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method ComputeFusc(N: int) returns (b: int)
  requires N >= 0
  ensures b == fusc(N)
{
  {true}

  {fusc(N) == fusc(N)}

  {fusc(N) == fusc(N) + 0 * fusc(N + 1)}

  b := 0;

  {fusc(N) == fusc(N) + b * fusc(N + 1)}

  {forall n :: fusc(N) == fusc(N) + b * fusc(N + 1)}

  var n := N;

  {fusc(N) == fusc(n) + b * fusc(n + 1)}

  {forall a :: 1 * fusc(N) == fusc(n) + b * fusc(n + 1)}

  var a := 1

  {fusc(N) == a * fusc(n) + b * fusc(n + 1)}

  while (n != 0)
    invariant fusc(N) == a * fusc(n) + b * fusc(n + 1)
    decreases n
    {
      {fusc(N) == a * fusc(n) + b * fusc(n + 1)} // strengthen (A || A == B -> A
as this reduces sample space of A)

      {fusc(N) == a * fusc(n) + b * fusc(n + 1) || a * fusc(n) + b * fusc(n + 1)
== a * fusc(n) + b * fusc((n + 1) / 2)}

      {(fusc(N) == a * fusc(n) + b * fusc(n + 1) && (n % 2 == 0 || n % 2 == 1))
||
      (fusc(N) == a * fusc(n) + b * fusc(n + 1) &&
fusc(N) == a * fusc(n) + b * fusc((n + 1) / 2))

      {false || (n % 2 == 1 && fusc(N) == a * fusc(n) + b * fusc(n + 1) ||
(fusc(N) == a * fusc(n) + b * fusc(n + 1) && n % 2 == 0) ||
(fusc(N) == a * fusc(n) + b
* fusc(n + 1) && fusc(N) == a * fusc(n) + b * fusc((n + 1) / 2))

      {(n % 2 == 1 && n % 2 == 0) || (n % 2 == 1 && fusc(N) == a * fusc(n) + b *
fusc(n + 1) / 2) ||
      (fusc(N) == a * fusc(n) + b * fusc(n + 1) && n % 2 ==
0) || (fusc(N) == a * fusc(n) + b * fusc(n + 1) && fusc(N) == a * fusc(n) + b *

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fusc(n + 1) / 2)}

{(n % 2 == 1 || fusc(N) == a \* fusc(n) + b \* fusc(n + 1)) && (n % 2 == 0 ||  
fusc(N) == a \* fusc(n) + b \* fusc(n + 1) / 2)}

{n % 2 == 0 ==> fusc(N) == a \* fusc(n) + b \* fusc(n + 1) && n % 2 == 1 ==>  
fusc(N) == a \* fusc(n) + b \* fusc(n + 1) / 2)}

if (n % 2 == 0) {

{fusc(N) == a \* fusc(n) + b \* fusc(n + 1)} -- as an input of a  
number (n) with a multiple of 2 is equal to an input of itself (n) {rule iii}

{fusc(N) == a \* fusc(n / 2) + b \* fusc(n + 1)}

{fusc(N) == a \* fusc(n / 2) + b \* fusc(2 \* (n / 2) + 1)}

{fusc(N) == a \* fusc(n / 2) + b \* fusc(n / 2) + b \* fusc((n / 2) + 1)}

{fusc(N) == (a + b) \* fusc(n / 2) + b \* fusc((n / 2) + 1)}

a := a + b;

{fusc(N) == a \* fusc(n / 2) + b \* fusc((n / 2) + 1)}

n := n / 2;

{fusc(N) == a \* fusc(n) + b \* fusc(n + 1)}

} else {

{fusc(N) == a \* fusc(n) + b \* fusc((n + 1) / 2)}

{fusc(N) == a \* (fusc(2 \* ((n - 1) / 2) + 1)) + b \* fusc((n + 1) / 2)}

{fusc(N) == a \* (fusc((n - 1) / 2) + fusc(((n - 1) / 2) + 1)) + b \*  
fusc((n + 1) / 2)}

{fusc(N) == a \* fusc((n - 1) / 2) + a \* fusc(((n - 1) / 2) + 1) + b \*  
fusc((n + 1) / 2)}

{fusc(N) == a \* fusc((n - 1) / 2) + a \* (fusc(((n - 1) / 2) + 1) + b \*  
fusc(((n - 1) / 2) + 1)}

{fusc(N) == a \* fusc((n - 1) / 2) + (b + a) \* fusc(((n - 1) / 2) + 1)}

b := b + a;

{fusc(N) == a \* fusc((n - 1) / 2) + b \* fusc(((n - 1) / 2) + 1)}

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    {fusc(N) == a * fusc((n - 1) / 2) + b * fusc(((n - 1) / 2) + 1)}

    n := (n - 1) / 2;

    {fusc(N) == a * fusc(n) + b * fusc(n + 1)}

  }

  {fusc(N) == a * fusc(n) + b * fusc(n + 1)}

}

{fusc(N) == a * fusc(n) + b * fusc(n + 1) && n == 0}
}

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