Personalized cancer diagnosis

Assignment 4-

Try any of the feature engineering techniques discussed in the course to reduce the CV and test log-loss to a value less than 1.0.

1. Business Problem

1.1. Description

Source: https://www.kaggle.com/c/msk-redefining-cancer-treatment/

Data: Memorial Sloan Kettering Cancer Center (MSKCC)

Download training_variants.zip and training_text.zip from Kaggle.

Context:

Source: https://www.kaggle.com/c/msk-redefining-cancer-treatment/discussion/35336#198462

Problem statement:

Classify the given genetic variations/mutations based on evidence from text-based clinical literature.

1.2. Source/Useful Links

Some articles and reference blogs about the problem statement

- 1. https://www.forbes.com/sites/matthewherper/2017/06/03/a-new-cancer-drug-helped-almost-everyone-who-took-it-almost-heres-what-it-teaches-us/#2a44ee2f6b25
- 2. https://www.youtube.com/watch?v=UwbuW7oK8rk
- 3. https://www.youtube.com/watch?v=qxXRKVompl8

1.3. Real-world/Business objectives and constraints.

- · No low-latency requirement.
- · Interpretability is important.
- Errors can be very costly.
- · Probability of a data-point belonging to each class is needed.

2. Machine Learning Problem Formulation

2.1. Data

2.1.1. Data Overview

- Source: https://www.kaggle.com/c/msk-redefining-cancer-treatment/data
- We have two data files: one conatins the information about the genetic mutations and the other contains the clinical evidence (text) that human experts/pathologists use to classify the genetic mutations.
- Roth those data files are have a common column called ID.

- DULLI LITESE UALA IITES ALE HAVE A COMITION COIUMIN CAREU ID
- · Data file's information:
 - training_variants (ID, Gene, Variations, Class)
 - training text (ID, Text)

2.1.2. Example Data Point

training_variants

ID,Gene,Variation,Class 0,FAM58A,Truncating Mutations,1 1,CBL,W802*,2 2,CBL,Q249E,2

training_text

ID,Text

0||Cyclin-dependent kinases (CDKs) regulate a variety of fundamental cellular processes. CDK10 stands out as one of the last orphan CDKs for which no activating cyclin has been identified and no kinase activity revealed. Previous work has shown that CDK10 silencing increases ETS2 (v-ets erythroblastosis virus E26 oncogene homolog 2)-driven activation of the MAPK pathway, which confers tamoxifen resistance to breast cancer cells. The precise mechanisms by which CDK10 modulates ETS2 activity, and more generally the functions of CDK10, remain elusive. Here we demonstrate that CDK10 is a cyclin-dependent kinase by identifying cyclin M as an activating cyclin. Cyclin M, an orphan cyclin, is the product of FAM58A, whose mutations cause STAR syndrome, a human developmental anomaly whose features include toe syndactyly, telecanthus, and anogenital and renal malformations. We show that STAR syndrome-associated cyclin M mutants are unable to interact with CDK10. Cyclin M silencing phenocopies CDK10 silencing in increasing c-Raf and in conferring tamoxifen resistance to breast cancer cells. CDK10/cyclin M phosphorylates ETS2 in vitro, and in cells it positively controls ETS2 degradation by the proteasome. ETS2 protein levels are increased in cells derived from a STAR patient, and this increase is attributable to decreased cyclin M levels. Altogether, our results reveal an additional regulatory mechanism for ETS2, which plays key roles in cancer and development. They also shed light on the molecular mechanisms underlying STAR syndrome. Cyclin-dependent kinases (CDKs) play a pivotal role in the control of a number of fundamental cellular processes (1). The human genome contains 21 genes encoding proteins that can be considered as members of the CDK family owing to their sequence similarity with bona fide CDKs, those known to be activated by cyclins (2). Although discovered almost 20 y ago (3, 4), CDK10 remains one of the two CDKs without an identified cyclin partner. This knowledge gap has largely impeded the exploration of its biological functions. CDK10 can act as a positive cell cycle regulator in some cells (5, 6) or as a tumor suppressor in others (7, 8). CDK10 interacts with the ETS2 (v-ets erythroblastosis virus E26 oncogene homolog 2) transcription factor and inhibits its transcriptional activity through an unknown mechanism (9). CDK10 knockdown derepresses ETS2, which increases the expression of the c-Raf protein kinase, activates the MAPK pathway, and induces resistance of MCF7 cells to tamoxifen (6). ...

2.2. Mapping the real-world problem to an ML problem

2.2.1. Type of Machine Learning Problem

There are nine different classes a genetic mutation can be classified into => Multi class classification problem

2.2.2. Performance Metric

Source: https://www.kaggle.com/c/msk-redefining-cancer-treatment#evaluation

Metric(s):

- · Multi class log-loss
- Confusion matrix

2.2.3. Machine Learing Objectives and Constraints

Objective: Predict the probability of each data-point belonging to each of the nine classes.

Constraints:

- Interpretability
- · Class probabilities are needed.
- Penalize the errors in class probabilites => Metric is Log-loss.
- · No Latency constraints.

2.3. Train, CV and Test Datasets

Split the dataset randomly into three parts train, cross validation and test with 64%,16%, 20% of data respectively

3. Exploratory Data Analysis

```
In [1]:
```

```
import pandas as pd
import matplotlib.pyplot as plt
import re
import time
import warnings
import numpy as np
from nltk.corpus import stopwords
from sklearn.decomposition import TruncatedSVD
from sklearn.preprocessing import normalize
from sklearn.feature_extraction.text import CountVectorizer
from sklearn.manifold import TSNE
import seaborn as sns
from sklearn.neighbors import KNeighborsClassifier
from sklearn.metrics import confusion_matrix
from sklearn.metrics.classification import accuracy score, log loss
from sklearn.feature extraction.text import TfidfVectorizer
from sklearn.linear model import SGDClassifier
from imblearn.over_sampling import SMOTE
from collections import Counter
from scipy.sparse import hstack
from sklearn.multiclass import OneVsRestClassifier
from sklearn.svm import SVC
from sklearn.model selection import StratifiedKFold
from collections import Counter, defaultdict
from sklearn.calibration import CalibratedClassifierCV
from sklearn.naive bayes import MultinomialNB
from sklearn.naive bayes import GaussianNB
from sklearn.model_selection import train_test_split
from sklearn.model selection import GridSearchCV
import math
from sklearn.metrics import normalized mutual info score
from sklearn.ensemble import RandomForestClassifier
warnings.filterwarnings("ignore")
from mlxtend.classifier import StackingClassifier
from sklearn import model selection
from sklearn.linear_model import LogisticRegression
```

3.1. Reading Data

3.1.1. Reading Gene and Variation Data

```
In [2]:
```

```
data = pd.read_csv('E:\\Machine Learning\\Assignments\\Personalized_Cancer_Diagnosis\\Data\\traini
ng_variants')
print('Number of data points : ', data.shape[0])
print('Number of features : ', data.shape[1])
print('Features : ', data.columns.values)
```

```
Number of data points : 3321
Number of features : 4
Features : ['ID' 'Gene' 'Variation' 'Class']
Out[2]:
```

	ID	Gene	Variation	Class
0	0	FAM58A	Truncating Mutations	1
1	1	CBL	W802*	2
2	2	CBL	Q249E	2
3	3	CBL	N454D	3
4	4	CBL	L399V	4

training/training_variants is a comma separated file containing the description of the genetic mutations used for training. Fields are

- ID: the id of the row used to link the mutation to the clinical evidence
- Gene: the gene where this genetic mutation is located
- Variation: the aminoacid change for this mutations
- Class: 1-9 the class this genetic mutation has been classified on

3.1.2. Reading Text Data

```
In [3]:
```

```
# note the seprator in this file
data text =pd.read csv("E:\\Machine Learning\\Assignments\\Personalized Cancer Diagnosis\\Data\\tr
aining text",sep="\|\|",engine="python",names=["ID","TEXT"],skiprows=1)
print('Number of data points : ', data_text.shape[0])
print('Number of features : ', data text.shape[1])
print('Features : ', data_text.columns.values)
data_text.head()
Number of data points: 3321
Number of features : 2
Features : ['ID' 'TEXT']
Out[3]:
   ID
                                       TEXT
       Cyclin-dependent kinases (CDKs) regulate a var...
   1
        Abstract Background Non-small cell lung canc...
 1
2 2
         Abstract Background Non-small cell lung canc...
              Recent evidence has demonstrated that
 3 3
                                   acquired...
         Oncogenic mutations in the monomeric Casitas
```

3.1.3. Preprocessing of text

```
In [4]:
```

```
# loading stop words from nltk library
stop_words = set(stopwords.words('english'))

def nlp_preprocessing(total_text, index, column):
    if type(total text) is not int:
```

```
string = ""
# replace every special char with space
total_text = re.sub('[^a-zA-Z0-9\n]', ' ', total_text)
# replace multiple spaces with single space
total_text = re.sub('\s+',' ', total_text)
# converting all the chars into lower-case.
total_text = total_text.lower()

for word in total_text.split():
# if the word is a not a stop word then retain that word from the data
    if not word in stop_words:
        string += word + " "

data_text[column][index] = string
```

In [5]:

```
#text processing stage.
start_time = time.clock()
for index, row in data_text.iterrows():
    if type(row['TEXT']) is str:
        nlp_preprocessing(row['TEXT'], index, 'TEXT')
    else:
        print("there is no text description for id:",index)
print('Time took for preprocessing the text :',time.clock() - start_time, "seconds")

there is no text description for id: 1109
```

```
there is no text description for id: 1277
there is no text description for id: 1407
there is no text description for id: 1639
there is no text description for id: 2755
Time took for preprocessing the text: 186.522559797 seconds
```

In [6]:

```
#merging both gene_variations and text data based on ID
result = pd.merge(data, data_text,on='ID', how='left')
result.head()
```

Out[6]:

TEXT	Class	Variation	Gene	ID	
cyclin dependent kinases cdks regulate variety	1	Truncating Mutations	FAM58A	0	0
abstract background non small cell lung cancer	2	W802*	CBL	1	1
abstract background non small cell lung cancer	2	Q249E	CBL	2	2
recent evidence demonstrated acquired uniparen	3	N454D	CBL	3	3
oncogenic mutations monomeric casitas b lineag	4	L399V	CBL	4	4

In [7]:

```
result[result.isnull().any(axis=1)]
```

Out[7]:

	ID	Gene	Variation	Class	TEXT
1109	1109	FANCA	S1088F	1	NaN
1277	1277	ARID5B	Truncating Mutations	1	NaN
1407	1407	FGFR3	K508M	6	NaN
1639	1639	FLT1	Amplification	6	NaN
2755	2755	BRAF	G596C	7	NaN

In [8]:

```
result.loc[result['TEXT'].lsnull(),'TEXT'] = result['Gene'] +' '+result['Variation']

In [9]:

result[result['ID']==1109]

Out[9]:

ID Gene Variation Class TEXT
```

3.1.4. Test, Train and Cross Validation Split

S1088F

3.1.4.1. Splitting data into train, test and cross validation (64:20:16)

1 FANCA S1088F

```
In [10]:
```

1109 1109 FANCA

```
from sklearn.model_selection import train_test_split
y_true = result['Class'].values
result.Gene = result.Gene.str.replace('\s+', '_')
result.Variation = result.Variation.str.replace('\s+', '_')

# split the data into test and train by maintaining same distribution of output varaible 'y_true'
[stratify=y_true]
X_train, test_df, y_train, y_test = train_test_split(result, y_true, stratify=y_true, test_size=0.2)
# split the train data into train and cross validation by maintaining same distribution of output
varaible 'y_train' [stratify=y_train]
train_df, cv_df, y_train, y_cv = train_test_split(X_train, y_train, stratify=y_train, test_size=0.2)
```

We split the data into train, test and cross validation data sets, preserving the ratio of class distribution in the original data set

```
In [11]:
```

```
print('Number of data points in train data:', train_df.shape[0])
print('Number of data points in test data:', test_df.shape[0])
print('Number of data points in cross validation data:', cv_df.shape[0])

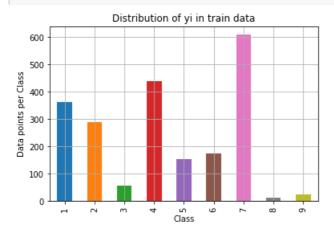
Number of data points in train data: 2124
Number of data points in test data: 665
Number of data points in cross validation data: 532
```

3.1.4.2. Distribution of y_i's in Train, Test and Cross Validation datasets

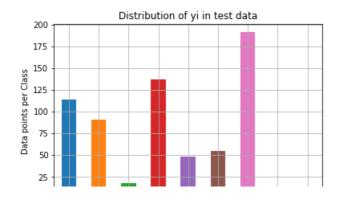
In [12]:

```
# it returns a dict, keys as class labels and values as the number of data points in that class
train class distribution = train df['Class'].value counts().sortlevel()
test class distribution = test df['Class'].value counts().sortlevel()
cv class distribution = cv df['Class'].value counts().sortlevel()
my_colors = 'rgbkymc'
train class_distribution.plot(kind='bar')
plt.xlabel('Class')
plt.ylabel('Data points per Class')
plt.title('Distribution of yi in train data')
plt.grid()
plt.show()
# ref: argsort https://docs.scipy.org/doc/numpy/reference/generated/numpy.argsort.html
# -(train class distribution.values): the minus sign will give us in decreasing order
sorted yi = np.argsort(-train class distribution.values)
for i in sorted yi:
   print('Number of data points in class', i+1, ':', train class distribution.values[i], '(', np.ro
und((train class distribution.values[i]/train df.shape[0]*100), 3), '%)')
```

```
print('-'*80)
my colors = 'rgbkymc'
test_class_distribution.plot(kind='bar')
plt.xlabel('Class')
plt.ylabel('Data points per Class')
plt.title('Distribution of yi in test data')
plt.grid()
plt.show()
# ref: argsort https://docs.scipy.org/doc/numpy/reference/generated/numpy.argsort.html
# -(train class distribution.values): the minus sign will give us in decreasing order
sorted yi = np.argsort(-test class distribution.values)
for i in sorted yi:
    print('Number of data points in class', i+1, ':',test class distribution.values[i], '(', np.rou
nd((test class distribution.values[i]/test df.shape[0]*100), 3), '%)')
print('-'*80)
my colors = 'rgbkymc'
cv_class_distribution.plot(kind='bar')
plt.xlabel('Class')
plt.ylabel('Data points per Class')
plt.title('Distribution of yi in cross validation data')
plt.grid()
plt.show()
# ref: argsort https://docs.scipy.org/doc/numpy/reference/generated/numpy.argsort.html
# -(train class distribution.values): the minus sign will give us in decreasing order
sorted_yi = np.argsort(-train_class_distribution.values)
for i in sorted yi:
   print('Number of data points in class', i+1, ':',cv class distribution.values[i], '(', np.round
((cv_class_distribution.values[i]/cv_df.shape[0]*100), 3), '%)')
```



```
Number of data points in class 7 : 609 ( 28.672 %) Number of data points in class 4 : 439 ( 20.669 %) Number of data points in class 1 : 363 ( 17.09 %) Number of data points in class 2 : 289 ( 13.606 %) Number of data points in class 6 : 176 ( 8.286 %) Number of data points in class 5 : 155 ( 7.298 %) Number of data points in class 3 : 57 ( 2.684 %) Number of data points in class 9 : 24 ( 1.13 %) Number of data points in class 8 : 12 ( 0.565 %)
```



```
Number of data points in class 7: 191 (28.722 %)

Number of data points in class 4: 137 (20.602 %)

Number of data points in class 1: 114 (17.143 %)

Number of data points in class 2: 91 (13.684 %)

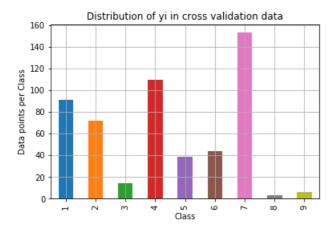
Number of data points in class 6: 55 (8.271 %)

Number of data points in class 5: 48 (7.218 %)

Number of data points in class 3: 18 (2.707 %)

Number of data points in class 9: 7 (1.053 %)

Number of data points in class 8: 4 (0.602 %)
```



```
Number of data points in class 7 : 153 ( 28.759 %)

Number of data points in class 4 : 110 ( 20.677 %)

Number of data points in class 1 : 91 ( 17.105 %)

Number of data points in class 2 : 72 ( 13.534 %)

Number of data points in class 6 : 44 ( 8.271 %)

Number of data points in class 5 : 39 ( 7.331 %)

Number of data points in class 3 : 14 ( 2.632 %)

Number of data points in class 9 : 6 ( 1.128 %)

Number of data points in class 8 : 3 ( 0.564 %)
```

3.2 Prediction using a 'Random' Model

In a 'Random' Model, we generate the NINE class probabilites randomly such that they sum to 1.

