

Hints

- Without the Sbox, all operations preserve bit-wise linearity. In other words, if a block of plaintext has 128 bits b_1, b_2, \dots, b_{128} , then every single ciphertext bit has the form

$$c_0 + c_1b_1 + c_2b_2 + \dots + c_{128}b_{128}$$

- It's possible to find c_1, c_2, \dots, c_{128} without knowing the key, or you can recover all c_i from the plaintext-ciphertext pairs.
- If you have issues solving linear equations in booleans in python, try python package `galois` (<https://github.com/mhostetter/galois>):

```
import numpy as np
import galois

GF2 = galois.GF(2) # create the binary field
M = GF2([[0, 1], [1, 0]]) # build a 2x2 matrix
v = GF2([1, 0]) # build a vector of length 2
solution = np.linalg.solve(M, v) # solve linear equation Mx = v
first_number = int(solution[0]) # get the first entry of the solution
```