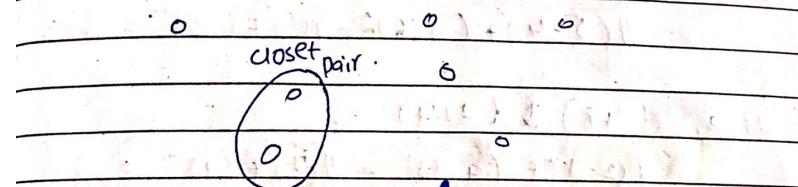


## Brute force Algorithm..

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The Brute force algorithm is all about trial & error, letting a computer work systematically through a range of possibilities until it arrives at the correct solution.  
→ e.g; Padlock with 4 digit 0 to 9

**Closet pair problem-** In metric space  
→ find a pair of points with the smallest distance b/w them -



**Example To find Closet pair  
Using brute force algorithm:**

Points = (1,2), (4,6), (7,8), (2,9), (5,3)

**(calculate Distance):**  $\because \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$

→ Distance b/w (1,2) & (4,6)

$$= \sqrt{(4-1)^2 + (6-2)^2} = \sqrt{3^2 + 4^2} = 5$$

→ Distance : (1,2) & (7,8)

$$= \sqrt{(7-1)^2 + (8-2)^2} = \sqrt{6^2 + 6^2} = 6\sqrt{2}$$

→ Distance = (1,2), (2,9)

$$= \sqrt{(2-1)^2 + (9-2)^2} = \sqrt{1^2 + 7^2} = 5\sqrt{2}$$

$$\begin{array}{c} \text{Date: } \\ \text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ = \sqrt{(2-1)^2 + (9-2)^2} = \sqrt{7^2 + 1^2} = \sqrt{50} \end{array}$$

$$\begin{array}{c} \text{Distance} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ = \sqrt{(5-1)^2 + (3-2)^2} = \sqrt{4^2 + 1^2} = \sqrt{17} \end{array}$$

$$\begin{array}{c} \text{Now: } (4, 6) \& (7, 8) \\ = \sqrt{(7-4)^2 + (8-6)^2} = \sqrt{3^2 + 2^2} = \sqrt{13} \end{array}$$

$$\rightarrow (4, 6) \& (2, 9) \\ = \sqrt{(2-4)^2 + (9-6)^2} = \sqrt{7^2 + 2^2} = \sqrt{53}$$

$$\rightarrow (4, 6) \& (5, 3) \\ = \sqrt{(5-4)^2 + (3-6)^2} = \sqrt{1^2 + 3^2} = \sqrt{10}$$

$$\begin{array}{c} \text{Now, } (7, 8) \& (2, 9) \\ = \sqrt{(2-7)^2 + (9-8)^2} = \sqrt{5^2 + 1^2} = \sqrt{26} \end{array}$$

$$\begin{array}{c} (7, 8) \& (5, 3) \\ = \sqrt{(5-7)^2 + (3-8)^2} = \sqrt{2^2 + 5^2} = \sqrt{29} \end{array}$$

$$\begin{array}{c} \text{Now, } (2, 9) \& (5, 3) \\ = \sqrt{(5-2)^2 + (3-9)^2} = \sqrt{3^2 + 6^2} = \sqrt{45} \end{array}$$

So; the smallest distance is between  $(4, 6)$  &  $(5, 3)$ .

Time Complexity =  $O(N^2)$ .

## Complexity analysis of Close Pair:

The time Complexity of Euclidian distance algorithm depends on the dimensionality of the space in which the distance are being calculated.

Euclidian distance b/w two point =

$$(P_1, P_2, P_3 \dots P_n) \text{ & } (q_1, q_2, q_3 \dots q_n)$$

$$= \sqrt{(q_1 - P_1)^2 + (q_2 - P_2)^2 + \dots + (q_n - P_n)^2}$$

### Operations of Euclidian:

- Difference Compute b/w Corresponding point.
- Square of difference.
- Sum of squared differences
- Take the square root of sum.

Each operation is constant time, so

the overall Complexity of b/w two Points in n-dimensional Space is  $O(N)$ .

→ If you have m pair of points to complexity is  $O(N * m)$ .

### Convex hull -Problem:

A set of points  $\Omega$  is convex if for point,  $P \in \Omega$ , the entire line seg  $PQ$  is in the set-

They are used for detecting outlier by some statistical techniques.  
Also used in Collision detection-

### What is polygon in Convex Hull

A polygon is a region of the plane bounded by a cycle of line segments joined end-to-end.

Two types of polygon;

→ Regular polygon: Equal length of all sides

→ Irregular polygons: Unequal length sides

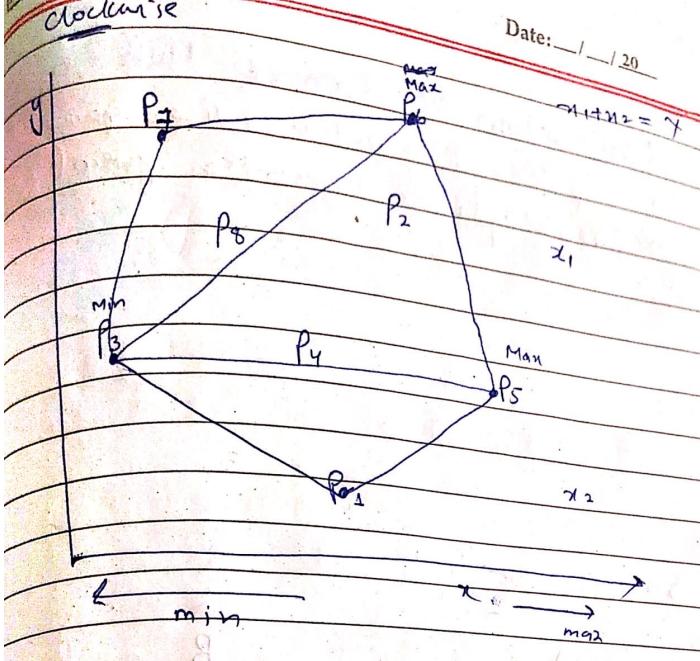
Identical angle at each vertex.

Angle differ from one another

### Difference between Convex & Concave polygons

Each angle  $< 180^\circ$  called Convex.

$> 180^\circ$  called concave.



Inter point of polygon are =  $P_8, P_2, P_4$

line Segment / outlier are

$P_1, P_5, P_6, P_7, P_3$

### Extreme point in Polygon-

Extreme point of a Convex set is a point of this set that is not a middle point of any line segment with end points in the set.

→ that does not lie on any open line segment.

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## Application of Convex Hull -

- Computer Visualization, Video games.
- Geographical information system ( G )

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# Dynamic Programming:

dynamic programming is a powerful design technique that can be used to solve problems of a computational nature.

- It refers to the tabular method.
- It is a technique where an algorithmic problem is first broken down into sub-problems, the results are saved & then sub-problems are optimized to find overall solution.

"Programming" here means "planning".

## Main Idea:

- Set up recurrence relation.
- Solve smaller instances.
- Record solution in a table.
- Extract solution.

## Element of DP(1) (overlapping subproblem).

- Split problem into subproblems that are similar as divide & conquer.
- It is found in that where bigger problem share the same smaller problem.

## ② Optimal substructure:-

It is an optimal selection among all the possible substructures that can help to select the best.