In [13]:

```
# This function plots the confusion matrices given y i, y i hat.
def plot confusion matrix(test y, predict y):
   C = confusion_matrix(test_y, predict_y)
    \# C = 9,9 matrix, each cell (i,j) represents number of points of class i are predicted class j
    A = (((C.T)/(C.sum(axis=1))).T)
    #divid each element of the confusion matrix with the sum of elements in that column
    \# C = [[1, 2],
          [3, 4]]
    # C.T = [[1, 3],
             [2, 4]]
    \# C.sum(axis = 1)
                      axis=0 corresonds to columns and axis=1 corresponds to rows in two
diamensional arrav
   \# C.sum(axix = 1) = [[3, 7]]
    \# ((C.T)/(C.sum(axis=1))) = [[1/3, 3/7]
                                 [2/3, 4/7]]
    # ((C.T)/(C.sum(axis=1))).T = [[1/3, 2/3]
                                 [3/7, 4/7]]
    \# sum of row elements = 1
    B = (C/C.sum(axis=0))
    #divid each element of the confusion matrix with the sum of elements in that row
```

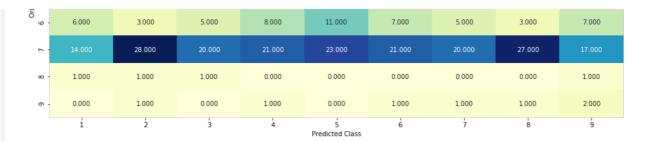
```
\# C = [[1, 2],
         [3, 4]]
   # C.sum(axis = 0) axis=0 corresonds to columns and axis=1 corresponds to rows in two
diamensional array
   \# C.sum(axix = 0) = [[4, 6]]
   \# (C/C.sum(axis=0)) = [[1/4, 2/6],
                           [3/4, 4/6]]
   labels = [1,2,3,4,5,6,7,8,9]
   # representing A in heatmap format
   print("-"*20, "Confusion matrix", "-"*20)
   plt.figure(figsize=(20,7))
   sns.heatmap(C, annot=True, cmap="YlGnBu", fmt=".3f", xticklabels=labels, yticklabels=labels)
   plt.xlabel('Predicted Class')
   plt.ylabel('Original Class')
   plt.show()
   print("-"*20, "Precision matrix (Column Sum=1)", "-"*20)
   plt.figure(figsize=(20,7))
   sns.heatmap(B, annot=True, cmap="YlGnBu", fmt=".3f", xticklabels=labels, yticklabels=labels)
   plt.xlabel('Predicted Class')
   plt.ylabel('Original Class')
   plt.show()
    # representing B in heatmap format
   print("-"*20, "Recall matrix (Row sum=1)", "-"*20)
   plt.figure(figsize=(20,7))
   sns.heatmap(A, annot=True, cmap="YlGnBu", fmt=".3f", xticklabels=labels, yticklabels=labels)
   plt.xlabel('Predicted Class')
   plt.ylabel('Original Class')
   plt.show()
```

In [14]:

```
\# we need to generate 9 numbers and the sum of numbers should be 1
# one solution is to genarate 9 numbers and divide each of the numbers by their sum
# ref: https://stackoverflow.com/a/18662466/4084039
test data len = test df.shape[0]
cv data len = cv df.shape[0]
# we create a output array that has exactly same size as the CV data
cv predicted y = np.zeros((cv_data_len,9))
for i in range(cv data len):
   rand_probs = np.random.rand(1,9)
    cv_predicted_y[i] = ((rand_probs/sum(sum(rand_probs)))[0])
print("Log loss on Cross Validation Data using Random Model", log loss(y cv,cv predicted y, eps=1e-
15))
# Test-Set error.
#we create a output array that has exactly same as the test data
test predicted y = np.zeros((test data len,9))
for i in range(test data len):
    rand probs = np.random.rand(1,9)
    test_predicted_y[i] = ((rand_probs/sum(sum(rand_probs)))[0])
print("Log loss on Test Data using Random Model",log_loss(y_test,test_predicted_y, eps=1e-15))
predicted_y =np.argmax(test_predicted_y, axis=1)
plot_confusion_matrix(y_test, predicted_y+1)
```

Log loss on Cross Validation Data using Random Model 2.479776112529109 Log loss on Test Data using Random Model 2.544516852113641

·	10.000	9.000	8.000	10.000	16.000	14.000	16.000	12.000	19.000
- 5	10.000	7.000	10.000	7.000	8.000	10.000		12.000	12.000
m -	3.000	1.000	3.000	2.000	1.000	3.000	3.000	2.000	0.000
SS 4	13.000	11.000	15.000	18.000	21.000	15.000	19.000	6.000	19.000
iginal Class 5	8.000	11.000	3.000	5.000	3.000	2.000	7.000	5.000	4.000



- 5

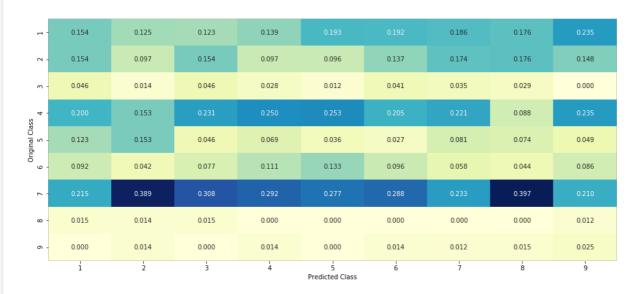
- 0.32

0.24

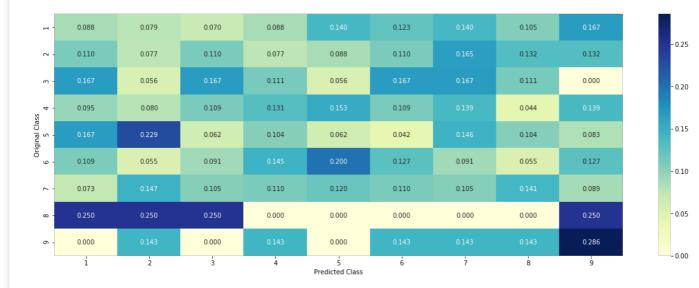
-0.16

- 0.08

----- Precision matrix (Columm Sum=1) -----



----- Recall matrix (Row sum=1) -----



3.3 Univariate Analysis

In [15]:

```
# code for response coding with Laplace smoothing.
# alpha : used for laplace smoothing
# feature: ['gene', 'variation']
# df: ['train_df', 'test_df', 'cv_df']
# algorithm
# ------
# Consider all unique values and the number of occurances of given feature in train data dataframe
# build a vector (1*9) , the first element = (number of times it occured in class1 + 10*alpha / nu
mber of time it occurred in total data+90*alpha)
# gv_dict is like a look up table, for every gene it store a (1*9) representation of it
# for a value of feature in df:
```

```
# we add the vector that was stored in 'gv dict' look up table to 'gv fea'
# if it is not there is train:
# we add [1/9, 1/9, 1/9, 1/9, 1/9, 1/9, 1/9, 1/9] to 'gv fea'
# return 'gv fea'
# get_gv_fea_dict: Get Gene varaition Feature Dict
def get gv fea dict(alpha, feature, df):
   # value count: it contains a dict like
   # print(train df['Gene'].value counts())
    # output:
            {BRCA1
                     174
             TP5.3
                       106
            EGFR
                        86
            BRCA2
                       7.5
            PTEN
                       69
                        6.1
            KIT
             BRAF
                        60
             ERBB2
                        47
                       46
             PDGFRA
             ...}
   # print(train df['Variation'].value counts())
   # output:
   # {
   # Truncating Mutations
                                            63
   # Deletion
                                            43
   # Amplification
                                             43
   # Fusions
   # Overexpression
   # E17K
                                             3
   # 0611
                                             .3
   # S222D
    # P130S
   # }
   value count = train df[feature].value counts()
   # gv dict : Gene Variation Dict, which contains the probability array for each gene/variation
   gv dict = dict()
    # denominator will contain the number of time that particular feature occured in whole data
   for i, denominator in value count.items():
       # vec will contain (p(yi==1/Gi) probability of gene/variation belongs to perticular class
       # vec is 9 diamensional vector
       vec = []
       for k in range (1,10):
           # print(train df.loc[(train df['Class']==1) & (train df['Gene']=='BRCA1')])
                   ID Gene
                                         Variation Class
           # 2470 2470 BRCA1
                                           S1715C
           # 2486 2486 BRCA1
                                            S1841R
           # 2614 2614 BRCA1
# 2432 2432 BRCA1
                                               M1R
                                            L1657P
           # 2567 2567 BRCA1
                                            T1685A
           # 2583 2583 BRCA1
                                           E1660G
           # 2634 2634 BRCA1
                                            W1718L
           # cls cnt.shape[0] will return the number of rows
           cls cnt = train df.loc[(train df['Class']==k) & (train df[feature]==i)]
           # cls cnt.shape[0](numerator) will contain the number of time that particular feature (
ccured in whole data
           vec.append((cls cnt.shape[0] + alpha*10)/ (denominator + 90*alpha))
       # we are adding the gene/variation to the dict as key and vec as value
       gv dict[i]=vec
   return gv_dict
# Get Gene variation feature
def get gv feature(alpha, feature, df):
   # print(gv dict)
      {'BRCA1': [0.2007575757575757575, 0.037878787878787878, 0.068181818181818177,
0.13636363636363635,\ 0.25,\ 0.193181818181818181,\ 0.03787878787878788,\ 0.03787878787878788,
0.03787878787878787881,
      'TP53': [0.32142857142857145, 0.061224489795918366, 0.061224489795918366,
163265307, 0.056122448979591837],
```

if it is in train data:

```
'EGFR': [0.056818181818181816, 0.215909090909091, 0.0625, 0.068181818181818177,
0.0681818181818177, 0.0625, 0.346590909090912, 0.0625, 0.056818181818181816],
0.06060606060606060608, 0.0606060606060608]
        'PTEN': [0.069182389937106917, 0.062893081761006289, 0.069182389937106917,
761006289, 0.062893081761006289],
        'KIT': [0.066225165562913912, 0.25165562913907286, 0.072847682119205295,
0.072847682119205295, 0.066225165562913912, 0.066225165562913912, 0.27152317880794702,
0.066225165562913912, 0.066225165562913912],
        'BRAF': [0.066666666666666666, 0.17999999999999, 0.07333333333333334,
#
  gv dict = get gv fea dict(alpha, feature, df)
   # value count is similar in get gv fea dict
   value count = train df[feature].value counts()
   # gv fea: Gene variation feature, it will contain the feature for each feature value in the da
ta
   gv fea = []
   # for every feature values in the given data frame we will check if it is there in the train
data then we will add the feature to gv fea
   # if not we will add [1/9,1/9,1/9,1/9,1/9,1/9,1/9,1/9,1/9] to gv fea
   for index, row in df.iterrows():
      if row[feature] in dict(value count).keys():
         gv fea.append(gv dict[row[feature]])
      else:
         gv fea.append([1/9,1/9,1/9,1/9,1/9,1/9,1/9,1/9])
           gv fea.append([-1,-1,-1,-1,-1,-1,-1,-1])
   return qv fea
```

when we caculate the probability of a feature belongs to any particular class, we apply laplace smoothing

• (numerator + 10*alpha) / (denominator + 90*alpha)

3.2.1 Univariate Analysis on Gene Feature

Q1. Gene, What type of feature it is?

Ans. Gene is a categorical variable

Q2. How many categories are there and How they are distributed?

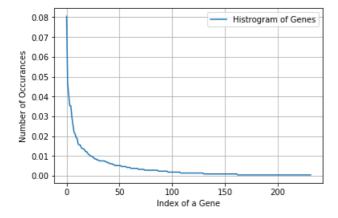
```
In [16]:
```

```
unique genes = train df['Gene'].value counts()
print('Number of Unique Genes :', unique genes.shape[0])
# the top 10 genes that occured most
print(unique_genes.head(10))
Number of Unique Genes: 232
BRCA1
         171
TP53
          99
           87
EGFR
           75
BRCA2
PTEN
           75
           63
KIT
BRAF
           5.5
ERBB2
           47
ALK
           45
           41
PDGFRA
Name: Gene, dtype: int64
In [17]:
print("Ans: There are", unique genes.shape[0], "different categories of genes in the train data, an
d they are distibuted as follows",)
```

lows

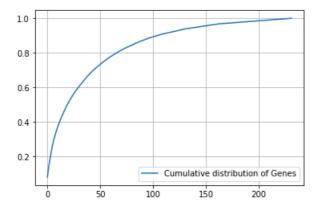
In [18]:

```
s = sum(unique_genes.values);
h = unique_genes.values/s;
plt.plot(h, label="Histrogram of Genes")
plt.xlabel('Index of a Gene')
plt.ylabel('Number of Occurances')
plt.legend()
plt.grid()
plt.show()
```



In [19]:

```
c = np.cumsum(h)
plt.plot(c,label='Cumulative distribution of Genes')
plt.grid()
plt.legend()
plt.show()
```



Q3. How to featurize this Gene feature?

Ans.there are two ways we can featurize this variable check out this video: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/handling-categorical-and-numerical-features/

- 1. One hot Encoding
- 2. Response coding

We will choose the appropriate featurization based on the ML model we use. For this problem of multi-class classification with categorical features, one-hot encoding is better for Logistic regression while response coding is better for Random Forests.

