

	D_1	D_2	D_3	D_4	D_5	D_6	D_7	D_8	D_9	D_{10}
X	1	2	3	4	5	1	2	3	4	5
Y	3	4	1	2	1	4	1	2	5	4

	D_1	D_2	D_3	D_4	D_5	D_6	D_7	D_8	D_9	D_{10}
D_1	0									
D_2	1.4	0								
D_3	2.8	3.1	0							
D_4	3.1	2.8	1.4	0						
D_5	4.5	4.2	2	1.4	0					
D_6	1	1	3.6	3.6	5	0	0			
D_7	2.2	3	1	2.2	3	3.1	0			
D_8	2	2.2	1	1	2.2	2.8	1.4	0		
D_9	3.6	2.2	4.1	3	4.1	3.1	4.4	3.1	0	
D_{10}	4.1	3	3.6	2.2	3	4	4.2	2.8	1.4	0

$(D_1, D_2) = \sqrt{(2-1)^2 + (4-3)^2}$

 $= \sqrt{1+1}$
 $= \sqrt{2}$

$(D_1, D_3) = \sqrt{(3-1)^2 + (1-3)^2}$

 $= \sqrt{4 + (-2)^2}$
 $= 2.8$

$(D_1, D_4) = \sqrt{(4-1)^2 + (2-3)^2}$

 $= \sqrt{9+1}$
 $= 3.1$

$(D_1, D_5) = \sqrt{(5-1)^2 + (1-3)^2}$

 $= \sqrt{16+4}$
 $= 4.5$

$$(D_1 D_6) = \sqrt{(1-1)^2 + (4-3)^2}$$
$$= \sqrt{0+1}$$

$$= 1$$

$$(D_1 D_7) = \sqrt{(2-1)^2 + (1-3)^2}$$
$$= \sqrt{1+4}$$
$$= 2.2$$

$$(D_1 D_8) = \sqrt{(3-1)^2 + (3-3)^2}$$
$$= \sqrt{4}$$
$$= 2$$

$$(D_1 D_9) = \sqrt{(4-1)^2 + (5-3)^2}$$
$$= \sqrt{9+4}$$
$$= 3.6$$

$$(D_1 D_{10}) = \sqrt{(5-1)^2 + (4-3)^2}$$
$$= \sqrt{16+1}$$
$$= 4.1$$

$$(D_2 D_3) = \sqrt{(3-2)^2 + (1-4)^2}$$
$$= \sqrt{1+9}$$
$$= 3.1$$

$$(D_2 D_9) = \sqrt{(4-2)^2 + (2-4)^2}$$
$$= \sqrt{4+4}$$
$$= 2.8$$

$$(D_2 D_5) = \sqrt{(5-2)^2 + (1-4)^2}$$
$$= \sqrt{9+9}$$
$$= 4.2$$

$$(D_2 D_6) = \sqrt{(1-2)^2 + (4-4)^2}$$
$$= \sqrt{1}$$
$$= 1$$

$$(D_2 D_1) = \sqrt{(2-2)^2 + (1-4)^2}$$
$$= \sqrt{0+9}$$

$$(D_2 D_8) = \sqrt{(3-2)^2 + (2-4)^2}$$
$$= \sqrt{1+4}$$
$$= 2.2$$

$$(D_2 D_9) = \sqrt{(4-2)^2 + (5-4)^2}$$
$$= \sqrt{4+1}$$
$$= 2.2$$

$$(D_2 D_{10}) = \sqrt{(5-2)^2 + (4-4)^2}$$
$$= \sqrt{9}$$

$$(D_3 D_4) = \sqrt{(4-3)^2 + (2-1)^2}$$
$$= \sqrt{1+1}$$
