

Unit No. 11

Loci And Construction

Exercise No. 11.1

Question No. 1.

Construct $\triangle ABC$ with the given measurements and verify that the perpendicular bisectors of the triangle are concurrent.

(i) $m AB = 5 \text{ cm}$, $m BC = 6 \text{ cm}$ and $m AC = 7 \text{ cm}$

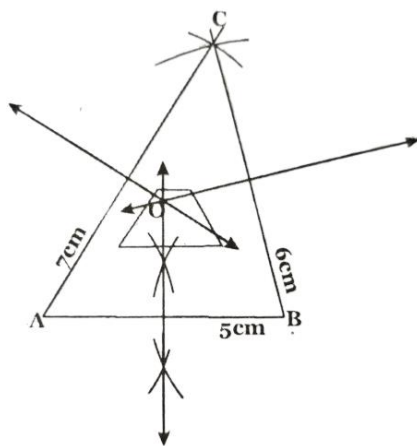
Construction:

- (i) Construct $\triangle ABC$ with given measurements.
- (ii) Draw right bisectors of sides AB , BC and CA of triangle.
- (iii) All right bisectors meet at point O .

So right bisectors of sides of $\triangle ABC$ are concurrent.

(Pass through same point.)

Figure:



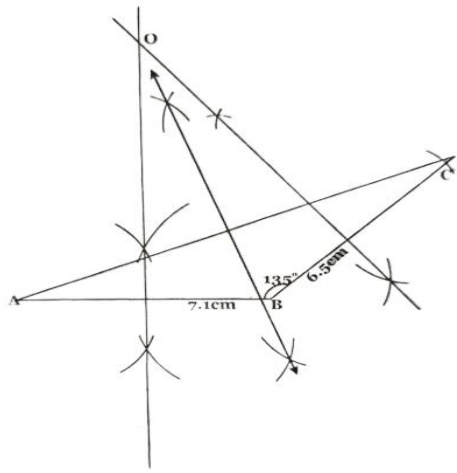
(ii) $m AB = 7.1 \text{ cm}$, $m \angle B = 135^\circ$ and $m BC = 6.5 \text{ cm}$

Construction Steps:

- (i) Construct triangle according to measurement.
- (ii) This is an obtuse angle triangle.
- (iii) Draw perpendicular bisector of sides AB , BC and CA of triangle.
- (iv) All perpendicular bisectors pass through same point O .

So perpendicular bisectors are concurrent.

Figure:



Question No. 2.

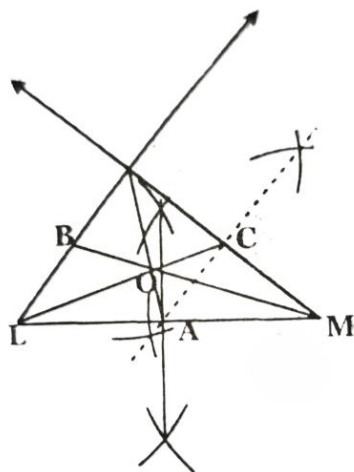
Construct $\triangle LMN$ of the following measurements and verify that the medians of the triangle are concurrent.

- (i) $m LM = 4.9$ cm, $m \angle L = 51^\circ$ and $m \angle M = 38^\circ$

Construction Steps:

- (i) Construct $\triangle LMN$ according to given measurement.
- (ii) Find mid points of all sides of $\triangle LMN$.
- (iii) Join mid points A, B, C with opposite vertices.
- (iv) All medians pass through same point O. So, medians of triangle are concurrent.

Figure:

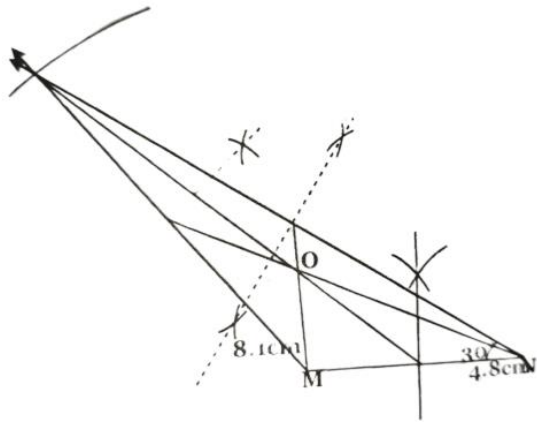


- (ii) $m MN = 4.8$ cm, $m \angle N = 30^\circ$ and $m LM = 8.1$ cm

Construction Steps:

- (i) Construct $\triangle LMN$ with give measurements.
- (ii) Find mid points of all sides.
- (iii) All these mid points are joined to opposite vertices. As all medians pass through same point O. So, medians are concurrent.