In [20]:

```
#response-coding of the Gene feature
# alpha is used for laplace smoothing
alpha = 1
# train gene feature
```

```
# LIAIN YENE LEALUIE
train_gene_feature_responseCoding = np.array(get_gv_feature(alpha, "Gene", train_df))
# test gene feature
test gene feature responseCoding = np.array(get gv feature(alpha, "Gene", test df))
# cross validation gene feature
cv_gene_feature_responseCoding = np.array(get_gv_feature(alpha, "Gene", cv_df))
In [21]:
print("train gene feature responseCoding is converted feature using respone coding method. The sha
pe of gene feature:", train gene feature responseCoding.shape)
train_gene_feature_responseCoding is converted feature using respone coding method. The shape of g
ene feature: (2124, 9)
In [22]:
# one-hot encoding of Gene feature.
gene vectorizer = CountVectorizer()
train gene feature onehotCoding = gene vectorizer.fit transform(train df['Gene'])
test_gene_feature_onehotCoding = gene_vectorizer.transform(test_df['Gene'])
cv gene feature onehotCoding = gene vectorizer.transform(cv df['Gene'])
In [23]:
train df['Gene'].head()
Out[23]:
       TP53
490
       NRAS
3192
2352
     AURKA
552
       SMAD2
2425
       BRCA1
Name: Gene, dtype: object
In [24]:
gene vectorizer.get feature names()
Out[24]:
['abl1',
 'acvr1',
 'ago2',
 'akt1',
 'akt2',
 'akt3',
 'alk',
 'apc',
 'ar',
 'araf',
 'arid1b',
 'arid2',
 'arid5b',
 'asxl2',
 'atm',
 'atr',
 'atrx',
 'aurka',
 'aurkb',
 'axl',
 'b2m',
 'bap1',
 'bard1',
 'bcl2111',
 'bcor',
 'braf',
 'brca1',
 'brca2',
 'brd4',
 'brip1',
```

```
'btk',
'card11',
'carm1',
'casp8',
'cbl',
'ccnd1',
'ccnd2',
'ccnd3',
'ccne1',
'cdh1',
'cdk12',
'cdk4',
'cdk6',
'cdk8',
'cdkn1a',
'cdkn2a',
'cdkn2b',
'cdkn2c',
'chek2',
'cic',
'crebbp',
'ctcf',
'ctla4',
'ctnnb1',
'ddr2',
'dicer1',
'dnmt3a',
'dnmt3b',
'egfr',
'eiflax',
'elf3',
'ep300',
'epas1',
'epcam',
'erbb2',
'erbb3',
'erbb4',
'ercc2',
'ercc3',
'ercc4',
'erg',
'errfil',
'esr1',
'etv1',
'etv6',
'ewsr1',
'ezh2',
'fanca',
'fat1',
'fbxw7',
'fgf19',
'fgf3',
'fgf4',
'fgfr1',
'fgfr2',
'fgfr3',
'fgfr4',
'flt3',
'foxa1',
'fox12',
'foxp1',
'fubp1',
'gata3',
'gli1',
'gna11',
'gnaq',
'gnas',
'h3f3a',
'hist1h1c',
'hla',
'hnfla',
'hras',
'idh1',
'idh2',
'igf1r',
'ikbke',
'ikzf1',
```

```
'il7r',
'jak1',
'jak2',
'jun',
'kdm5a',
'kdm5c',
'kdr',
'keap1',
'kit',
'kmt2a',
'kmt2b',
'kmt2c',
'kmt2d',
'knstrn',
'kras',
'lats1',
'map2k1',
'map2k2',
'map2k4',
'map3k1',
'mapk1',
'mdm2',
'med12',
'mef2b',
'men1',
'met',
'mga',
'mlh1',
'mpl',
'msh2',
'msh6',
'mtor',
'myc',
'myd88',
'nf1',
'nf2',
'nfe212',
'nfkbia',
'nkx2',
'notch1',
'notch2',
'npm1',
'nras',
'ntrk1',
'ntrk2',
'ntrk3',
'nup93',
'pak1',
'pbrm1',
'pdgfra',
'pdgfrb',
'pik3ca',
'pik3cb',
'pik3cd',
'pik3r1',
'pik3r2',
'pim1',
'pms1',
'pole',
'ppm1d',
'ppp2r1a',
'ppp6c',
'prdm1',
'ptch1',
'pten',
'ptpn11',
'ptprd',
'ptprt',
'rac1',
'rad21',
'rad50',
'rad51b',
'rad51c',
'rad51d',
'raf1',
'rara',
```

```
'rasa1',
'rb1',
 'rbm10'
 'ret',
 'rheb'
 'rhoa',
'rit1',
'ros1',
 'rras2'
 'runx1',
 'rxra',
'sdhc',
'setd2',
'sf3b1',
 'shoc2',
 'shq1',
 'smad2'.
'smad3',
'smad4',
 'smarca4'
 'smarcb1'
 'smo',
'sos1',
'sox9',
'spop',
 'src',
 'srsf2',
 'stat3',
'stk11',
'tcf3',
 'tcf712',
 'tert',
 'tet1',
'tet2',
'tgfbr1',
'tgfbr2',
 'tmprss2',
 'tp53',
 'tp53bp1',
'tsc1',
'tsc2',
 'u2af1',
 'vegfa',
 'vhl',
'whsc1l1',
'xpo1',
'yap1']
In [25]:
of gene feature:", train_gene_feature_onehotCoding.shape)
```

```
print("train_gene_feature_onehotCoding is converted feature using tfidf encoding method. The shape
```

train gene feature onehotCoding is converted feature using tfidf encoding method. The shape of gene feature: (2124, 231)

Q4. How good is this gene feature in predicting y_i?

There are many ways to estimate how good a feature is, in predicting y_i. One of the good methods is to build a proper ML model using just this feature. In this case, we will build a logistic regression model using only Gene feature (one hot encoded) to predict y_i.

```
In [26]:
```

```
alpha = [10 ** x for x in range(-5, 1)] # hyperparam for SGD classifier.
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear\_model.SGDClassifier.html \\
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11_ratio=0.15, fit_intercept=True, max_i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n_jobs=1, random_state=None, learning_rate='optimal', eta0
=0.0, power t=0.5,
```

```
# class weight=None, warm start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef init, intercept init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link:
cv_log_error_array=[]
for i in alpha:
   clf = SGDClassifier(alpha=i, penalty='12', loss='log', random_state=42)
    clf.fit(train gene feature onehotCoding, y train)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_gene_feature_onehotCoding, y_train)
    predict_y = sig_clf.predict_proba(cv_gene_feature_onehotCoding)
    cv_log_error_array.append(log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
    print('For values of alpha = ', i, "The log loss is:",log_loss(y_cv, predict_y, labels=clf.clas
ses , eps=1e-15))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
   ax.annotate((alpha[i],np.round(txt,3)), (alpha[i],cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = SGDClassifier(alpha=alpha[best alpha], penalty='12', loss='log', random state=42)
clf.fit(train gene feature onehotCoding, y train)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train gene feature onehotCoding, y train)
predict_y = sig_clf.predict_proba(train_gene_feature_onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The train log loss is:",log loss(y train,
predict_y, labels=clf.classes_, eps=1e-15))
predict y = sig clf.predict proba(cv gene feature onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The cross validation log loss is:",log lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict y = sig clf.predict proba(test gene feature onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=1e-15))
For values of alpha = 1e-05 The log loss is: 1.3381574466347526
For values of alpha = 0.0001 The log loss is: 1.1781569576276634
For values of alpha =
                      0.001 The log loss is: 1.2120001369797957
```

```
For values of alpha = 1e-05 The log loss is: 1.3381574466347526

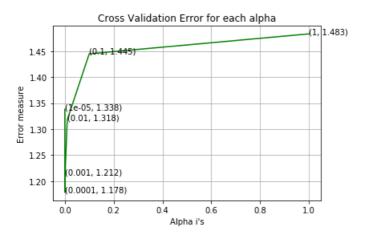
For values of alpha = 0.0001 The log loss is: 1.178156957627663-

For values of alpha = 0.001 The log loss is: 1.2120001369797957

For values of alpha = 0.01 The log loss is: 1.317761793325431

For values of alpha = 0.1 The log loss is: 1.4447224796205975

For values of alpha = 1 The log loss is: 1.4831127234027244
```



For values of best alpha = 0.0001 The train log loss is: 1.0401226134001003For values of best alpha = 0.0001 The cross validation log loss is: 1.1781569576276634

```
For values of best alpha = 0.0001 The test log loss is: 1.2137502770025546
```

Q5. Is the Gene feature stable across all the data sets (Test, Train, Cross validation)?

Ans. Yes, it is. Otherwise, the CV and Test errors would be significantly more than train error.

```
In [27]:
```

```
print ("Q6. How many data points in Test and CV datasets are covered by the ", unique genes.shape[0
], " genes in train dataset?")
test_coverage=test_df[test_df['Gene'].isin(list(set(train_df['Gene'])))].shape[0]
cv_coverage=cv_df[cv_df['Gene'].isin(list(set(train_df['Gene'])))].shape[0]
print('Ans\n1. In test data', test coverage, 'out of', test df.shape[0], ":", (test coverage/test df.
shape[0])*100)
print('2. In cross validation data',cv coverage, 'out of ',cv df.shape[0],":" ,(cv coverage/cv df.s
hape[0])*100)
Q6. How many data points in Test and CV datasets are covered by the 232 genes in train dataset?
1. In test data 636 out of 665 : 95.6390977443609
2. In cross validation data 520 out of 532: 97.74436090225564
```

3.2.2 Univariate Analysis on Variation Feature

Q7. Variation, What type of feature is it?

Ans. Variation is a categorical variable

Q8. How many categories are there?

```
In [28]:
```

```
unique variations = train df['Variation'].value counts()
print('Number of Unique Variations :', unique_variations.shape[0])
# the top 10 variations that occured most
print(unique variations.head(10))
Number of Unique Variations: 1929
Amplification
                        52
Truncating Mutations
                        50
Deletion
                        46
                        22
Fusions
Overexpression
                         3
E17K
061R
                         3
T58T
A146V
Name: Variation, dtype: int64
```

In [29]:

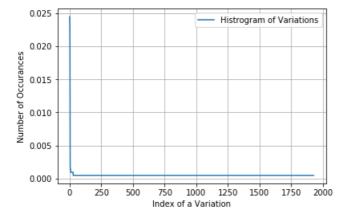
```
print ("Ans: There are", unique variations.shape[0], "different categories of variations in the
train data, and they are distibuted as follows",)
```

Ans: There are 1929 different categories of variations in the train data, and they are distibuted as follows

In [30]:

```
s = sum(unique variations.values);
h = unique variations.values/s;
plt.plot(h, label="Histrogram of Variations")
plt.xlabel('Index of a Variation')
plt.ylabel('Number of Occurances')
```

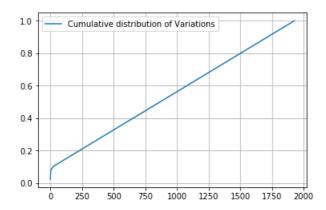
```
plt.legena()
plt.grid()
plt.show()
```



In [31]:

```
c = np.cumsum(h)
print(c)
plt.plot(c,label='Cumulative distribution of Variations')
plt.grid()
plt.legend()
plt.show()
```

```
[0.02448211 0.0480226 0.06967985 ... 0.99905838 0.99952919 1.
```



Q9. How to featurize this Variation feature?

Ans. There are two ways we can featurize this variable check out this video: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/handling-categorical-and-numerical-features/

- 1. One hot Encoding
- 2. Response coding

We will be using both these methods to featurize the Variation Feature

In [32]:

```
# alpha is used for laplace smoothing
alpha = 1
# train gene feature
train_variation_feature_responseCoding = np.array(get_gv_feature(alpha, "Variation", train_df))
# test gene feature
test_variation_feature_responseCoding = np.array(get_gv_feature(alpha, "Variation", test_df))
# cross validation gene feature
cv_variation_feature_responseCoding = np.array(get_gv_feature(alpha, "Variation", cv_df))
```

```
print("train_variation_feature_responseCoding is a converted feature using the response coding met
hod. The shape of Variation feature:", train_variation_feature_responseCoding.shape)
```

train_variation_feature_responseCoding is a converted feature using the response coding method. The shape of Variation feature: (2124, 9)

In [34]:

```
# one-hot encoding of variation feature.
variation_vectorizer = CountVectorizer()
train_variation_feature_onehotCoding = variation_vectorizer.fit_transform(train_df['Variation'])
test_variation_feature_onehotCoding = variation_vectorizer.transform(test_df['Variation'])
cv_variation_feature_onehotCoding = variation_vectorizer.transform(cv_df['Variation'])
```

In [35]:

```
print("train_variation_feature_onehotEncoded is converted feature using the Tfidf encoding method.
The shape of Variation feature:", train_variation_feature_onehotCoding.shape)
```

train_variation_feature_onehotEncoded is converted feature using the Tfidf encoding method. The sh ape of Variation feature: (2124, 1956)

Q10. How good is this Variation feature in predicting y_i?

Let's build a model just like the earlier!

In [36]:

```
alpha = [10 ** x for x in range(-5, 1)]
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n jobs=1, random state=None, learning rate='optimal', eta0
=0.0, power t=0.5,
# class weight=None, warm start=False, average=False, n iter=None)
# some of methods
# fit(X, y[, coef init, intercept init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link:
cv log error array=[]
for i in alpha:
    clf = SGDClassifier(alpha=i, penalty='12', loss='log', random state=42)
    clf.fit(train variation feature onehotCoding, y train)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train variation feature onehotCoding, y train)
    predict_y = sig_clf.predict_proba(cv_variation_feature_onehotCoding)
    cv_log_error_array.append(log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
   print (For values of alpha = ", i, "The log loss is:",log_loss(y_cv, predict_y, labels=clf.clas
ses_, eps=1e-15))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
   ax.annotate((alpha[i],np.round(txt,3)), (alpha[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
```

```
best_alpha = np.argmin(cv_log_error_array)
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='log', random_state=42)
clf.fit(train_variation_feature_onehotCoding, y_train)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_variation_feature_onehotCoding, y_train)

predict_y = sig_clf.predict_proba(train_variation_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train, predict_y = sig_clf.predict_proba(cv_variation_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_loss(y_cv, predict_y, labels=clf.classes_, eps=le-15))
predict_y = sig_clf.predict_proba(test_variation_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p_redict_y, labels=clf.classes_, eps=le-15))
```

```
For values of alpha = 1e-05 The log loss is: 1.7189279183722028

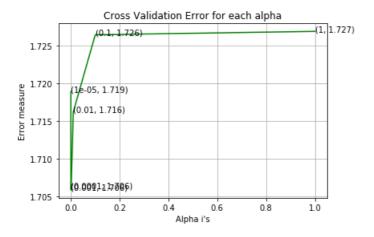
For values of alpha = 0.0001 The log loss is: 1.706090857543447

For values of alpha = 0.001 The log loss is: 1.705897792199417

For values of alpha = 0.01 The log loss is: 1.7162574521316176

For values of alpha = 0.1 The log loss is: 1.72648752011323

For values of alpha = 1 The log loss is: 1.7269419769038998
```



```
For values of best alpha = 0.001 The train log loss is: 1.083994583936251
For values of best alpha = 0.001 The cross validation log loss is: 1.705897792199417
For values of best alpha = 0.001 The test log loss is: 1.6940714910265862
```

Q11. Is the Variation feature stable across all the data sets (Test, Train, Cross validation)?

Ans. Not sure! But lets be very sure using the below analysis.

```
In [37]:
```

```
print("Q12. How many data points are covered by total ", unique_variations.shape[0], " genes in te
st and cross validation data sets?")
test_coverage=test_df[test_df['Variation'].isin(list(set(train_df['Variation'])))].shape[0]
cv_coverage=cv_df[cv_df['Variation'].isin(list(set(train_df['Variation'])))].shape[0]
print('Ans\n1. In test data',test_coverage, 'out of',test_df.shape[0], ":",(test_coverage/test_df.shape[0])*100)
print('2. In cross validation data',cv_coverage, 'out of ',cv_df.shape[0],":",(cv_coverage/cv_df.shape[0])*100)
```

Q12. How many data points are covered by total 1929 genes in test and cross validation data sets? Ans

- 1. In test data 75 out of 665 : 11.278195488721805
- 2. In cross validation data 52 out of 532 : 9.774436090225564

3.2.3 Univariate Analysis on Text Feature

1. How many unique words are present in train data?

.. How many anique nerve are precent in train data.