$$= 1.4$$

$$(D_3 D_5) = \sqrt{(5-3)^2 + (1-1)^2}$$
$$= \sqrt{4}$$
$$= 2$$

$$(D_3 D_6) = \sqrt{(1-3)^2 + (4-1)^2}$$
$$= \sqrt{4+9}$$

$$= 3.6$$

$$(D_3 D_7) = \sqrt{(2-3)^2 + (1-1)^2}$$
$$= \sqrt{1}$$

$$= 1$$

$$(D_3 D_8) = \sqrt{(3-3)^2 + (2-1)^2}$$
$$= \sqrt{1}$$
$$= 1$$

$$(D_3 D_9) = \sqrt{(4-3)^2 + (5-1)^2}$$
$$= \sqrt{1+16}$$
$$= 4.1$$

$$(D_3 D_{10}) = \sqrt{(5-3)^2 + (4-1)^2}$$
$$= \sqrt{4+9}$$
$$= 3.6$$

$$(D_4 D_5) = \sqrt{(5-4)^2 + (1-2)^2}$$
$$= \sqrt{1+1}$$
$$= 1.4$$

$$(D_4 D_6) = \sqrt{(1-4)^2 + (4-2)^2}$$
$$= \sqrt{9+4}$$
$$= 3.6$$

$$(D_4 D_7) = \sqrt{(2-4)^2 + (1-2)^2}$$
$$= \sqrt{4+1}$$
$$= 2.2$$

$$(D_4 D_8) = \sqrt{(3-4)^2 + (2-2)^2}$$
$$= \sqrt{1}$$

$$(D_4 D_9) = \sqrt{(4-4)^2 + (5-2)^2}$$
$$= \sqrt{9}$$
$$= 3$$

$$(D_4 D_{10}) = \sqrt{(5-4)^2 + (4-2)^2}$$
$$= \sqrt{1+4}$$
$$= 2.2$$

$$(D_5 D_6) = \sqrt{(1-5)^2 + (4-1)^2}$$
$$= \sqrt{16+9}$$
$$= \sqrt{25}$$
$$= 5$$

$$(D_5 D_7) = \sqrt{(2-5)^2 + (1-1)^2}$$
$$= \sqrt{9}$$
$$= 3$$

$$(D_5 D_8) = \sqrt{(3-5)^2 + (2-1)^2}$$
$$= \sqrt{4+1}$$
$$= \sqrt{5}$$
$$= 2.2$$

$$(D_5 D_9) = \sqrt{(4-5)^2 + (5-1)^2}$$
$$= \sqrt{1+16}$$
$$= \sqrt{17}$$
$$= 4.1$$

$$(D_5 D_{10}) = \sqrt{(5-5)^2 + (4-1)^2}$$
$$= \sqrt{9}$$
$$= 3$$

$$(D_6 D_7) = \sqrt{(2-1)^2 + (1-4)^2}$$
$$= \sqrt{1+9}$$
$$= \sqrt{10}$$
$$= 3.1$$

$$(D_6 D_8) = \sqrt{(3-1)^2 + (2-4)^2}$$
$$= \sqrt{4+4}$$
$$= \sqrt{8}$$
$$= 2.8$$

$$(D_6 D_9) = \sqrt{(4-1)^2 + (5-4)^2}$$
$$= \sqrt{9+1}$$
$$= \sqrt{10}$$
$$= 3.1$$

$$(D_6 D_{10}) = \sqrt{(5-1)^2 + (4-4)^2}$$
$$= \sqrt{16+0}$$
$$= 4$$

$$(D_7 D_8) = \sqrt{(3-2)^2 + (2-1)^2}$$
$$= \sqrt{1+1}$$
$$= \sqrt{2}$$
$$= 1.4$$

