

ARTIFICIAL INTELLIGENCE

LAB ASSIGNMENT - 6

The state space for this problem can be described as the set of ordered pairs of integers (x, y)

$x \rightarrow$ quantity of water in 4-gallon jug
 $x = 0, 1, 2, 3, 4$

$y \rightarrow$ quantity of water in 3-gallon jug
 $y = 0, 1, 2, 3$

Start state $\equiv (0, 0)$

Goal state $\equiv (2, 0)$

RULE

STATE

PROCESS

1

$(x, y | x < 4)$

$(4, y)$

Fill 4-gal jug

2

$(x, y | y < 3)$

$(x, 3)$

Fill 3-gal jug.

3

$(x, y | x > 0)$

$(0, y)$

Empty 4-gal jug.

4.

$(x, y | y > 0)$

$(x, 0)$

Empty 3-gal jug.

5 $(x, y \mid x+y \geq 4, y > 0)$ $(4, y - (4-x))$
 Pour water from 3-gal to 4-gal until its full.

6 $(x, y \mid x+y \geq 3, x > 0)$ $(x - (3-y), 3)$
 Pour water from 4-gal to 3-gal until its full.

7 $(x, y \mid x+y \leq 4, y > 0)$ $(x+y, 0)$
 Pour water (all) from 3-gal to 4-gal.

8 $(x, y \mid x+y \leq 3, x > 0)$ $(0, x+y)$
 Pour all water from 4-gal to 3-gal.

9 $(0, 2)$ $(2, 0)$
 Pour 2-gal water from 3-gal to 4-gal.

INITIALIZATION:

start state $\equiv (0, 0)$

Apply Rule 2:

$(x, y \mid y < 3) \rightarrow (x, 3)$
 (Fill 3-gal jug)

Now the state is $(x, 3)$

Iteration 1:

current state $\equiv (x, 3)$

Apply rule 7:

$$(x, y \mid x+y \leq 4 \rightarrow (x+y, 0) \\ y > 0)$$

Pour all water from
3-gal to 4-gal jug

Now the state is (3, 0).

Iteration 2:

current state $\equiv (3, 0)$

Apply Rule 2:

$$(x, y \mid y < 3) \rightarrow (3, 3)$$

Fill 3-gal jug.

Now the state is (3, 3).

Iteration 3:

current state $\equiv (3, 3)$

Apply Rule 5:

$$(x, y \mid x+y \geq 4 \rightarrow (4, y-(4-x)) \\ y > 0)$$

Pour water from
3-gal to 4-gal until
full.

Now the state is (4, 2).

Iteration 4 :

current state $\equiv (4, 2)$

Apply Rule 3:

$(x, y | x > 0) \rightarrow (0, y)$

empty 4-gal jug.

Now the state is $(0, 2)$.

Iteration 5:

current state $\equiv (0, 2)$

Apply Rule 9:

$(0, 2) \rightarrow (2, 0)$

Pour 2-gal water from
3 to 4-gal jug.

Now the state is $(2, 0)$.

GOAL ACHIEVED

Following is my approach for solving the above problem:

1. Relationship was always mutual, which means that if 1 has a friend 2, then 2 has a friend 1.

2. 1 has a friend 2, 2 has a friend 3, doesn't mean that 1 and 3 are friends. Thus, be careful to use the disjoint set.

3. ANALYSIS: seemingly, two-point diagram. But it's simpler than a binary chart.

Open two-tag array, record whether every one has friend in the first group, the second group.

sweep the person once:

1) If the first group doesn't have his friend: then put it in the first group and mark his friends in the first group with friends.

2) Otherwise:

i) If the 2nd group doesn't have his friend, then put it in the 2nd group and mark his friends in the 2nd group with friends.

2) Otherwise, the description in both groups has no friends.

you can put him casually in a group, also cannot handle it.

3. Analysis: Because there are M representatives of country A and N representatives of country B, and k pairs of representatives were chosen such that for each pair, 1 member is from delegation A & other member is from delegation B.

The problem can be represented bipartite graph G in which vertices are divided into 2 disjoint sets X & Y , such that M representatives of country A are set X and N representatives of country B are set Y .

And $N+M$ is the number of vertices G .

Based on graph theory, edge cover
no. + the number of edges in a
max. matching = $N+M$.

For the problem, the number of edges
in a max. matching is computed
first.

Then the edge cover is obtained:
 $N+M - \text{ans.}$

It is the minimum number of needed
telephone connections.