- 2. How are word frequencies distributed?
- 3. How to featurize text field?
- 4. Is the text feature useful in predicitng y i?
- 5. Is the text feature stable across train, test and CV datasets?

In [62]:

In [63]:

Feature Engineering

Taken top 3000 Features.
Calculated 1 to 4 gram words.

```
In [147]:
```

```
#from sklearn.feature_extraction.text import TfidfVectorizer
# building a CountVectorizer with all the words that occured minimum 3 times in train data
text_vectorizer = TfidfVectorizer(min_df=3,max_features=3000,ngram_range=(1,3))
train_text_feature_onehotCoding = text_vectorizer.fit_transform(train_df['TEXT'])
# getting all the feature names (words)
train_text_features= text_vectorizer.get_feature_names()

# train_text_feature_onehotCoding.sum(axis=0).Al will sum every row and returns (1*number of features) vector
train_text_fea_counts = train_text_feature_onehotCoding.sum(axis=0).Al

# zip(list(text_features),text_fea_counts) will zip a word with its number of times it occured
text_fea_dict = dict(zip(list(train_text_features),train_text_fea_counts))

print("Total number of unique words in train data :", len(train_text_features))
```

Total number of unique words in train data: 3000

```
In [148]:
```

```
print(train_text_feature_onehotCoding.shape)
```

(2124, 3000)

```
In [ ]:
In [149]:
dict list = []
# dict_list =[] contains 9 dictoinaries each corresponds to a class
for i in range (1,10):
    cls text = train df[train df['Class']==i]
    # build a word dict based on the words in that class
    dict list.append(extract dictionary paddle(cls text))
    # append it to dict_list
# dict list[i] is build on i'th class text data
# total dict is buid on whole training text data
total_dict = extract_dictionary_paddle(train_df)
confuse array = []
for i in train_text_features:
   ratios = []
    \max val = -1
    for j in range (0,9):
       ratios.append((dict_list[j][i]+10 )/(total_dict[i]+90))
    confuse array.append(ratios)
confuse_array = np.array(confuse_array)
In [150]:
#response coding of text features
train_text_feature_responseCoding = get_text_responsecoding(train_df)
test_text_feature_responseCoding = get_text_responsecoding(test_df)
cv_text_feature_responseCoding = get_text_responsecoding(cv_df)
In [151]:
# https://stackoverflow.com/a/16202486
# we convert each row values such that they sum to 1
train text feature responseCoding =
(train text feature responseCoding.T/train text feature responseCoding.sum(axis=1)).T
test_text_feature_responseCoding =
(test text feature responseCoding.T/test text feature responseCoding.sum(axis=1)).T
cv text feature responseCoding = (cv text feature responseCoding.T/cv text feature responseCoding.
sum(axis=1)).T
In [152]:
# don't forget to normalize every feature
train_text_feature_onehotCoding = normalize(train_text_feature_onehotCoding, axis=0)
# we use the same vectorizer that was trained on train data
test text feature onehotCoding = text vectorizer.transform(test df['TEXT'])
# don't forget to normalize every feature
test_text_feature_onehotCoding = normalize(test_text_feature_onehotCoding, axis=0)
# we use the same vectorizer that was trained on train data
cv text feature onehotCoding = text vectorizer.transform(cv df['TEXT'])
# don't forget to normalize every feature
cv_text_feature_onehotCoding = normalize(cv_text_feature_onehotCoding, axis=0)
In [153]:
#https://stackoverflow.com/a/2258273/4084039
sorted_text_fea_dict = dict(sorted(text_fea_dict.items(), key=lambda x: x[1] , reverse=True))
sorted_text_occur = np.array(list(sorted_text_fea_dict.values()))
```

Number of words for a given frequency.
print(Counter(sorted_text_occur))

In [154]:

```
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                                                                                                ▶
In [155]:
# Train a Logistic regression+Calibration model using text features whicha re on-hot encoded
alpha = [10 ** x for x in range(-5, 1)]
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n_jobs=1, random_state=None, learning_rate='optimal', eta0
=0.0, power t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef_init, intercept_init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link:
cv_log_error_array=[]
for i in alpha:
    clf = SGDClassifier(alpha=i, penalty='12', loss='log', random_state=42)
    clf.fit(train_text_feature_onehotCoding, y_train)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_text_feature_onehotCoding, y_train)
    predict_y = sig_clf.predict_proba(cv_text_feature_onehotCoding)
```

cv_log_error_array.append(log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))

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```
print('For values of alpha = ', i, "The log loss is:",log_loss(y_cv, predict_y, labels=clf.clas
ses_, eps=1e-15))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
    ax.annotate((alpha[i],np.round(txt,3)), (alpha[i],cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='log', random_state=42)
clf.fit(train_text_feature_onehotCoding, y_train)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train text feature onehotCoding, y train)
predict_y = sig_clf.predict_proba(train_text_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(cv_text_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_text_feature_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=1e-15))
```

```
For values of alpha = 1e-05 The log loss is: 1.1266411864732777

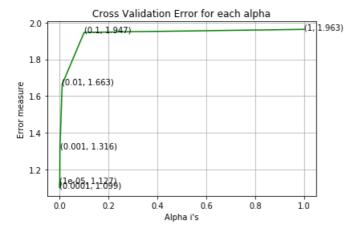
For values of alpha = 0.0001 The log loss is: 1.0990823938262766

For values of alpha = 0.001 The log loss is: 1.3156469219838092

For values of alpha = 0.01 The log loss is: 1.6634603291292935

For values of alpha = 0.1 The log loss is: 1.9468386614193944

For values of alpha = 1 The log loss is: 1.9633280879120718
```



```
For values of best alpha = 0.0001 The train log loss is: 0.6984468146483667

For values of best alpha = 0.0001 The cross validation log loss is: 1.0990823938262766

For values of best alpha = 0.0001 The test log loss is: 1.1071223707490347
```

Q. Is the Text feature stable across all the data sets (Test, Train, Cross validation)?

Ans. Yes, it seems like!

```
In [156]:
```

```
def get_intersec_text(df):
    df_text_vec = TfidfVectorizer(min_df=3)
    df_text_fea = df_text_vec.fit_transform(df['TEXT'])
    df_text_features = df_text_vec.get_feature_names()

df_text_fea_counts = df_text_fea.sum(axis=0).A1
    df_text_fea_dict = dict(zip(list(df_text_features),df_text_fea_counts))
    len1 = len(set(df_text_features))
    len2 = len(set(train_text_features) & set(df_text_features))
```

```
return len1,len2
len1,len2 = get intersec text(test df)
print(np.round((len2/len1)*100, 3), "% of word of test data appeared in train data")
len1,len2 = get_intersec_text(cv_df)
print(np.round((len2/len1)*100, 3), "% of word of Cross Validation appeared in train data")
8.411 % of word of test data appeared in train data
9.278 % of word of Cross Validation appeared in train data
4. Machine Learning Models
In [158]:
#Data preparation for ML models.
#Misc. functionns for ML models
def predict_and_plot_confusion_matrix(train_x, train_y,test_x, test_y, clf):
    clf.fit(train_x, train_y)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_x, train_y)
    pred y = sig_clf.predict(test_x)
    # for calculating log_loss we will1 provide the array of probabilities belongs to each class
    print("Log loss :",log_loss(test_y, sig_clf.predict_proba(test_x)))
    # calculating the number of data points that are misclassified
    print("Number of mis-classified points :", np.count_nonzero((pred_y- test_y))/test_y.shape[0])
    plot_confusion_matrix(test_y, pred_y)
In [159]:
def report log loss(train x, train y, test x, test y, clf):
    clf.fit(train x, train y)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train x, train y)
    sig_clf_probs = sig_clf.predict_proba(test_x)
    return log_loss(test_y, sig_clf_probs, eps=1e-15)
In [160]:
# this function will be used just for naive bayes
# for the given indices, we will print the name of the features
# and we will check whether the feature present in the test point text or not
def get impfeature names (indices, text, gene, var, no features):
    gene count vec = CountVectorizer()
```

```
var_count_vec = CountVectorizer()
text count vec = CountVectorizer(min df=3)
gene_vec = gene_count_vec.fit(train_df['Gene'])
var vec = var count vec.fit(train df['Variation'])
text_vec = text_count_vec.fit(train_df['TEXT'])
fea1_len = len(gene_vec.get_feature_names())
fea2_len = len(var_count_vec.get_feature_names())
word_present = 0
for i,v in enumerate(indices):
   if (v < feal len):
        word = gene_vec.get_feature_names()[v]
        yes no = True if word == gene else False
        if yes no:
            word present += 1
            print(i, "Gene feature [{}] present in test data point [{}]".format(word,yes_no))
    elif (v < fea1_len+fea2_len):</pre>
        word = var_vec.get_feature_names()[v-(fea1_len)]
        yes no = True if word == var else False
        if was no.
```

Stacking the three types of features

```
In [161]:
```

```
# merging gene, variance and text features
# building train, test and cross validation data sets
# a = [[1, 2],
      [3, 4]]
#b = [[4, 5],
      [6, 7]]
\# hstack(a, b) = [[1, 2, 4, 5],
                 [ 3, 4, 6, 7]]
train_gene_var_onehotCoding =
hstack((train_gene_feature_onehotCoding,train_variation_feature_onehotCoding))
test_gene_var_onehotCoding =
hstack((test_gene_feature_onehotCoding,test_variation_feature_onehotCoding))
cv_gene_var_onehotCoding = hstack((cv_gene_feature_onehotCoding,cv_variation_feature_onehotCoding)
train_x_onehotCoding = hstack((train_gene_var_onehotCoding, train_text_feature_onehotCoding)).tocs
train_y = np.array(list(train_df['Class']))
test x onehotCoding = hstack((test gene var onehotCoding, test text feature onehotCoding)).tocsr()
test_y = np.array(list(test_df['Class']))
cv_x_onehotCoding = hstack((cv_gene_var_onehotCoding, cv_text_feature_onehotCoding)).tocsr()
cv_y = np.array(list(cv_df['Class']))
train gene var responseCoding =
np.hstack((train_gene_feature_responseCoding,train_variation_feature_responseCoding))
test_gene_var_responseCoding =
np.hstack((test gene feature responseCoding,test variation feature responseCoding))
cv_gene_var_responseCoding =
np.hstack((cv gene feature responseCoding,cv variation feature responseCoding))
train_x_responseCoding = np.hstack((train_gene_var_responseCoding,
train text feature responseCoding))
test_x_responseCoding = np.hstack((test_gene_var_responseCoding, test_text_feature_responseCoding)
cv_x_responseCoding = np.hstack((cv_gene_var_responseCoding, cv_text_feature_responseCoding))
```

In [162]:

```
print("TFIDF encoding features :")
print("(number of data points * number of features) in train data = ", train_x_onehotCoding.shape)
print("(number of data points * number of features) in test data = ", test_x_onehotCoding.shape)
print("(number of data points * number of features) in cross validation data = ", cv_x_onehotCoding.shape)
.shape)
```

```
TFIDF encoding features:

(number of data points * number of features) in train data = (2124, 5187)

(number of data points * number of features) in test data = (665, 5187)

(number of data points * number of features) in cross validation data = (532, 5187)
```

```
In [163]:

print(" Response encoding features :")
print("(number of data points * number of features) in train data = ", train_x_responseCoding.shape)
print("(number of data points * number of features) in test data = ", test_x_responseCoding.shape)
print("(number of data points * number of features) in cross validation data = ",
cv_x_responseCoding.shape)

Response encoding features :
(number of data points * number of features) in train data = (2124, 27)
(number of data points * number of features) in test data = (665, 27)
(number of data points * number of features) in cross validation data = (532, 27)
```

4.1. Base Line Model

4.1.1. Naive Bayes

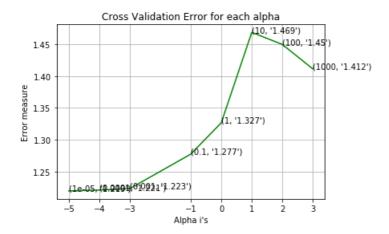
4.1.1.1. Hyper parameter tuning

In [165]:

```
# find more about Multinomial Naive base function here http://scikit-
learn.org/stable/modules/generated/sklearn.naive bayes.MultinomialNB.html
# default paramters
# sklearn.naive bayes.MultinomialNB(alpha=1.0, fit prior=True, class prior=None)
# some of methods of MultinomialNB()
# fit(X, y[, sample weight]) Fit Naive Bayes classifier according to X, y
# predict(X) Perform classification on an array of test vectors X.
# predict_log_proba(X) Return log-probability estimates for the test vector X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/naive-bayes-
algorithm-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/qenerated/sklearn.calibration.CalibratedClassifierCV.html
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get_params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict_proba(X) Posterior probabilities of classification
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/naive-bayes-
algorithm-1/
alpha = [0.00001, 0.0001, 0.001, 0.1, 1, 10, 100,1000]
cv_log_error_array = []
for i in alpha:
   print("for alpha =", i)
   clf = MultinomialNB(alpha=i)
   clf.fit(train x onehotCoding, train y)
   sig clf = CalibratedClassifierCV(clf, method="sigmoid")
   sig_clf.fit(train_x_onehotCoding, train_y)
   sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
   cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    # to avoid rounding error while multiplying probabilites we use log-probability estimates
   print("Log Loss :",log_loss(cv_y, sig_clf_probs))
fig, ax = plt.subplots()
ax.plot(np.log10(alpha), cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
```

```
ax.annotate((alpha[i],str(txt)), (np.log10(alpha[i]),cv_log_error_array[i]))
plt.grid()
plt.xticks(np.log10(alpha))
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = MultinomialNB(alpha=alpha[best alpha])
clf.fit(train_x_onehotCoding, train_y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)
predict_y = sig_clf.predict_proba(train_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict_y, labels=clf.classes_, eps=1e-15))
predict y = sig clf.predict proba(cv x onehotCoding)
print('For values of best alpha = ', alpha[best alpha], "The cross validation log loss is:",log lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=1e-15))
```

for alpha = 1e-05Log Loss: 1.2194059934143313 for alpha = 0.0001Log Loss: 1.2207934887276566 for alpha = 0.001Log Loss: 1.2230649820922408 for alpha = 0.1Log Loss: 1.2773086642148628 for alpha = 1Log Loss: 1.3266445279314851 for alpha = 10 Log Loss: 1.4689143909250757 for alpha = 100Log Loss: 1.4499743161707415 for alpha = 1000Log Loss: 1.411508129897685



```
For values of best alpha = 1e-05 The train log loss is: 0.589518145764967

For values of best alpha = 1e-05 The cross validation log loss is: 1.2194059934143313

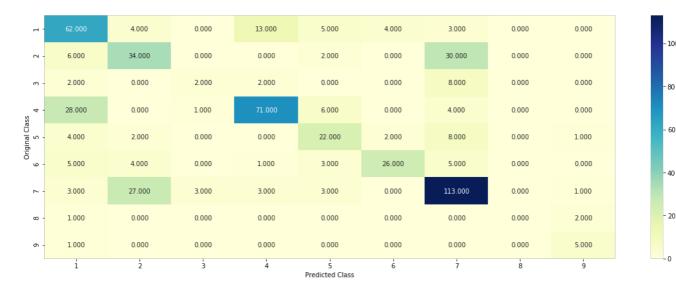
For values of best alpha = 1e-05 The test log loss is: 1.2348532379192088
```

4.1.1.2. Testing the model with best hyper paramters

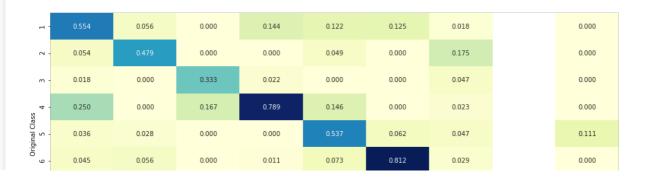
In [166]:

```
# find more about Multinomial Naive base function here http://scikit-
learn.org/stable/modules/generated/sklearn.naive_bayes.MultinomialNB.html
# ------
# default paramters
# sklearn.naive bayes.MultinomialNB(alpha=1.0. fit prior=True. class prior=None)
```

```
" ourcorn.norto_boyco.norornomeano.tarrio 1.0, rro_prior rroo, ordoo_prior nono,
# some of methods of MultinomialNB()
# fit(X, y[, sample_weight]) Fit Naive Bayes classifier according to X, y
# predict(X) Perform classification on an array of test vectors X.
# predict_log proba(X) Return log-probability estimates for the test vector X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/naive-bayes-
algorithm-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base_estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample_weight]) Fit the calibrated model
# get_params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
clf = MultinomialNB(alpha=alpha[best alpha])
clf.fit(train x onehotCoding, train_y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)
sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
# to avoid rounding error while multiplying probabilites we use log-probability estimates
print("Log Loss :",log_loss(cv_y, sig_clf_probs))
print("Number of missclassified point : ", np.count_nonzero((sig_clf.predict(cv_x_onehotCoding) - cv
_y))/cv_y.shape[0])
plot_confusion_matrix(cv_y, sig_clf.predict(cv_x_onehotCoding.toarray()))
```



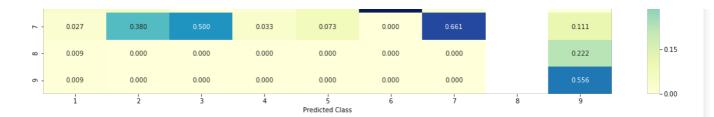
----- Precision matrix (Columm Sum=1) -----



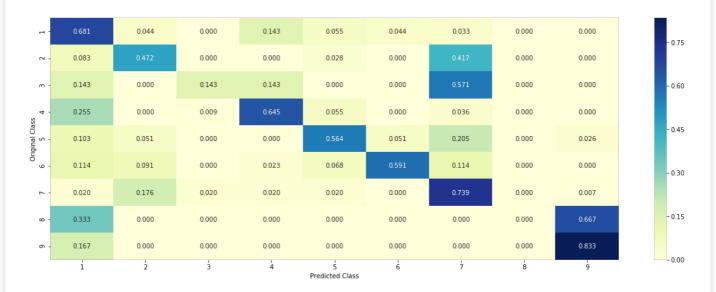
0.75

- 0.60

- 0.45



----- Recall matrix (Row sum=1) ------



4.1.1.3. Feature Importance, Correctly classified point

```
In [167]:
```

```
test_point_index = 1
no feature = 100
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef_) [predicted_cls-1][:,:no_feature]
print("-"*50)
get_impfeature_names(indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test_point_index], no_feature)
Predicted Class: 7
Predicted Class Probabilities: [[0.0656 0.0571 0.0168 0.0758 0.0409 0.0386 0.6981 0.0042 0.0029]]
Actual Class: 7
62 Text feature [2g] present in test data point [True]
Out of the top 100 features 1 are present in query point
```

4.1.1.4. Feature Importance, Incorrectly classified point

In [168]:

```
test_point_index = 100
no_feature = 100
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef_)[predicted_cls-1][:,:no_feature]
print("-"*50)
get_impfeature_names(indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
```

4.2. K Nearest Neighbour Classification

4.2.1. Hyper parameter tuning

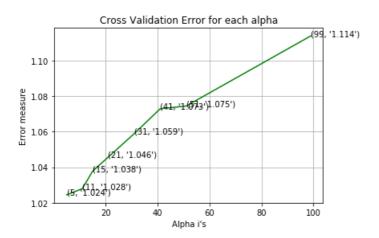
```
In [169]:
```

```
# find more about KNeighborsClassifier() here http://scikit-
learn.org/stable/modules/generated/sklearn.neighbors. KN eighborsClassifier.html \\
# default parameter
# KNeighborsClassifier(n neighbors=5, weights='uniform', algorithm='auto', leaf size=30, p=2,
# metric='minkowski', metric_params=None, n_jobs=1, **kwargs)
# methods of
# fit(X, y) : Fit the model using X as training data and y as target values
# predict(X):Predict the class labels for the provided data
# predict proba(X): Return probability estimates for the test data X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/k-nearest-ne
ighbors-geometric-intuition-with-a-toy-example-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link:
alpha = [5, 11, 15, 21, 31, 41, 51, 99]
cv_log_error_array = []
for i in alpha:
   print("for alpha =", i)
    clf = KNeighborsClassifier(n neighbors=i)
    clf.fit(train_x_responseCoding, train_y)
    sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train x responseCoding, train y)
    sig_clf_probs = sig_clf.predict_proba(cv_x_responseCoding)
    cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    # to avoid rounding error while multiplying probabilites we use log-probability estimates
    print("Log Loss :",log_loss(cv_y, sig_clf_probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
    ax.annotate((alpha[i],str(txt)), (alpha[i],cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
```

```
best_alpha = np.argmin(cv_log_error_array)
clf = KNeighborsClassifier(n_neighbors=alpha[best_alpha])
clf.fit(train_x_responseCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_responseCoding, train_y)

predict_y = sig_clf.predict_proba(train_x_responseCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train, predict_y, labels=clf.classes_, eps=le-15))
predict_y = sig_clf.predict_proba(cv_x_responseCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_loss(y_cv, predict_y, labels=clf.classes_, eps=le-15))
predict_y = sig_clf.predict_proba(test_x_responseCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p redict_y, labels=clf.classes_, eps=le-15))
```

for alpha = 5Log Loss: 1.0244406216745023 for alpha = 11 Log Loss : 1.0279061357877384 for alpha = 15Log Loss: 1.0378128782396658 for alpha = 21 Log Loss: 1.045715412362981 for alpha = 31Log Loss : 1.058952645307042 for alpha = 41Log Loss: 1.072955246242509 for alpha = 51 Log Loss: 1.074524309299886 for alpha = 99 Log Loss: 1.1140671249609737



For values of best alpha = 5 The train log loss is: 0.4886395645354538

For values of best alpha = 5 The cross validation log loss is: 1.0244406216745023

For values of best alpha = 5 The test log loss is: 1.07723312219067

4.2.2. Testing the model with best hyper paramters

In [170]:

"
clf = KNeighborsClassifier(n_neighbors=alpha[best_alpha])
predict_and_plot_confusion_matrix(train_x_responseCoding, train_y, cv_x_responseCoding, cv_y, clf)

- 100

- 80

- 60

40

- 20

1.0

- 0.8

- 0.6

- 0.4

0.2

0.75

0.60

- 0.45

- 0.30

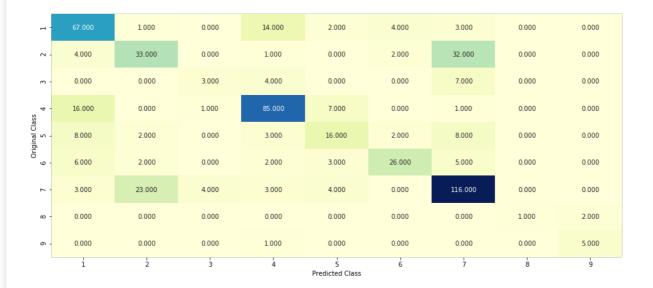
-0.15

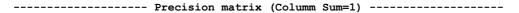
- 0.00

Log loss : 1.0244406216745023

Number of mis-classified points: 0.3383458646616541

------ Confusion matrix







----- Recall matrix (Row sum=1) ------



4.2.3. Sample Query point -1

```
In [171]:
clf = KNeighborsClassifier(n_neighbors=alpha[best_alpha])
clf.fit(train_x_responseCoding, train_y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_responseCoding, train_y)
test point index = 1
predicted_cls = sig_clf.predict(test_x_responseCoding[0].reshape(1,-1))
print("Predicted Class :", predicted cls[0])
print("Actual Class :", test y[test point index])
neighbors = clf.kneighbors(test_x_responseCoding[test_point_index].reshape(1, -1), alpha[best_alpha
1)
print("The ",alpha[best_alpha]," nearest neighbours of the test points belongs to classes",train_y
[neighbors[1][0]])
print("Fequency of nearest points :",Counter(train_y[neighbors[1][0]]))
Predicted Class: 7
Actual Class: 7
The 5 nearest neighbours of the test points belongs to classes [3 7 7 7 7]
Fequency of nearest points : Counter({7: 4, 3: 1})
```

4.2.4. Sample Query Point-2

```
In [172]:
```

```
clf = KNeighborsClassifier(n_neighbors=alpha[best_alpha])
clf.fit(train_x_responseCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_responseCoding, train_y)

test_point_index = 100

predicted_cls = sig_clf.predict(test_x_responseCoding[test_point_index].reshape(1,-1))
print("Predicted Class :", predicted_cls[0])
print("Actual Class :", test_y[test_point_index])
neighbors = clf.kneighbors(test_x_responseCoding[test_point_index].reshape(1, -1), alpha[best_alpha])
print("the k value for knn is",alpha[best_alpha],"and the nearest neighbours of the test points be longs to classes",train_y[neighbors[1][0]])
print("Fequency of nearest points :",Counter(train_y[neighbors[1][0]]))

Predicted Class : 1
Actual Class : 6
```

Actual Class : 6
the k value for knn is 5 and the nearest neighbours of the test points belongs to classes [1 1 1 1 1 1]
Fequency of nearest points : Counter({1: 5})

4.3. Logistic Regression

4.3.1. With Class balancing

4.3.1.1. Hyper paramter tuning

```
In [173]:
```

```
# SHULLIE-ILUE, VELDOSE-V, EPSILOH-V.I, H_JODS-I, LAHGOH_SCACE-NOHE, LEALHIHY_LACE- OPCIMAL , ECAV
=0.0, power_t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef_init, intercept_init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/geometric-in
tuition-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base_estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample_weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link:
alpha = [10 ** x for x in range(-6, 3)]
cv_log_error_array = []
for i in alpha:
   print("for alpha =", i)
    clf = SGDClassifier(class_weight='balanced', alpha=i, penalty='12', loss='log', random_state=42
    clf.fit(train x onehotCoding, train y)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig_clf.fit(train_x_onehotCoding, train_y)
    sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
    cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
    # to avoid rounding error while multiplying probabilites we use log-probability estimates
   print("Log Loss :",log_loss(cv_y, sig_clf_probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv log error array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
    ax.annotate((alpha[i],str(txt)), (alpha[i],cv_log_error_array[i]))
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = SGDClassifier(class weight='balanced', alpha=alpha[best alpha], penalty='12', loss='log', ran
dom state=42)
clf.fit(train x onehotCoding, train y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)
predict_y = sig_clf.predict_proba(train_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is: ",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=1e-15))
for alpha = 1e-06
```

Log Loss: 1.112287140255073 for alpha = 1e-05 Log Loss: 1.071724244995298 for alpha = 0.0001 Log Loss: 0.9944756312849151 for alpha = 0.001

Log Loss: 1.037668198417139

for alpha = 0.01

Log Loss : 1.152900488194322

for alpha = 0.1

Log Loss: 1.6556050167603393

for alpha = 1

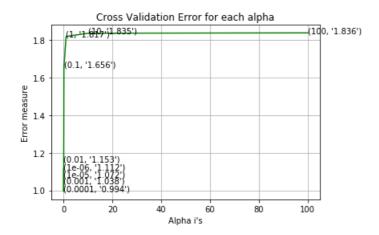
Log Loss : 1.8174110711678708

for alpha = 10

Log Loss: 1.834553887619345

for alpha = 100

Log Loss : 1.8364174919258738



For values of best alpha = 0.0001 The train log loss is: 0.42092795117266746

For values of best alpha = 0.0001 The cross validation log loss is: 0.9944756312849151

For values of best alpha = 0.0001 The test log loss is: 0.9979471387962748

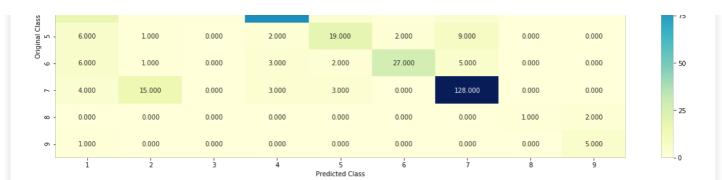
4.3.1.2. Testing the model with best hyper paramters

In [174]:

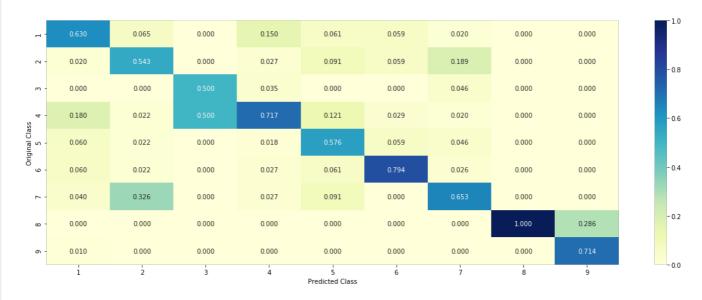
```
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n jobs=1, random state=None, learning rate='optimal', eta0
=0.0, power t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef init, intercept init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/geometric-in
tuition-1/
#-----
clf = SGDClassifier(class_weight='balanced', alpha=alpha[best_alpha], penalty='12', loss='log', ran
dom state=42)
predict_and_plot_confusion_matrix(train_x_onehotCoding, train_y, cv_x_onehotCoding, cv_y, clf)
```

п -		3.000	0.000	17.000	2.000	2.000	4.000	0.000	0.000
- 2	2.000	25.000	0.000	3.000	3.000	2.000	37.000	0.000	0.000
m -	0.000	0.000	1.000	4.000	0.000	0.000	9.000	0.000	0.000
4 -	18.000	1.000	1.000	81.000	4.000	1.000	4.000	0.000	0.000

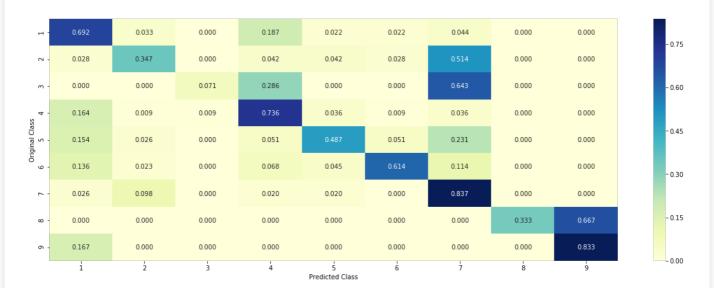
- 125 - 100



----- Precision matrix (Columm Sum=1) ------



----- Recall matrix (Row sum=1) -----



4.3.1.3. Feature Importance

In [175]:

```
def get_imp_feature_names(text, indices, removed_ind = []):
    word_present = 0
    tabulte_list = []
    incresingorder_ind = 0
    for i in indices:
        if i < train_gene_feature_onehotCoding.shape[1]:
            tabulte_list.append([incresingorder_ind, "Gene", "Yes"])
    elif i < 18:
        tabulte_list.append([incresingorder_ind,"Variation", "Yes"])</pre>
```