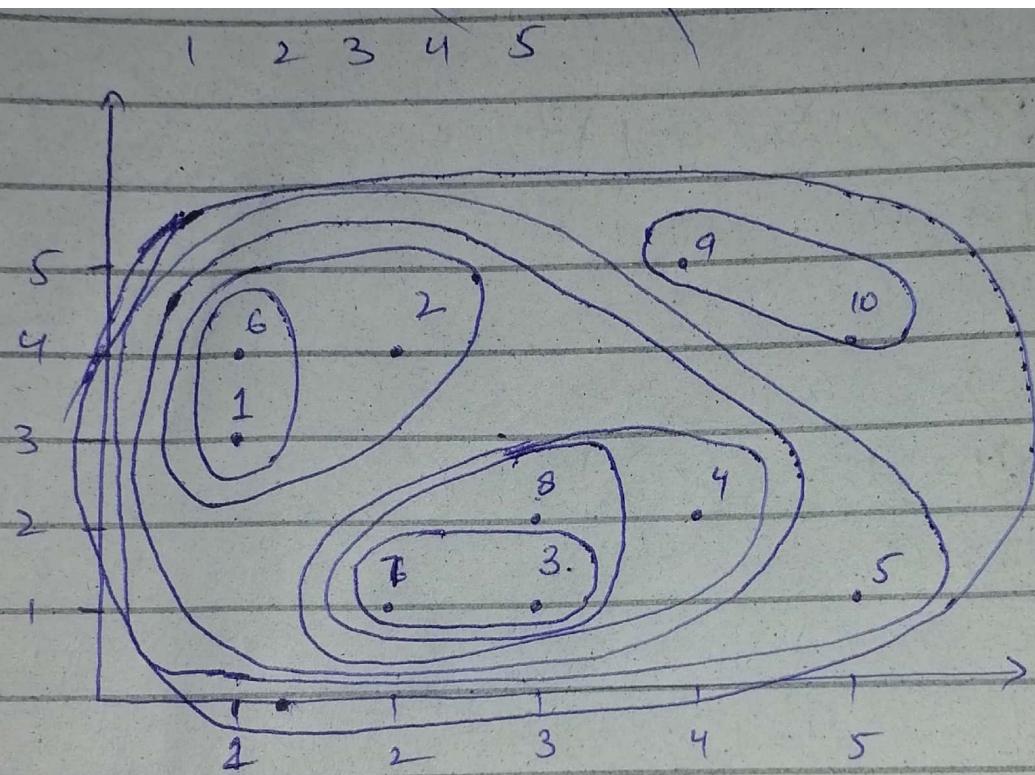
$$(D_7 D_9) = \sqrt{(4-2)^2 + (5-1)^2}$$
$$= \sqrt{4+16}$$
$$= \sqrt{20}$$
$$= 4.4$$

$$(D_7 D_{10}) = \sqrt{(5-2)^2 + (4-1)^2}$$
$$= \sqrt{9+9}$$
$$= \sqrt{18}$$
$$= 4.2$$

