

PRESENTATION OF DATA

⇒ Methods

→ Textual Method

Rearrange from lowest to highest
Stem & leaf plot

→ Tabular Method

Frequency Distribution

Commutative Frequency Distribution

Percentage Frequency Distribution

→ Graphs

Histogram

Frequency Polygon

Frequency Curve

MEASURES OF CENTRAL TENDENCY

⇒ Arithmetic Mean

→ Population

$$\mu = \frac{X_1 + X_2 + X_3 + \dots + X_n}{N}$$

→ Sample

$$\bar{X} = \frac{X_1 + X_2 + \dots + X_n}{n}$$

⇒ Geometric Mean

$$G.M = \frac{(X_1 \cdot X_2 \cdot X_3 \cdot \dots \cdot X_n)^{1/N}}{N} \quad \text{OR} \quad \left[\prod_{i=1}^N X_i \right]^{1/N}$$

$$\text{OR } G.M = \text{Antilog} \left[\frac{\sum_{i=1}^N \log x_i}{N} \right]$$

\Rightarrow Harmonic Mean

$$\frac{N}{\frac{1}{x_1} + \frac{1}{x_2} + \frac{1}{x_3} + \dots + \frac{1}{x_n}}$$

OR

$$\frac{N}{\sum_{i=1}^N \left(\frac{1}{x_i} \right)}$$

\Rightarrow Median

Mid Value after sorting

\Rightarrow Mode

Most repeated value.

MEASURES OF DISPERSION

\Rightarrow ABSOLUTE MEASURES

\Rightarrow Range

$$X_{\max} - X_{\min}$$

\Rightarrow Mean Deviation (M.D)

Population

$$M.D = \frac{\sum_{i=1}^N |x_i - \mu|}{N}$$

Sample

$$M.D = \frac{\sum_{i=1}^n |x_i - \bar{x}|}{n}$$

→ Variance

$$\sigma^2 = \frac{\sum_{i=1}^N (X_i - \mu)^2}{N} \rightarrow \text{Population}$$

$$\sigma^2 = \frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n} \rightarrow \text{Sample}$$

→ Standard Deviation (S.D)

$$\sigma = \sqrt{\text{Variance}}$$

OR

$$\sigma = \sqrt{\frac{\sum_{i=1}^N (X_i - \mu)^2}{N}} \Rightarrow \text{Population}$$

$$\sigma = \sqrt{\frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n}} \Rightarrow \text{Sample}$$

⇒ RELATIVE MEASURES

→ Coeff of Range

$$\frac{X_{\max} - X_{\min}}{X_{\max} + X_{\min}}$$

→ Coeff of Mean Deviation (M.D)

$$\frac{\text{M.D}}{\text{Mean}} \times 100$$

→ Coeff of Variance

$$\frac{\text{Standard Deviation}}{\text{Mean}} \times 100$$

⇒ ABSOLUTE MEASURES OF SKEWNESS

→ Symmetric

$$\text{Mean} = \text{Median} = \text{Mode}$$

$$\text{Mean} - \text{Median} = 0$$

$$\text{Mean} - \text{Mode} = 0$$

→ Positive/Right Skewed

$$\text{Mean} > \text{Median} > \text{Mode}$$

$$\text{Mean} - \text{Median} > 0$$

$$\text{Mean} - \text{Mode} > 0$$

→ Negative/Left Skewed

$$\text{Mean} < \text{Median} < \text{Mode}$$

$$\text{Mean} - \text{Median} < 0$$

$$\text{Mean} - \text{Mode} < 0$$

⇒ PEARSON COEFF OF SKEWNESS

$$SKP = \frac{\text{Mean} - \text{Mode}}{\text{Standard Deviation}}$$

$$\text{OR } \frac{3(\text{Mean} - \text{Mode})}{S.D.}$$

$$\beta_1 = \frac{\mu_3^2}{\mu_2^3}$$

$$\beta_2 = \frac{\mu_4}{\mu_2^2}$$

\Rightarrow MOMENTS

$\rightarrow r^{\text{th}}$ Moment about Mean

$$\mu_r = \frac{(x_i - \mu)^r}{N}$$

$$\mu_1 = \frac{(x_i - \mu)}{N}$$

$$\mu_2 = \frac{(x_i - \mu)^2}{N} = \sigma^2$$

$$\mu_3 = \frac{(x_i - \mu)^3}{N}$$

$$\mu_4 = \frac{(x_i - \mu)^4}{N}$$

→ Coeff of Skewness

$$\gamma_1 = \sqrt{\beta_1}$$

OR

$$\gamma_1 = \frac{\sqrt{\mu_3^2}}{\sqrt{\mu_2^3}}$$

OR

$$\gamma_1 = \frac{\mu_3}{\mu_2^{3/2}}$$

⇒ MEASURES OF KURTOSIS

$$\gamma_2 = \beta_2 - 3$$

OR

$$\gamma_2 = \frac{\mu_4}{\mu_2^2} - 3$$

$$\therefore \mu_2 = \sigma^2$$

OR

$$\gamma_2 = \frac{\mu_4}{\sigma^4} - 3$$

$\gamma_2 > 0 \rightarrow$ leptokurtic

$\gamma_2 = 0 \rightarrow$ Mesokurtic

$\gamma_2 < 0 \rightarrow$ Platykurtic