```
if ((i > 17) & (i not in removed_ind)) :
    word = train_text_features[i]
    yes_no = True if word in text.split() else False
    if yes_no:
        word_present += 1
        tabulte_list.append([incresingorder_ind,train_text_features[i], yes_no])
    incresingorder_ind += 1
print(word_present, "most importent features are present in our query point")
print("-"*50)
print("The features that are most importent of the ",predicted_cls[0]," class:")
print (tabulate(tabulte_list, headers=["Index",'Feature name', 'Present or Not']))
```

4.3.1.3.1. Correctly Classified point

```
In [176]:
```

```
# from tabulate import tabulate
clf = SGDClassifier(class_weight='balanced', alpha=alpha[best_alpha], penalty='12', loss='log', ran
dom state=42)
clf.fit(train x onehotCoding,train y)
test point index = 1
no feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.coef_) [predicted_cls-1][:,:no_feature]
print("-"*50)
get impfeature names (indices [0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test_point_index], no_feature)
Predicted Class: 7
Predicted Class Probabilities: [[1.300e-03 2.780e-02 1.408e-01 7.100e-03 6.500e-03 2.700e-03 8.122
  9.000e-04 7.000e-04]]
Actual Class: 7
73 Text feature [1e] present in test data point [True]
188 Text feature [19] present in test data point [True]
Out of the top 500 features 2 are present in query point
```

4.3.1.3.2. Incorrectly Classified point

```
In [177]:
```

```
test_point_index = 100
no feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef_) [predicted_cls-1][:,:no_feature]
print("-"*50)
get_impfeature_names(indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test point index], no feature)
Predicted Class: 1
Predicted Class Probabilities: [[9.664e-01 2.590e-02 0.000e+00 2.000e-04 1.500e-03 2.000e-04 4.900
  9.000e-04 0.000e+00]]
Actual Class: 6
178 Text feature [2b] present in test data point [True]
194 Text feature [23] present in test data point [True]
Out of the top 500 features 2 are present in query point
```

4.3.2. Without Class balancing

4.3.2.1. Hyper paramter tuning

```
In [178]:
```

```
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear_model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n_jobs=1, random_state=None, learning_rate='optimal', eta0
=0.0, power t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef_init, intercept_init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/geometric-in
tuition-1/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample_weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict_proba(X) Posterior probabilities of classification
# video link:
alpha = [10 ** x for x in range(-6, 1)]
cv_log_error_array = []
for i in alpha:
   print("for alpha =", i)
    clf = SGDClassifier(alpha=i, penalty='12', loss='log', random state=42)
    clf.fit(train_x_onehotCoding, train_y)
    sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train x onehotCoding, train y)
    sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
    cv log error array.append(log loss(cv y, sig clf probs, labels=clf.classes , eps=1e-15))
    print("Log Loss :",log loss(cv y, sig clf probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
   ax.annotate((alpha[i],str(txt)), (alpha[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best alpha = np.argmin(cv log error array)
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='log', random_state=42)
clf.fit(train_x_onehotCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)
predict_y = sig_clf.predict_proba(train_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict_y, labels=clf.classes_, eps=1e-15))
predict y = sig clf.predict proba(cv x onehotCoding)
```

```
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=le-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=le-15))
```

```
for alpha = 1e-06

Log Loss : 1.0673748952055069

for alpha = 1e-05

Log Loss : 1.0638504969277136

for alpha = 0.0001

Log Loss : 1.0235870345137565

for alpha = 0.001

Log Loss : 1.0977724750929096

for alpha = 0.01

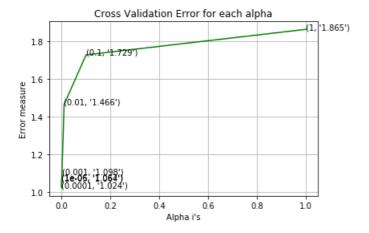
Log Loss : 1.4663008041914463

for alpha = 0.1

Log Loss : 1.729349590427073

for alpha = 1

Log Loss : 1.8647046593811563
```



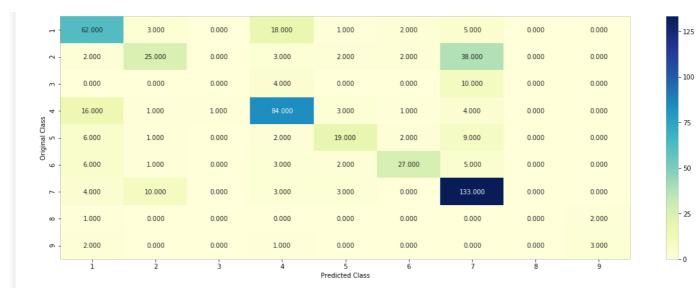
```
For values of best alpha = 0.0001 The train log loss is: 0.41720869741007016

For values of best alpha = 0.0001 The cross validation log loss is: 1.0235870345137565

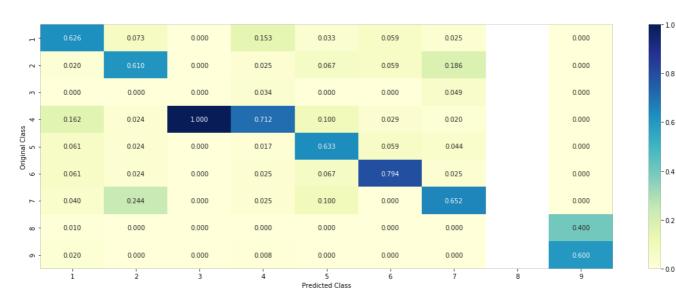
For values of best alpha = 0.0001 The test log loss is: 1.0125535005263862
```

4.3.2.2. Testing model with best hyper parameters

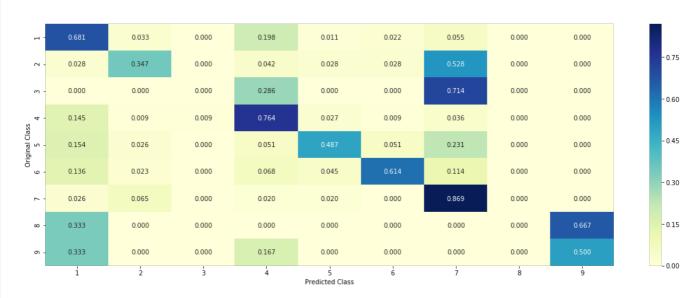
In [179]:



----- Precision matrix (Columm Sum=1) ------



----- Recall matrix (Row sum=1)



0.75

0.60

4.3.2.3. Feature Importance, Correctly Classified point

In [180]:

```
cir.rit(train x onenotCoding,train y)
test point index = 1
no feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.coef_)[predicted_cls-1][:,:no_feature]
print("-"*50)
get impfeature names (indices [0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test point index], no feature)
Predicted Class: 7
Predicted Class Probabilities: [[1.200e-03 2.810e-02 9.940e-02 1.100e-02 5.100e-03 1.900e-03 8.521
  1.000e-03 1.000e-04]]
Actual Class: 7
100 Text feature [1e] present in test data point [True]
283 Text feature [19] present in test data point [True]
Out of the top 500 features 2 are present in query point
4.3.2.4. Feature Importance, Inorrectly Classified point
In [181]:
test_point_index = 100
no feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef_) [predicted_cls-1][:,:no_feature]
print("-"*50)
get impfeature names (indices [0],
test df['TEXT'].iloc[test point index],test df['Gene'].iloc[test point index],test df['Variation']
.iloc[test point index], no feature)
Predicted Class: 1
Predicted Class Probabilities: [[9.662e-01 2.460e-02 0.000e+00 3.000e-04 1.200e-03 1.000e-04 7.200
e - 0.3
  4.000e-04 0.000e+00]]
Actual Class : 6
183 Text feature [2b] present in test data point [True]
218 Text feature [23] present in test data point [True]
```

4.4. Linear Support Vector Machines

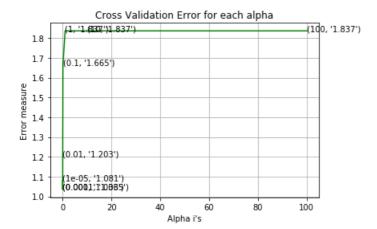
Out of the top 500 features 2 are present in query point

4.4.1. Hyper paramter tuning

```
In [182]:
```

```
# video link: https://www.appliedaicourse.com/course/applied-ai-course-
online/lessons/mathematical-derivation-copy-8/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample_weight]) Fit the calibrated model
# get_params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link:
alpha = [10 ** x for x in range(-5, 3)]
cv log error array = []
for i in alpha:
   print("for C =", i)
     clf = SVC(C=i,kernel='linear',probability=True, class_weight='balanced')
    clf = SGDClassifier( class_weight='balanced', alpha=i, penalty='12', loss='hinge', random_state
=42)
    clf.fit(train x onehotCoding, train y)
    sig clf = CalibratedClassifierCV(clf, method="sigmoid")
    sig clf.fit(train x onehotCoding, train y)
    sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
    print("Log Loss :",log_loss(cv_y, sig_clf_probs))
fig, ax = plt.subplots()
ax.plot(alpha, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
    ax.annotate((alpha[i],str(txt)), (alpha[i],cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best alpha = np.argmin(cv_log_error_array)
# clf = SVC(C=i,kernel='linear',probability=True, class_weight='balanced')
clf = SGDClassifier(class_weight='balanced', alpha=alpha[best_alpha], penalty='12', loss='hinge', r
andom state=42)
clf.fit(train x onehotCoding, train y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x onehotCoding, train y)
predict_y = sig_clf.predict_proba(train_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The train log loss is:",log_loss(y_train,
predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The cross validation log loss is:",log_lo
ss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best alpha = ', alpha[best_alpha], "The test log loss is:",log_loss(y_test, p
redict_y, labels=clf.classes_, eps=1e-15))
for C = 1e-05
Log Loss : 1.0811257336152222
for C = 0.0001
Log Loss: 1.0350393656837595
for C = 0.001
Log Loss: 1.0358481268390949
for C = 0.01
Log Loss : 1.2031173835713462
for C = 0.1
Log Loss: 1.6652042783153596
for C = 1
```

```
Log Loss: 1.8368581150069272
for C = 10
Log Loss: 1.836857614399901
for C = 100
Log Loss: 1.8368201139810911
```



```
For values of best alpha = 0.0001 The train log loss is: 0.484743680884268

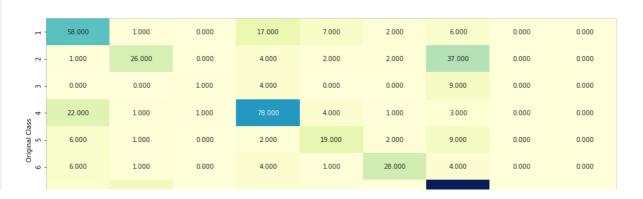
For values of best alpha = 0.0001 The cross validation log loss is: 1.0350393656837595

For values of best alpha = 0.0001 The test log loss is: 1.0712014562394097
```

4.4.2. Testing model with best hyper parameters

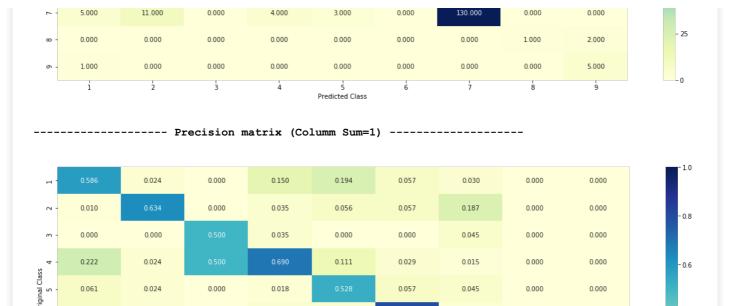
In [183]:

```
# read more about support vector machines with linear kernals here http://scikit-
learn.org/stable/modules/generated/sklearn.svm.SVC.html
# default parameters
# SVC(C=1.0, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, t
01=0.001,
# cache size=200, class weight=None, verbose=False, max iter=-1, decision function shape='ovr', ra
ndom state=None)
# Some of methods of SVM()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-
online/lessons/mathematical-derivation-copy-8/
# clf = SVC(C=alpha[best alpha], kernel='linear', probability=True, class weight='balanced')
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='hinge',
random_state=42,class_weight='balanced')
predict_and_plot_confusion_matrix(train_x_onehotCoding, train_y,cv_x_onehotCoding,cv_y, clf)
```



- 100

75



0.028

0.083

0.000

0.000

Predicted Class

0.000

0.000

0.000

0.020

0.000

0.000

0.000

0.000

0.000

0.000

0.000

0.286

0.4

- 0.2

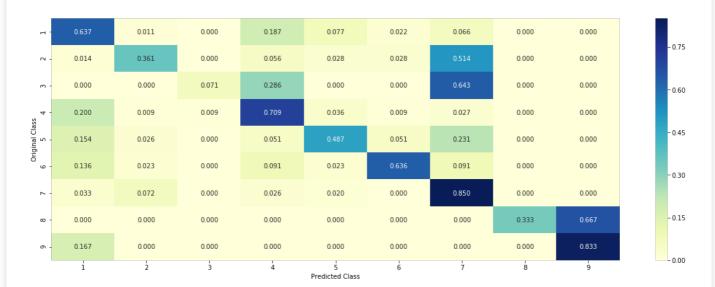
----- Recall matrix (Row sum=1) ------

0.035

0.035

0.000

0.000



4.3.3. Feature Importance

0.061

0.051

0.000

0.010

0.024

0.268

0.000

0.000

0.000

0.000

0.000

0.000

4.3.3.1. For Correctly classified point

```
In [184]:
```

```
clf = SGDClassifier(alpha=alpha[best_alpha], penalty='12', loss='hinge', random_state=42)
clf.fit(train_x_onehotCoding,train_y)
test_point_index = 1
# test_point_index = 100
no_feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef_)[predicted_cls-1][:,:no_feature]
```

```
print("-"*50)
get impfeature names (indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test_point_index], no_feature)
Predicted Class: 7
Predicted Class Probabilities: [[6.300e-03 2.840e-02 9.910e-02 3.230e-02 2.200e-02 1.060e-02 8.001
e-01
  7.000e-04 5.000e-04]]
Actual Class: 7
283 Text feature [1e] present in test data point [True]
298 Text feature [19] present in test data point [True]
332 Text feature [2g] present in test data point [True]
338 Text feature [118] present in test data point [True]
Out of the top 500 features 4 are present in query point
4.3.3.2. For Incorrectly classified point
In [185]:
test_point_index = 100
no feature = 500
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.coef_) [predicted_cls-1][:,:no_feature]
print("-"*50)
get impfeature names (indices[0],
test_df['TEXT'].iloc[test_point_index],test_df['Gene'].iloc[test_point_index],test_df['Variation']
.iloc[test point index], no feature)
```

4.5 Random Forest Classifier

4.5.1. Hyper paramter tuning (With Tfidf Encoding)

```
In [186]:
```

```
# -----
# default parameters
# sklearn.ensemble.RandomForestClassifier(n_estimators=10, criterion='gini', max_depth=None, min_s
amples_split=2,
# min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_
impurity_decrease=0.0,
# min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None,
verbose=0, warm_start=False,
# class weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict_proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature importances : array of shape = [n features]
# The feature importances (the higher, the more important the feature).
```