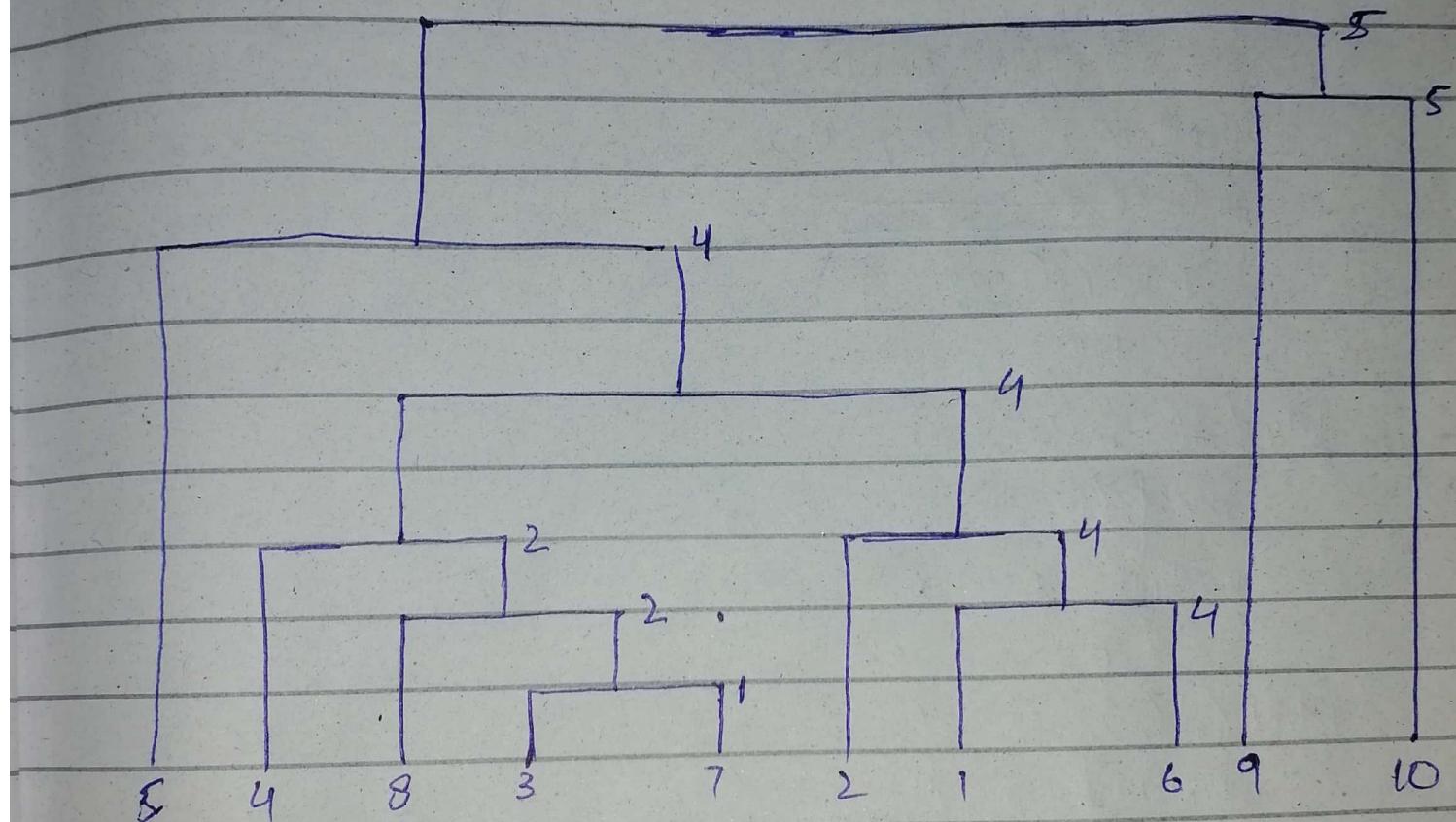
$$(D_8 D_9) = \sqrt{(4-3)^2 + (5-2)^2}$$
$$= \sqrt{1+9}$$
$$= \sqrt{10}$$
$$= 3.1$$

$$(D_8 D_{10}) = \sqrt{(5-3)^2 + (4-2)^2}$$
$$= \sqrt{4+4}$$
$$= \sqrt{8}$$
$$= 2.8$$

$$(D_9 D_{10}) = \sqrt{(5-4)^2 + (4-5)^2}$$
$$= \sqrt{1+1}$$
$$= \sqrt{2}$$
$$= 1.4$$



Clusters for threshold = 3 are 3



FIRST Cluster $\sim D_1, D_6$

To update the distance Matrix

$$\begin{aligned} & \text{MIN}(d(D_1, D_6), D_2) \\ = & \text{MIN}[(D_1, D_2), (D_6, D_2)] \\ = & \underline{\text{MIN}(1, 1.4)} \\ = & \text{MIN}(1.4, 1) \\ = & 1 \end{aligned}$$

$$\begin{aligned} & \text{MIN}(d(D_1, D_6), D_3) \\ = & \text{MIN}[(D_1, D_3), (D_6, D_3)] \\ = & \text{MIN}(2.8, 3.6) \\ = & 2.8 \end{aligned}$$

$$\begin{aligned} & \text{MIN}(d(D_1, D_6), D_4) \\ = & \text{MIN}[(D_1, D_4), (D_6, D_4)] \\ = & \text{MIN}(3.1, 3.6) \\ = & 3.6 \end{aligned}$$

$$\begin{aligned} & \text{MIN}(d(D_1, D_6), D_5) \\ = & \text{MIN}(D_1, D_5), (D_6, D_5) \\ = & \text{MIN}(4.5, 5) \\ = & 4.5 \end{aligned}$$

$$\begin{aligned} & \text{MIN}(d(D_1, D_6), D_7) \\ = & \text{MIN}[(D_1, D_7), (D_6, D_7)] \\ = & \text{MIN}(2.2, 3.1) \\ = & 2.2 \end{aligned}$$

