

Coupled Equations:

$$C_{\text{el}} \frac{\partial}{\partial t} T_{\text{el}}(t, z) = \frac{\partial}{\partial z} \kappa \frac{\partial}{\partial z} T_{\text{el}}(t, z) - g[T_{\text{el}}(t, z) - T_{\text{ph}}(t, z)] + S(t, z)$$

$$C_{\text{ph}} \frac{\partial}{\partial t} T_{\text{ph}}(t, z) = g[T_{\text{el}}(t, z) - T_{\text{ph}}(t, z)]$$

$$\frac{dU_{\text{ads}}}{dt} = \eta_{\text{el}}(U_{\text{el}} - U_{\text{ads}}) + \eta_{\text{ph}}(U_{\text{ph}} - U_{\text{ads}})$$

$$U_q = \frac{h\nu_{rc}}{\exp(h\nu_{rc}/k_B T_q) - 1}$$

$$T_{\text{ads}} = \frac{h\nu_{\text{ads}}}{k_B \ln\left(\frac{h\nu_{\text{ads}}}{U_{\text{ads}}} + 1\right)}$$

$$d\theta/dt = \nu_{PW}\theta(t)\exp(-E_a/k_B T_{\text{ads}})$$

Source:  $S(z, t) = \frac{1}{2B\lambda_z} \exp\left(-\frac{z}{\lambda_z}\right) \left[ F_1 \operatorname{sech}^2\left(\frac{t - t_1}{B}\right) + F_2 \operatorname{sech}^2\left(\frac{t - t_2}{B}\right) \right]$

