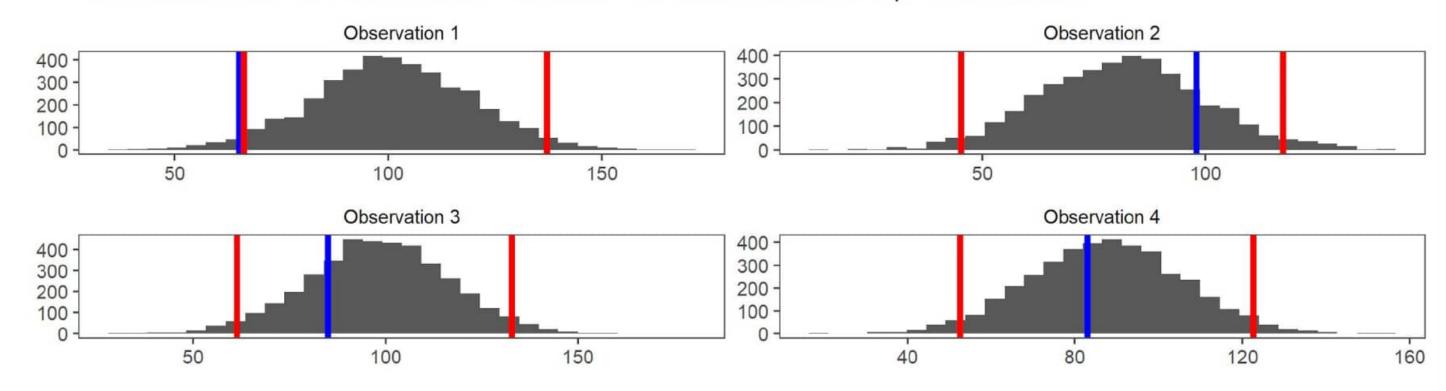
Belief about the World

Collect Data



Posterior Predictive Intervals for First Four Observations

The blue line is the observed value for Childs IQ. The red lines are the 95% predictive interval



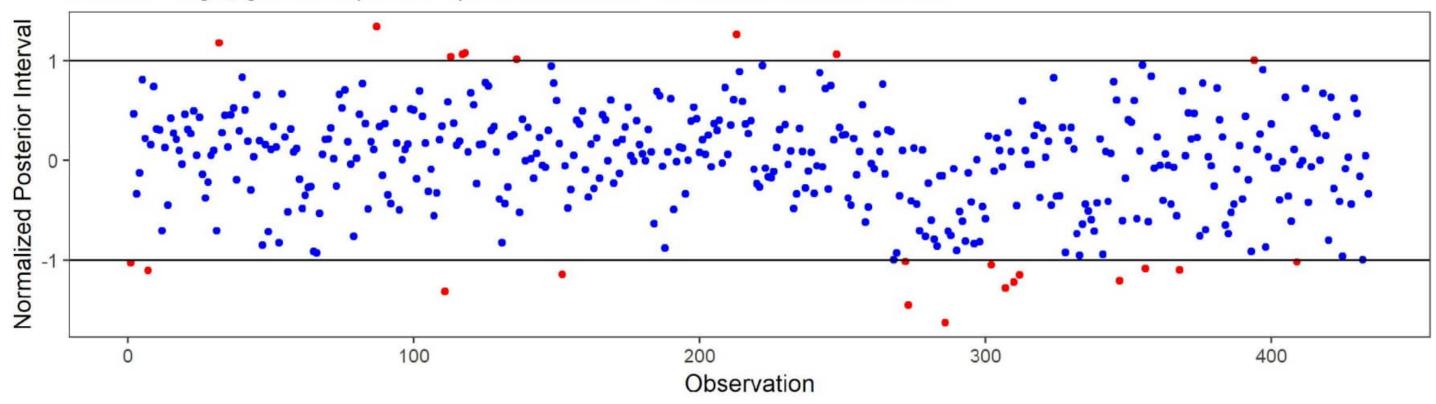
Belief about the World

Collect Data





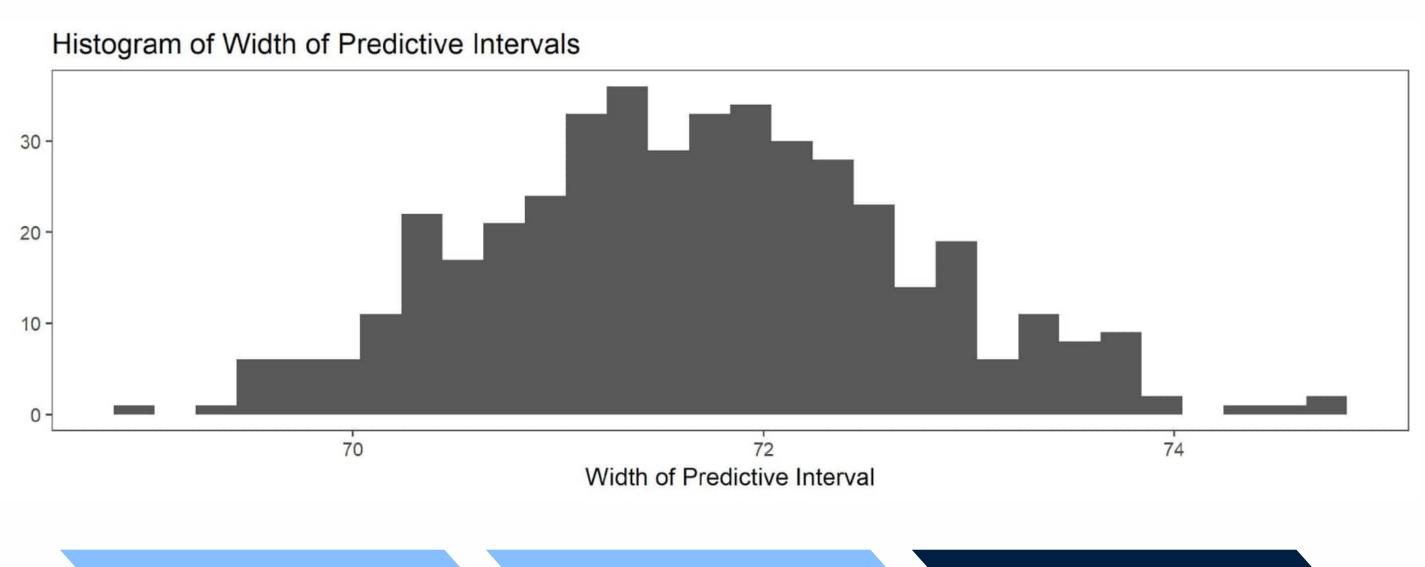
If a dot is in [-1,1] then the posterior predictive interval contained the true childs IQ