$$\begin{aligned} & \text{MIN}(d(D_1, D_6), D_8) \\ = & \text{MIN}[(D_1, D_8), (D_6, D_8)] \\ = & \text{MIN}(2, 2.8) \\ = & 2 \end{aligned}$$

$$\text{MIN}(d(D_1, D_6), D_9)$$

$$\text{MIN}\{(D_1, D_9), (D_6, D_9)\}$$

$$\text{MIN}(3.6, 3.1)$$

$$= 3.1$$

$$\text{MIN}(d(D_1, D_6), D_{10})$$

$$\text{MIN}\{(D_1, D_{10}), (D_6, D_{10})\}$$

$$\text{MIN}(4.1, 4)$$

4

~~D₆, D₁₀~~

	D ₁ , D ₆	D ₂	D ₃	D ₄	D ₅	D ₇	D ₈	D ₉	D ₁₀
D ₁ , D ₆	0								
D ₂	1	0							
D ₃	2.8	3.1	0						
D ₄	3.6	2.8	1.4	0					
D ₅	4.5	4.2	2	1.4	0				
D ₇	2.2	3	1	2.2	3	0			
D ₈	2	2.2	1	1	2.2	1.4	0		
D ₉	3.1	2.2	4.1	3	4.1	4.4	3.1	0	
D ₁₀	4	3	3.6	2.2	3	4.2	2.8	1.4	0

Select new cluster :- D₁, D₆, D₂

update distance

$$\text{MIN}(d(D_1, D_6, D_2), D_3)$$

$$\text{MIN}\{(D_1, D_6, D_2), (D_3, D_3)\}$$

$$\text{MIN}(2.8, 3.1)$$

$$= 2.8$$

$$\text{MIN}(d(D_1, D_6, D_2), D_4)$$

$$\text{MIN}\{(D_1, D_6, D_2), (D_4, D_4)\}$$

$$\text{MIN}(3.6, 2.8)$$

$$= 2.8$$

$$\text{MIN}((D_1, D_6, D_2), D_5)$$

$$\text{MIN}((D_1, D_6, D_5), (D_2, D_5))$$

$$\text{MIN}(4.5, 4.2)$$

$$= 4.2$$

$$\text{MIN}((D_1, D_6, D_2), D_4)$$

$$\text{MIN}((D_1, D_6, D_4), (D_2, D_4))$$

$$\text{MIN}(2.2, 3)$$

$$= 2.2$$

$$\text{MIN}((D_1, D_6, D_2), D_8)$$

$$\text{MIN}((D_1, D_6, D_8), (D_2, D_8))$$

$$\text{MIN}(2, 2.2)$$

$$= 2$$

$$\text{MIN}((D_1, D_6, D_2), D_9)$$

$$\text{MIN}((D_1, D_6, D_9), (D_2, D_9))$$

$$\text{MIN}(3.1, 2.2)$$

$$= 2.2$$

$$\text{MIN}((D_1, D_6, D_2), D_{10})$$

$$\text{MIN}((D_1, D_6, D_{10}), (D_2, D_{10}))$$

$$\text{MIN}(4, 3)$$

$$= 3$$

	D ₁ , D ₆ , D ₂	D ₃	D ₄	D ₈	D ₉	D ₈	D ₉	D ₁₀
D ₁ , D ₆ , D ₂	0							
D ₃	2.8	0						
D ₄	2.8	1.4	0					
D ₅	4.2	2	1.4	0				
D ₇	2.2	1	2.2	3	0			
D ₉	2	1	4.1	2.2	1.4	0		
D ₉	2.2	4.1	3	4.1	4.4	3.1	0	
D ₁₀	3	3.6	2.2	3	4.2	2.8	1.4	0