```
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample weight]) Fit the calibrated model
# get params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict_proba(X) Posterior probabilities of classification
# video link:
alpha = [100,200,500,1000,2000]
max depth = [5, 10]
cv log error array = []
for i in alpha:
    for j in max depth:
        print("for n estimators =", i,"and max depth = ", j)
        clf = RandomForestClassifier(n_estimators=i, criterion='gini', max_depth=j, random_state=42
, n jobs=-1)
        clf.fit(train_x_onehotCoding, train_y)
        sig clf = CalibratedClassifierCV(clf, method="sigmoid")
        sig clf.fit(train x onehotCoding, train y)
        sig_clf_probs = sig_clf.predict_proba(cv_x_onehotCoding)
        cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
        print("Log Loss :",log_loss(cv_y, sig_clf_probs))
fig, ax = plt.subplots()
features = np.dot(np.array(alpha)[:,None],np.array(max_depth)[None]).ravel()
ax.plot(features, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv_log_error_array,3)):
    ax.annotate((alpha[int(i/2)],max_depth[int(i%2)],str(txt)),
(features[i],cv_log_error_array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best_alpha = np.argmin(cv_log_error_array)
clf = RandomForestClassifier(n estimators=alpha[int(best alpha/2)], criterion='gini', max depth=max
_depth[int(best_alpha%2)], random_state=42, n_jobs=-1)
clf.fit(train_x_onehotCoding, train_y)
sig clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)
predict y = sig clf.predict proba(train x onehotCoding)
print('For values of best estimator = ', alpha[int(best_alpha/2)], "The train log loss
is:",log_loss(y_train, predict_y, labels=clf.classes_, eps=1e-15))
predict y = sig clf.predict proba(cv x onehotCoding)
print('For values of best estimator = ', alpha[int(best_alpha/2)], "The cross validation log loss
is:",log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_onehotCoding)
print('For values of best estimator = ', alpha[int(best_alpha/2)], "The test log loss
is:",log_loss(y_test, predict_y, labels=clf.classes_, eps=1e-15))
for n estimators = 100 and max depth = 5
Log Loss : 1.1961099672371338
for n estimators = 100 and max depth = 10
Log Loss : 1.188780444172098
for n estimators = 200 and max depth = 5
Log Loss: 1.1789605431113541
for n_{estimators} = 200 and max depth = 10
Log Loss: 1.1735059340151741
for n estimators = 500 and max depth = 5
Log Loss : 1.1766864021598995
for n estimators = 500 and max depth = 10
```

```
Log Loss: 1.1644327447602387

for n_estimators = 1000 and max depth = 5

Log Loss: 1.1718034896593095

for n_estimators = 1000 and max depth = 10

Log Loss: 1.1587798292862308

for n_estimators = 2000 and max depth = 5

Log Loss: 1.1715149584826912

for n_estimators = 2000 and max depth = 10

Log Loss: 1.1586226980717669

For values of best estimator = 2000 The train log loss is: 0.5661983939675271

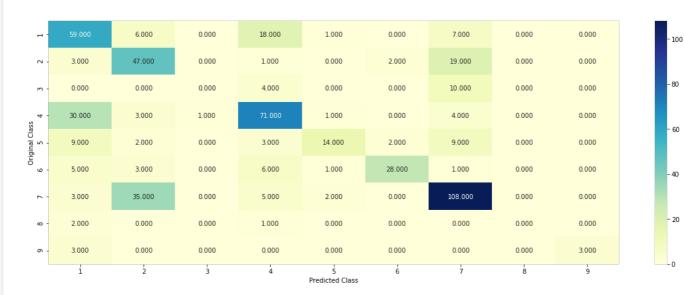
For values of best estimator = 2000 The cross validation log loss is: 1.1586226980717669

For values of best estimator = 2000 The test log loss is: 1.1425009459571944
```

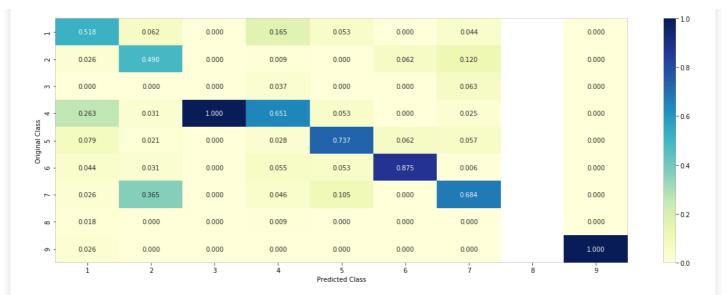
4.5.2. Testing model with best hyper parameters (Tfidf Encoding)

```
In [187]:
```

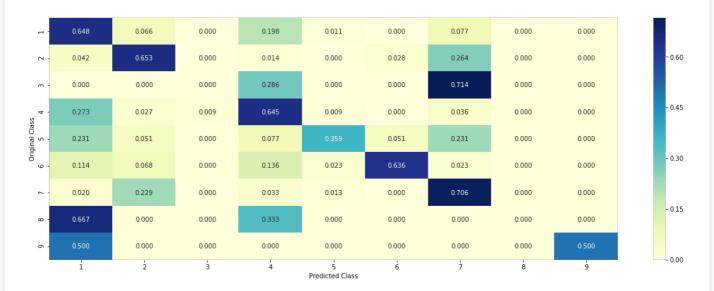
```
# -----
# default parameters
# sklearn.ensemble.RandomForestClassifier(n_estimators=10, criterion='gini', max_depth=None, min_s
amples split=2.
# min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_
impurity decrease=0.0,
# min impurity split=None, bootstrap=True, oob score=False, n_jobs=1, random_state=None,
verbose=0, warm start=False,
# class_weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict_proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature_importances_ : array of shape = [n_features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
clf = RandomForestClassifier(n_estimators=alpha[int(best_alpha/2)], criterion='gini', max_depth=max
_depth[int(best_alpha%2)], random_state=42, n_jobs=-1)
predict and plot confusion matrix(train x onehotCoding, train y,cv x onehotCoding,cv y, clf)
```



----- Precision matrix (Columm Sum=1) ------



----- Recall matrix (Row sum=1) -----



4.5.3. Feature Importance

4.5.3.1. Correctly Classified point

```
In [188]:
```

```
# test point index = 10
clf = RandomForestClassifier(n_estimators=alpha[int(best_alpha/2)], criterion='gini', max_depth=max
_depth[int(best_alpha%2)], random_state=42, n_jobs=-1)
clf.fit(train_x_onehotCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_onehotCoding, train_y)
test_point_index = 1
no feature = 100
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index]),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.feature_importances_)
print("-"*50)
get_impfeature_names(indices[:no_feature], test_df['TEXT'].iloc[test_point_index],test_df['Gene'].
iloc[test_point_index], test_df['Variation'].iloc[test_point_index], no_feature)
Predicted Class: 7
Predicted Class Probabilities: [[0.0997 0.2011 0.1509 0.0872 0.065 0.0582 0.319 0.0093 0.0096]]
```

```
Actual Class: 7
                    -----
Out of the top 100 features 0 are present in query point
4.5.3.2. Inorrectly Classified point
In [189]:
test point index = 100
no_feature = 100
predicted_cls = sig_clf.predict(test_x_onehotCoding[test_point_index])
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
\verb"np.round(sig_clf.predict_proba(test_x_onehotCoding[test_point_index])", 4)")" \\
print("Actuall Class :", test_y[test_point_index])
indices = np.argsort(-clf.feature_importances_)
print("-"*50)
get_impfeature_names(indices[:no_feature], test_df['TEXT'].iloc[test_point_index],test_df['Gene'].
iloc[test point index], test df['Variation'].iloc[test point index], no feature)
Predicted Class: 2
Predicted Class Probabilities: [[0.1902 0.2815 0.0248 0.124 0.0668 0.0616 0.2321 0.01 0.009 ]]
Actuall Class: 6
32 Text feature [2j] present in test data point [True]
Out of the top 100 features 1 are present in query point
```

4.5.3. Hyper paramter tuning (With Response Coding)

```
In [190]:
# default parameters
# sklearn.ensemble.RandomForestClassifier(n_estimators=10, criterion='gini', max_depth=None, min_s
amples split=2,
# min samples leaf=1, min weight fraction leaf=0.0, max features='auto', max leaf nodes=None, min
impurity_decrease=0.0,
# min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None,
verbose=0, warm start=False,
# class_weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample_weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature_importances_ : array of shape = [n_features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
# find more about CalibratedClassifierCV here at http://scikit-
learn.org/stable/modules/generated/sklearn.calibration.CalibratedClassifierCV.html \\
# default paramters
# sklearn.calibration.CalibratedClassifierCV(base estimator=None, method='sigmoid', cv=3)
# some of the methods of CalibratedClassifierCV()
# fit(X, y[, sample_weight]) Fit the calibrated model
# get_params([deep]) Get parameters for this estimator.
# predict(X) Predict the target of new samples.
# predict proba(X) Posterior probabilities of classification
# video link:
alpha = [10,50,100,200,500,1000]
```

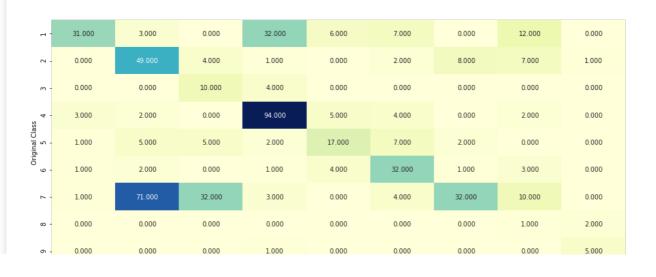
```
max_depth = [2,3,5,10]
cv_log_error_array = []
for i in alpha:
    for j in max depth:
        print("for n estimators =", i,"and max depth = ", j)
        clf = RandomForestClassifier(n estimators=i, criterion='gini', max depth=j, random state=42
, n_jobs=-1)
        clf.fit(train x responseCoding, train y)
        sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
        sig_clf.fit(train_x_responseCoding, train_y)
        sig_clf_probs = sig_clf.predict_proba(cv_x_responseCoding)
        cv_log_error_array.append(log_loss(cv_y, sig_clf_probs, labels=clf.classes_, eps=1e-15))
        print("Log Loss :",log_loss(cv_y, sig_clf_probs))
fig, ax = plt.subplots()
features = np.dot(np.array(alpha)[:,None],np.array(max_depth)[None]).ravel()
ax.plot(features, cv_log_error_array,c='g')
for i, txt in enumerate(np.round(cv log error array,3)):
    ax.annotate((alpha[int(i/4)],max_depth[int(i%4)],str(txt)),
(features[i],cv log error array[i]))
plt.grid()
plt.title("Cross Validation Error for each alpha")
plt.xlabel("Alpha i's")
plt.ylabel("Error measure")
plt.show()
best alpha = np.argmin(cv log error array)
clf = RandomForestClassifier(n_estimators=alpha[int(best_alpha/4)], criterion='gini', max_depth=max
_depth[int(best_alpha%4)], random_state=42, n_jobs=-1)
clf.fit(train x responseCoding, train y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig clf.fit(train x responseCoding, train y)
predict_y = sig_clf.predict_proba(train_x_responseCoding)
print('For values of best alpha = ', alpha[int(best alpha/4)], "The train log loss is:",log loss(y
_train, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(cv_x_responseCoding)
print('For values of best alpha = ', alpha[int(best_alpha/4)], "The cross validation log loss is:"
,log_loss(y_cv, predict_y, labels=clf.classes_, eps=1e-15))
predict_y = sig_clf.predict_proba(test_x_responseCoding)
print('For values of best alpha = ', alpha[int(best_alpha/4)], "The test log loss is:",log_loss(y_
test, predict_y, labels=clf.classes_, eps=1e-15))
for n estimators = 10 and max depth = 2
Log Loss: 2.1541825651587434
for n_estimators = 10 and max depth = 3
Log Loss: 1.6789156527120346
for n_estimators = 10 and max depth = 5
Log Loss : 1.648618719867701
for n estimators = 10 and max depth = 10
Log Loss: 1.7786257212391088
for n estimators = 50 and max depth = 2
Log Loss: 1.6721932708747345
for n_{estimators} = 50 and max depth = 3
Log Loss: 1.4209362234227703
for n_{estimators} = 50 and max depth = 5
Log Loss: 1.3702537986440313
for n estimators = 50 and max depth = 10
Log Loss: 1.6337129646045765
for n_{estimators} = 100 and max depth = 2
Log Loss: 1.566338074582179
for n_{estimators} = 100 and max depth = 3
Log Loss: 1.435388118067988
for n_{estimators} = 100 and max depth = 5
Log Loss : 1.3574844424318204
for n estimators = 100 and max depth = 10
Log Loss: 1.613046119924267
for n_{estimators} = 200 and max depth = 2
Log Loss: 1.634722393947789
for n estimators = 200 and max depth = 3
Log Loss : 1.441398008213494
for n estimators = 200 and max depth = 5
Log Loss: 1.3682059870937298
for n estimators = 200 and max depth = 10
Log Loss : 1.6826352050441715
```

```
for n estimators = 500 and max depth = 2
Log Loss: 1.689006872643716
for n estimators = 500 and max depth = 3
Log Loss : 1.5266353956937997
for n estimators = 500 and max depth = 5
Log Loss : 1.3608056229366212
for n_estimators = 500 and max depth = 10
Log Loss: 1.7051353255159676
for n_estimators = 1000 and max depth = 2
Log Loss: 1.7125146533473887
for n estimators = 1000 and max depth = 3
Log Loss: 1.5525452640257147
for n_{estimators} = 1000 and max depth = 5
Log Loss: 1.3448255541680398
for n estimators = 1000 and max depth = 10
Log Loss: 1.681880900791406
For values of best alpha = 1000 The train log loss is: 0.045090203018991776
For values of best alpha = 1000 The cross validation log loss is: 1.3448255541680398
For values of best alpha = 1000 The test log loss is: 1.4074976182469157
```

4.5.4. Testing model with best hyper parameters (Response Coding)

```
In [191]:
```

```
# -----
# default parameters
# sklearn.ensemble.RandomForestClassifier(n_estimators=10, criterion='gini', max_depth=None, min_s
amples split=2,
# min samples leaf=1, min weight fraction leaf=0.0, max features='auto', max leaf nodes=None, min
impurity decrease=0.0,
# min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None,
verbose=0, warm start=False,
# class weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict_proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature_importances_ : array of shape = [n_features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
clf = RandomForestClassifier(max depth=max depth[int(best alpha%4)],
n_estimators=alpha[int(best_alpha/4)], criterion='gini', max_features='auto',random_state=42)
predict_and_plot_confusion_matrix(train_x_responseCoding, train_y,cv_x_responseCoding,cv_y, clf)
```



60

- 40

- 20

1 2 3 4 5 6 7 8 9

Predicted Class

0.75

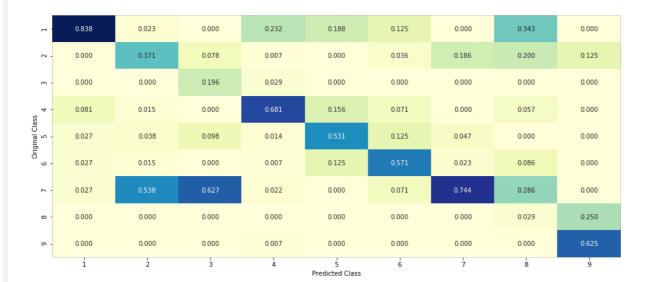
0.60

0.45

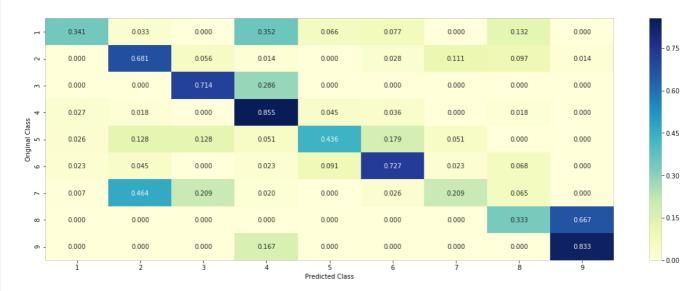
- 0.30

-015

----- Precision matrix (Columm Sum=1) ------



----- Recall matrix (Row sum=1) ------



4.5.5. Feature Importance

4.5.5.1. Correctly Classified point

In [192]:

```
clf = RandomForestClassifier(n_estimators=alpha[int(best_alpha/4)], criterion='gini', max_depth=max
    _depth[int(best_alpha%4)], random_state=42, n_jobs=-1)
clf.fit(train_x_responseCoding, train_y)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid")
sig_clf.fit(train_x_responseCoding, train_y)

test_point_index = 1
no_feature = 27
predicted_cls = sig_clf.predict(test_x_responseCoding[test_point_index].reshape(1,-1))
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
np.round(sig_clf.predict_proba(test_x_responseCoding[test_point_index].reshape(1,-1)),4))
print("Actual Class :", test_y[test_point_index])
indices = np.argsort(-clf.feature_importances_)
print("-"*50)
```

```
for i in indices:
    if i<9:
       print("Gene is important feature")
    elif i<18:
      print("Variation is important feature")
    else:
       print("Text is important feature")
Predicted Class: 3
Predicted Class Probabilities: [[0.0101 0.0902 0.5679 0.018 0.0223 0.0264 0.1897 0.0625 0.0129]]
Actual Class: 7
Variation is important feature
Gene is important feature
Text is important feature
Text is important feature
Gene is important feature
Text is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Variation is important feature
Text is important feature
Gene is important feature
Variation is important feature
Gene is important feature
Variation is important feature
Text is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Gene is important feature
4.5.5.2. Incorrectly Classified point
In [193]:
test point index = 100
predicted_cls = sig_clf.predict(test_x_responseCoding[test_point_index].reshape(1,-1))
print("Predicted Class :", predicted_cls[0])
print("Predicted Class Probabilities:",
print("Actual Class :", test y[test point index])
indices = np.argsort(-clf.feature importances )
print("-"*50)
for i in indices:
   if i<9:
       print("Gene is important feature")
    elif i<18:
      print("Variation is important feature")
    else:
       print("Text is important feature")
Predicted Class : 1
Predicted Class Probabilities: [[0.9721 0.0051 0.0026 0.0065 0.0021 0.0034 0.002 0.0032 0.0029]]
Actual Class : 6
Variation is important feature
Gene is important feature
Text is important feature
Text is important feature
```

PTINC

```
Gene is important feature
Text is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Variation is important feature
Text is important feature
Gene is important feature
Variation is important feature
Gene is important feature
Variation is important feature
Text is important feature
Text is important feature
Text is important feature
Gene is important feature
Gene is important feature
Gene is important feature
```

4.7 Stack the models

4.7.1 testing with hyper parameter tuning

```
In [194]:
```

```
# read more about SGDClassifier() at http://scikit-
learn.org/stable/modules/generated/sklearn.linear model.SGDClassifier.html
# default parameters
# SGDClassifier(loss='hinge', penalty='12', alpha=0.0001, 11 ratio=0.15, fit intercept=True, max i
ter=None, tol=None,
# shuffle=True, verbose=0, epsilon=0.1, n jobs=1, random state=None, learning rate='optimal', eta0
=0.0, power_t=0.5,
# class_weight=None, warm_start=False, average=False, n_iter=None)
# some of methods
# fit(X, y[, coef init, intercept init, ...]) Fit linear model with Stochastic Gradient Descent.
# predict(X) Predict class labels for samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/geometric-in
tuition-1/
# read more about support vector machines with linear kernals here http://scikit-
learn.org/stable/modules/generated/sklearn.svm.SVC.html
# default parameters
# SVC(C=1.0, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, t
# cache_size=200, class_weight=None, verbose=False, max_iter=-1, decision_function_shape='ovr', ra
ndom state=None)
# Some of methods of SVM()
# fit(X, y, [sample weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# video link: https://www.appliedaicourse.com/course/applied-ai-course-
online/lessons/mathematical-derivation-copy-8/
# read more about support vector machines with linear kernals here http://scikit-
learn.org/stable/modules/generated/sklearn.ensemble.RandomForestClassifier.html \\
# default parameters
# sklearn.ensemble.RandomForestClassifier(n estimators=10, criterion='gini', max depth=None, min s
amples split=2,
# min samples leaf=1, min weight fraction leaf=0.0, max features='auto', max leaf nodes=None, min
impurity decrease=0.0,
# min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None,
verbose=0, warm start=False,
```

```
# class_weight=None)
# Some of methods of RandomForestClassifier()
# fit(X, y, [sample_weight]) Fit the SVM model according to the given training data.
# predict(X) Perform classification on samples in X.
# predict proba (X) Perform classification on samples in X.
# some of attributes of RandomForestClassifier()
# feature_importances_ : array of shape = [n_features]
# The feature importances (the higher, the more important the feature).
# video link: https://www.appliedaicourse.com/course/applied-ai-course-online/lessons/random-fores
t-and-their-construction-2/
clf1 = SGDClassifier(alpha=0.001, penalty='12', loss='log', class weight='balanced', random state=0
clf1.fit(train x onehotCoding, train y)
sig clf1 = CalibratedClassifierCV(clf1, method="sigmoid")
clf2 = SGDClassifier(alpha=1, penalty='12', loss='hinge', class_weight='balanced', random_state=0)
clf2.fit(train_x_onehotCoding, train_y)
sig clf2 = CalibratedClassifierCV(clf2, method="sigmoid")
clf3 = MultinomialNB(alpha=0.001)
clf3.fit(train_x_onehotCoding, train_y)
sig clf3 = CalibratedClassifierCV(clf3, method="sigmoid")
sig_clf1.fit(train_x_onehotCoding, train_y)
print("Logistic Regression : Log Loss: %0.2f" % (log_loss(cv_y, sig_clf1.predict_proba(cv_x_onehot
Coding))))
sig_clf2.fit(train_x_onehotCoding, train_y)
print("Support vector machines : Log Loss: %0.2f" % (log loss(cv y,
sig clf2.predict proba(cv x onehotCoding))))
sig_clf3.fit(train_x_onehotCoding, train_y)
print("Naive Bayes : Log Loss: %0.2f" % (log_loss(cv y, sig_clf3.predict_proba(cv_x_onehotCoding)))
print("-"*50)
alpha = [0.0001, 0.001, 0.01, 0.1, 1, 1, 10]
best_alpha = 999
for i in alpha:
    lr = LogisticRegression(C=i)
    sclf = StackingClassifier(classifiers=[sig_clf1, sig_clf2, sig_clf3], meta_classifier=lr, use_p
robas=True)
    sclf.fit(train x onehotCoding, train y)
    print("Stacking Classifer : for the value of alpha: %f Log Loss: %0.3f" % (i, log_loss(cv_y, sc
lf.predict proba(cv x onehotCoding))))
    log error =log loss(cv y, sclf.predict proba(cv x onehotCoding))
    if best_alpha > log_error:
       best_alpha = log_error
4
Logistic Regression : Log Loss: 1.05
Support vector machines : Log Loss: 1.84
Naive Bayes : Log Loss: 1.22
Stacking Classifer: for the value of alpha: 0.000100 Log Loss: 2.178
Stacking Classifer: for the value of alpha: 0.001000 Log Loss: 2.031
Stacking Classifer : for the value of alpha: 0.010000 Log Loss: 1.493
Stacking Classifer: for the value of alpha: 0.100000 Log Loss: 1.158
Stacking Classifer : for the value of alpha: 1.000000 Log Loss: 1.335
Stacking Classifer: for the value of alpha: 10.000000 Log Loss: 1.698
```

4.7.2 testing the model with the best hyper parameters

```
In [195]:
```

```
lr = LogisticRegression(C=0.1)
sclf = StackingClassifier(classifiers=[sig_clf1, sig_clf2, sig_clf3], meta_classifier=lr, use_proba
s=True)
sclf.fit(train_x_onehotCoding, train_y)
```

```
log_error = log_loss(train_y, sclf.predict_proba(train_x_onehotCoding))
print("Log loss (train) on the stacking classifier :",log_error)

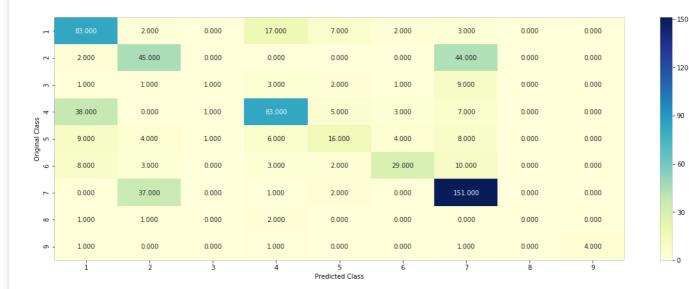
log_error = log_loss(cv_y, sclf.predict_proba(cv_x_onehotCoding))
print("Log loss (CV) on the stacking classifier :",log_error)

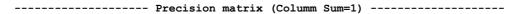
log_error = log_loss(test_y, sclf.predict_proba(test_x_onehotCoding))
print("Log loss (test) on the stacking classifier :",log_error)

print("Number of missclassified point :", np.count_nonzero((sclf.predict(test_x_onehotCoding)-test_y))/test_y.shape[0])
plot_confusion_matrix(test_y=test_y, predict_y=sclf.predict(test_x_onehotCoding))
```

Log loss (train) on the stacking classifier: 0.6336959417082211 Log loss (CV) on the stacking classifier: 1.1578735017349293 Log loss (test) on the stacking classifier: 1.1713063576119367

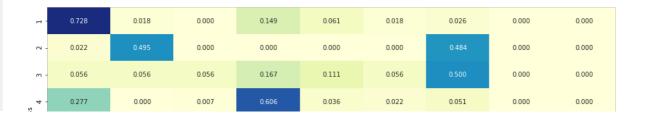
Number of missclassified point: 0.3804511278195489
------ Confusion matrix ------





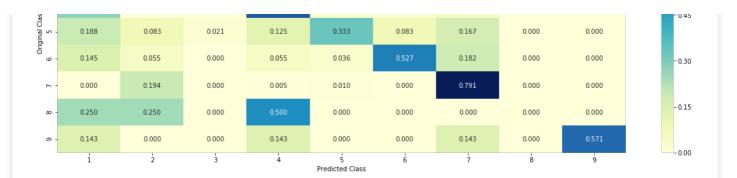


----- Recall matrix (Row sum=1) -----



0.75

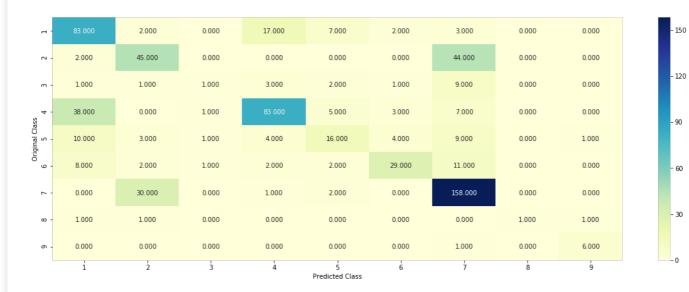
- 0.60



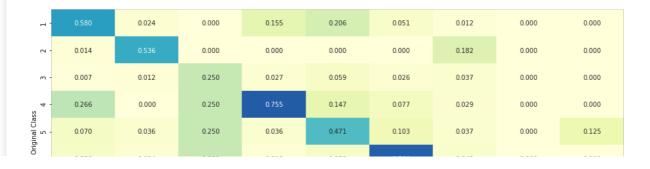
4.7.3 Maximum Voting classifier

In [196]:

```
#Refer:http://scikit-learn.org/stable/modules/generated/sklearn.ensemble.VotingClassifier.html
from sklearn.ensemble import VotingClassifier
vclf = VotingClassifier(estimators=[('lr', sig_clf1), ('svc', sig_clf2), ('rf', sig_clf3)], voting=
'soft')
vclf.fit(train_x_onehotCoding, train_y)
print("Log loss (train) on the VotingClassifier :", log_loss(train_y,
vclf.predict_proba(train_x_onehotCoding)))
print("Log loss (CV) on the VotingClassifier :", log_loss(cv_y,
vclf.predict_proba(cv_x_onehotCoding)))
print("Log loss (test) on the VotingClassifier :", log_loss(test_y,
vclf.predict_proba(test_x_onehotCoding)))
print("Number of missclassified point :", np.count_nonzero((vclf.predict(test_x_onehotCoding)-
test_y))/test_y.shape[0])
plot_confusion_matrix(test_y=test_y, predict_y=vclf.predict(test_x_onehotCoding))
```

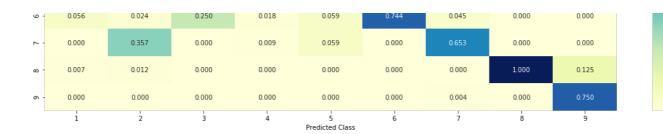


----- Precision matrix (Column Sum=1) -----



- 0.8

0.6



- 0.2

0.0

- 0.75

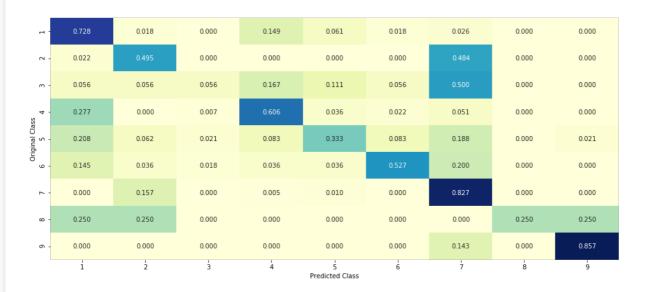
0.60

0.45

- 0.30

- 0.15

----- Recall matrix (Row sum=1)



5. Conclusion

5.1 Model Comarision

In [197]:

#https://www.kaggle.com/premvardhan/amazon-fine-food-reviews-analysis-using-knn
models = pd.DataFrame({'Model': ['Naive Bayes', "K-NN","Logistic Regression with Class Balancing",'
Logistic Regression without Class Balancing','Linear SVM','Random forest','Random forest(response
encoding)','Stacking classifier','Maximum voting classifier'], 'Log-Loss': [1.21,1.02,.99,1.02,1.0
3,1.15,1.3417,1.15,1.17], 'Percent of Misclassified points':[.370,.338,0.342,.336,.349,.379,.490,.3
80,.365], 'Hyperparameter': [1e-5,5,.0001,.0001,.0001,2000,1000,.1,0]}, columns = ["Model", "Log-L
oss", "Percent of Misclassified points", "Hyperparameter"])
models

Out[197]:

	Model	Log-Loss	Percent of Misclassified points	Hyperparameter
0	Naive Bayes	1.2100	0.370	0.00001
1	K-NN	1.0200	0.338	5.00000
2	Logistic Regression with Class Balancing	0.9900	0.342	0.00010
3	Logistic Regression without Class Balancing	1.0200	0.336	0.00010
4	Linear SVM	1.0300	0.349	0.00010
5	Random forest	1.1500	0.379	2000.00000
6	Random forest(response encoding)	1.3417	0.490	1000.00000
7	Stacking classifier	1.1500	0.380	0.10000
8	Maximum voting classifier	1.1700	0.365	0.00000

5.2 Observations

The log loss of logistic regression with class balancing is reduced to 0.99.

5.3 Steps Taken

To reduce the CV Log loss under 1.0 we have done TFidfvectorizer of Text features. Taken top 3000 Features.

Calculated 1 to 4 gram words.