Belief about the World

Collect Data

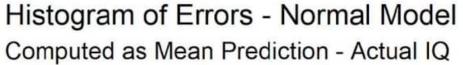


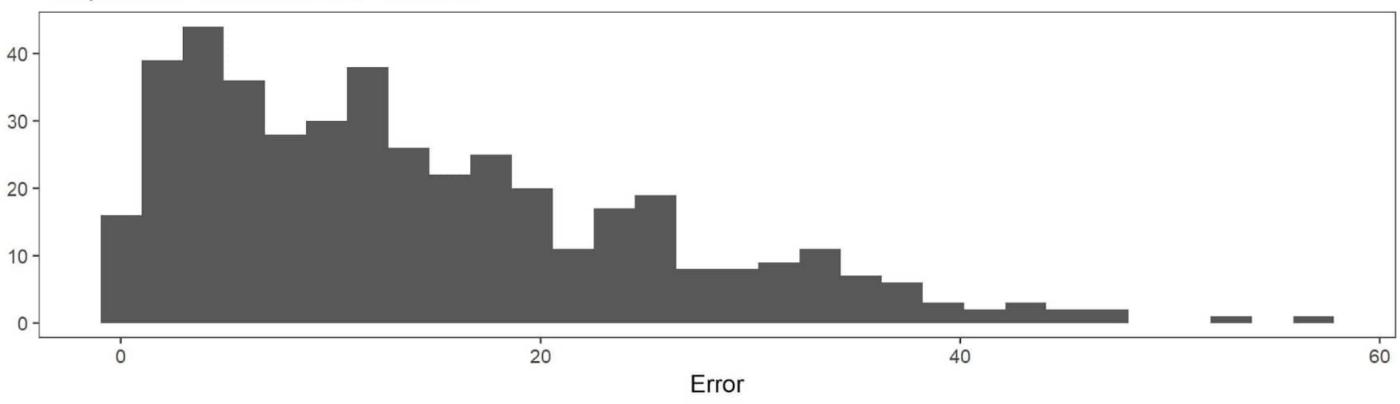


Belief about the World

Collect Data



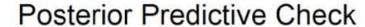




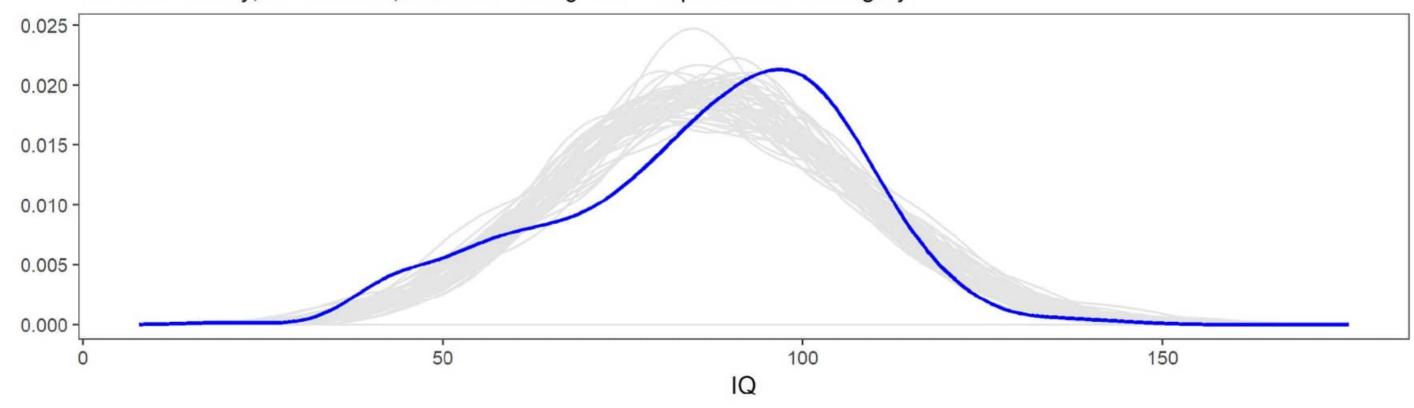
Belief about the World

Collect Data





The true density, of Child IQs, is in blue. The generated posteriors are in grey



Belief about the World

Collect Data



The Model - Observations

- We have not accounted for the high school education variable
- We have a reasonable number of observations that fall outside of their 95% predictive intervals ($\approx 5\%$)
- The width of the predictive intervals is pretty large. We should see if we can
 do better
- The estimates systematically overestimate IQ's of around 65-80 and underestimate those around 90-115

Belief about the World

Collect Data



The Model - Observations

- Next time, we are going to explore updates that we can make to this model
- We will look to incorporating the high school status of the mother and working with a hierarchal structure will improve our model
- We will need to come up with some way of addressing the skew of the data