Select New clusters:- D_3, D_7

Update distance

$$\text{MIN} \{(D_3, D_7), (D_1, D_6, D_2)\}$$

$$\text{MIN} \{(D_3, (D_1, D_6, D_2)), (D_7, (D_1, D_6, D_2))\}$$

$$\text{MIN} (2.8, 2.2)$$

$$= 2.2$$

$$\text{MIN} ((D_3, D_7), D_4)$$

$$\text{MIN} \{(D_3, D_4), (D_7, D_4)\}$$

$$\text{MIN} (1.4, 2.2)$$

$$= 1.4$$

$$\text{MIN} ((D_3, D_7), D_5)$$

$$\text{MIN} \{(D_3, D_5), (D_7, D_5)\}$$

$$\text{MIN} (2, 3)$$

$$= 3$$

$$\text{MIN} ((D_3, D_7), D_8)$$

$$\text{MIN} \{(D_3, D_8), (D_7, D_8)\}$$

$$\text{MIN} (1, 1.4)$$

$$= 1$$

$$\text{MIN} ((D_3, D_7), D_9)$$

$$\text{MIN} ((D_3, D_9), (D_7, D_9))$$

$$\text{MIN} (4.1, 4.4)$$

$$= 2 \cancel{4} 4.1$$

$$\text{MIN} ((D_3, D_7), D_{10})$$

$$\text{MIN} \{(D_3, D_{10}), (D_7, D_{10})\}$$

$$\text{MIN} (3.6, 4.2)$$

$$= 3.6$$

	D_1, D_6, D_2	D_3, D_7	D_4	D_5	D_8	D_9	D_{10}
D_1, D_6, D_2	2.0						
D_3, D_7	2.2	0					
D_5	1.8	1.4	0				
D_8	4.2	3	1.4	0			
D_8	2	1	1	2.2	0		
D_9	2.2	4.1	3	4.1	3.1	0	
D_{10}	3	3.6	2.2	3	2.8	1.4	0

Select New clusters:- D_3, D_7, D_8

Update distance

$$\text{MIN}[(D_3, D_7, D_8), (D_1, D_6, D_2)]$$

$$\text{MIN}[(D_3, D_7), (D_1, D_6, D_2)], (D_8, (D_1, D_6, D_2))]$$

$$\text{MIN}[(2.2, 1.8)]$$

$$= 2$$

$$\text{MIN}[(D_3, D_7, D_8), D_9]$$

$$\text{MIN}[(D_3, D_7, D_8), (D_8, D_4)]$$

$$\text{MIN}(1.4, 1)$$

$$= 1$$

$$\text{MIN}[(D_3, D_7, D_8), D_5]$$

$$\text{MIN}[(D_3, D_7, D_8), (D_9, D_5)]$$

$$\text{MIN}(3, 2.2)$$

$$= 2.2$$

$$\text{MIN}[(D_3, D_7, D_8), D_9]$$

$$\text{MIN}[(D_3, D_7, D_9), (D_8, D_9)]$$

$$\text{MIN}(4.1, 3.1)$$

$$= 3.1$$

$$\begin{aligned} & \text{MIN} \{ (D_3, D_7, D_8), D_{10} \} \\ & \text{MIN} \{ (D_3, D_7, D_{10}), (D_8, D_{10}) \} \\ & \text{MIN} (3.6, 2.8) \\ & \approx 2.8 \end{aligned}$$

	D ₁ , D ₆ , D ₂	D ₃ , D ₇ , D ₈	D ₄	D ₅	D ₉	D ₁₀
D ₁ , D ₆ , D ₂	0					
D ₃ , D ₇ , D ₈	2	0				
D ₄	2.8	11	0			
D ₅	4.2	2.2	1.4	0		
D ₉	2.2	3.1	3	4.1	0	
D ₁₀	3	2.8	2.2	3	1.4	0

Select New clusters :- D₃, D₇, D₈, D₄
 Update Distance

$$\begin{aligned} & \text{MIN} \{ (D_3, D_7, D_8, D_4), (D_1, D_6, D_2) \} \\ & \text{MIN} \{ ((D_3, D_7, D_8), (D_1, D_6, D_2)), ((D_4, D_5, D_9, D_{10})) \} \\ & \text{MIN} (2, 2.8) \\ & \approx 2 \end{aligned}$$

$$\begin{aligned} & \text{MIN} \{ (D_3, D_7, D_8, D_4); D_5 \} \\ & \text{MIN} \{ (D_3, D_7, D_8, D_5), (D_9, D_{10}) \} \\ & \text{MIN} (2.2, 1.4) \\ & \approx 1.4 \end{aligned}$$

$$\begin{aligned} & \text{MIN} \{ (D_3, D_7, D_8, D_4), D_9 \} \\ & \text{MIN} \{ (D_3, D_7, D_8, D_9), (D_4, D_5) \} \\ & \text{MIN} (3.1, 3) \\ & \approx 3 \end{aligned}$$

$$\begin{aligned} & \text{MIN} \{ (D_3, D_7, D_8, D_4), D_{10} \} \\ & \text{MIN} \{ (D_3, D_7, D_8, D_{10}), (D_9, D_{10}) \} \\ & \text{MIN} (2.8, 2.2) \\ & \approx 2.2 \end{aligned}$$

D_1	D_2, D_6	D_3, D_7, D_8, D_4	D_5	D_9	D_{10}
D_1, D_2, D_6	0				
D_3, D_7, D_8, D_4	2	0			
D_5	4.2	1.4	0		
D_9	2.2	3	4.1	0	
D_{10}	3	2.2	3	1.4	0

Select New cluster :- $D_1, D_2, D_6, D_3, D_7, D_8, D_4$

Update Distance

$$\text{MIN}[(D_1, D_2, D_6, D_3, D_7, D_8, D_4), D_5]$$

$$\text{MIN}[(D_1, D_2, D_6, D_5), (D_3, D_7, D_8, D_4, D_5)]$$

$$\text{MIN}(4.2, 1.4)$$

$$= 1.4$$

$$\text{MIN}[(D_1, D_2, D_6, D_3, D_7, D_8, D_4), D_9]$$

$$\text{MIN}[(D_1, D_2, D_6, D_9), (D_3, D_7, D_8, D_4, D_9)]$$

$$\text{MIN}(2.2, 3)$$

$$= 2.2$$

$$\text{MIN}[(D_1, D_2, D_6, D_3, D_7, D_8, D_4), D_{10}]$$

$$\text{MIN}[(D_1, D_2, D_6, D_{10}), (D_3, D_7, D_8, D_4, D_{10})]$$

$$\text{MIN}(3, 2.2)$$

$$= 2.2$$

$D_1, D_2, D_6, D_3, D_7, D_8, D_4$	$D_1, D_2, D_6, D_3, D_7, D_8, D_4$	D_5	D_9	D_{10}
D_5	0			
D_9	1.4	0		
D_{10}	2.2	4.1	0	

Select new cluster:-

$D_1, D_2, D_6, D_3, D_7, D_8, D_4, D_5$

$$D_{\Delta} = D_1, D_2, D_6, D_3, D_7, D_8; D_9$$

Update Distance

$$\text{MIN} \{ (D_{\Delta}, D_5), D_9 \}$$

$$\text{MIN} \{ (D_{\Delta}, D_9), (D_5, D_9) \}$$

$$\text{MIN} (2.2, 4.1)$$

$$= 2.2$$

$$\text{MIN} \{ (D_{\Delta}, D_5), D_{10} \}$$

$$\text{MIN} \{ (D_{\Delta}, D_{10}), (D_5, D_{10}) \}$$

$$\text{MIN} (2.2, 3)$$

$$= 2.2$$

Step 3

$$D_{\Delta} = D_1, D_2, D_6, D_3, D_7, D_8, D_4, D_5$$

	D_{Δ}	D_9	D_{10}
D_{Δ}	0		
D_9	2.2	0	
D_{10}	2.2	1.4	0

Select New clusters - D_9, D_{10}

Update Distance

$$\text{MIN} \{ (D_9, D_{10}), D_{\Delta} \}$$

$$\text{MIN} \{ (D_9, D_{\Delta}), (D_{10}, D_{\Delta}) \}$$

$$\text{MIN} (2.2, 2.2)$$

$$= 2.2$$

	D_{Δ}	D_9, D_{10}
D_{Δ}	0	
D_9, D_{10}	2.2	0

Select New clusters - D_{Δ}, D_9, D_{10}