Figure:



Question No. 3.

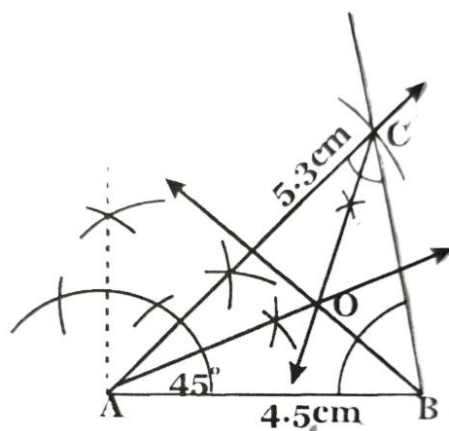
Verify that the angle bisectors of $\triangle ABC$ are concurrent with the following measurement:

(i) $m AB = 4.5 \text{ cm}$, $m \angle A = 45^\circ$ and $m AC = 5.3 \text{ cm}$

Construction Steps:

- (i) Construct $\triangle ABC$ according to given measurements.
- (ii) Draw angle bisectors of each angle.
- (iii) All these angle bisectors pass through the same point O. So, angle bisectors are concurrent.

Figure:



(ii) $m AB = 6 \text{ cm}$, $m \angle A = 150^\circ$ and $m \angle B = 60^\circ$

Solution:

Sum of three angles of a triangle is 180° . But here sum of two given angles in $150^\circ + 60^\circ = 210^\circ$ which is not possible. So, triangle is not possible to construct.

Hence no angle bisectors and so no point of concurrency exist here.

Question No. 4.

Given the measurements of $\triangle DEF$: $m DE = 4.8 \text{ cm}$, $m EF = 4 \text{ cm}$ and $m \angle E = 45^\circ$, draw altitude of $\triangle DEF$ and find orthocentre.

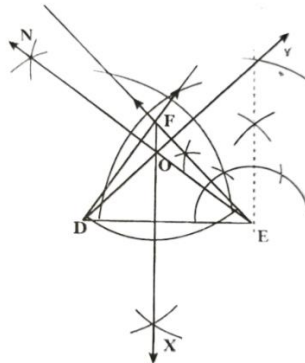
Construction Steps:

- (i) Construct triangle DEF according to given measurements.

(ii) Draw altitudes FX , DY , EZ of the triangle. All these altitudes pass through same point O . Thus, altitudes of triangle are concurrent.

So, orthocentre is point " O ".

Figure:



Question No. 5.

Construct the following triangles and find whether there exists any ambiguous case.

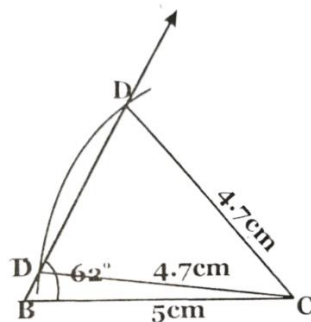
(i) $\triangle BCD$; $m BC = 5 \text{ cm}$, $m \angle B = 62^\circ$ and $m CD = 4.7 \text{ cm}$

Construction Steps:

(i) Construct triangle with the given measurements.

(ii) An arc of length 4.7 cm intersects angle arm of 62° at two distinct points D and D' . So here two triangles are constructed named as $\triangle BCD'$ and $\triangle BCD$.

Figure:



(ii) $\triangle KLM$; $m LM = 5 \text{ cm}$, $m \angle M = 42^\circ$ and $m LN = 5 \text{ cm}$

Construction Steps:

(i) Construct triangle with given measurements.

(ii) An arc of length 5 cm intersects angle arm at two distinct points N and N' . So we have two triangles named as $\triangle LMN$ and $\triangle LMN'$.

Figure:

