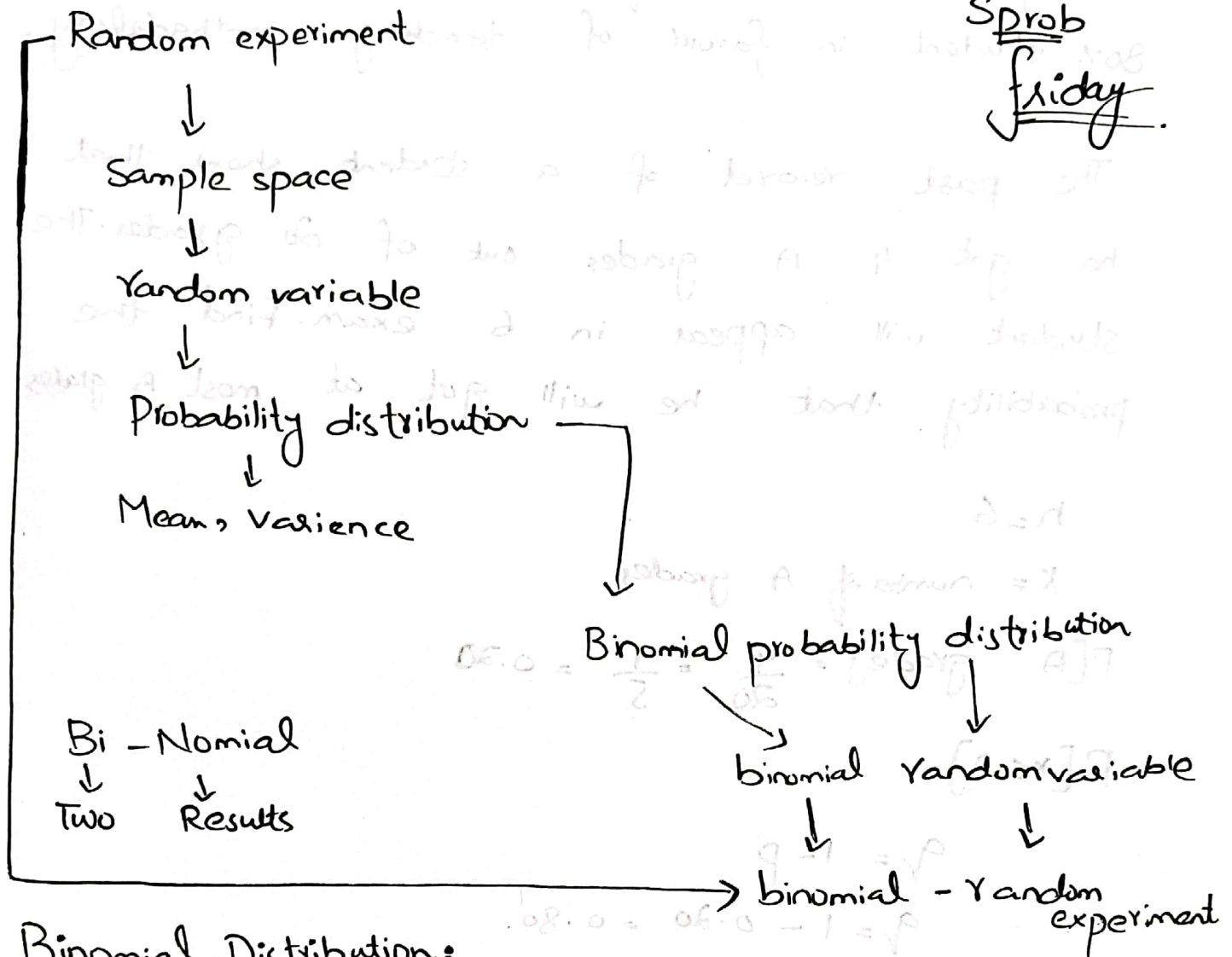


15.12.2023

S_{prob}

Friday



Binomial Distribution:

A random variable x has binomial distribution if it has the probability function.

$$b(\underbrace{x: n, p}_{\text{parameters}}) = \binom{n}{x} p^x q^{n-x}, \quad x = 0, 1, 2, 3, \dots, n$$

where

x : number of success outcomes

n : number of trial (sample size)

p : probability of success outcomes in a single trial.

$q = 1 - p$: probability of failure outcomes.

Example:-

The past feedback of an instructor shows that 80% student in favour of teaching methodology.

The past record of a student show that he got 4 A grades out of 20 grades. The student will appear in 6 exam. Find the probability that he will get at most A grades

$$n = 6$$

X = number of A grades

$$P[A \text{ grade}] = \frac{4}{20} = \frac{1}{5} = 0.20$$

$$P[X \leq 2]$$

$$q = 1 - p$$

$$q = 1 - 0.20 = 0.80$$

$$X \sim b(n, p)$$

$$b(X; 6, 0.20) = \binom{6}{x} (0.20)^x (0.80)^{6-x}$$

$$P[X \leq 2] = \sum_{x=0}^2 \binom{6}{x} (0.20)^x (0.80)^{6-x}$$