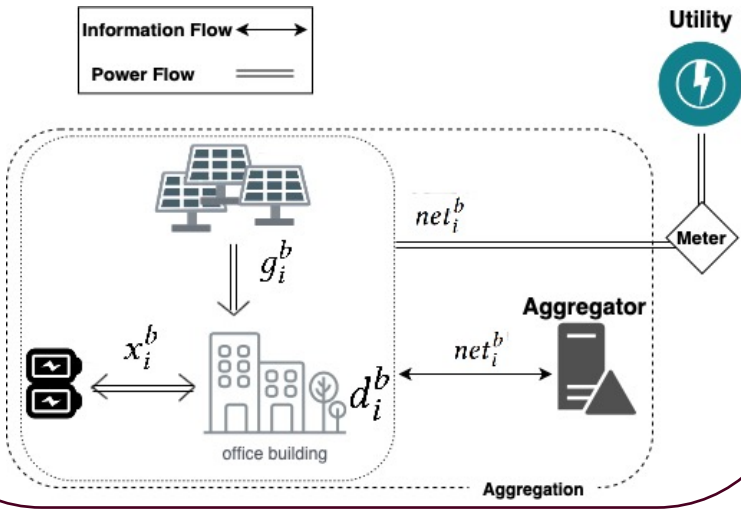


# Optimal Composition of Prosumer Aggregations

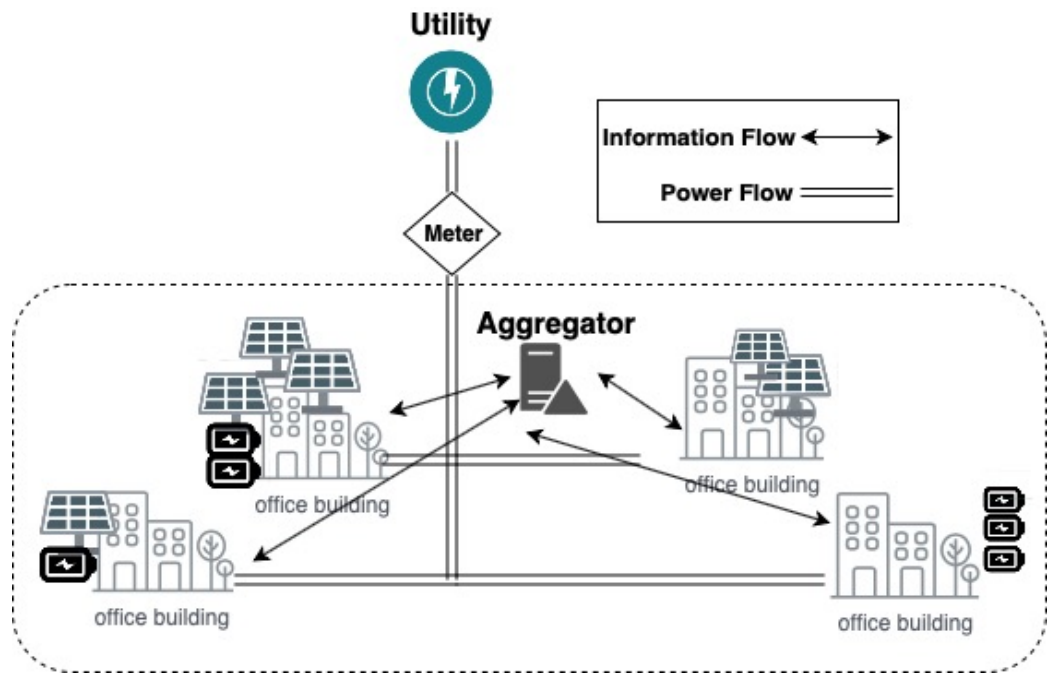
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A **prosumer** is an entity which can both **produce** and **consume** energy. Typically, prosumers are cost-sensitive and modify their net energy consumption in response to energy prices.



Aggregations can make use of **social net-metering schemes**, where the prosumer participants trade energy with each other first, and then present the net demand to the utility as a single entity.

Utilities sell energy at a higher price than the price at which they buy back surplus generation from retail customers. Aggregations can profit off this price differential.



**Research question:** *Which prosumers would form the optimal aggregation, i.e., an aggregation that benefits the participants the most?*

Model: The prosumer acts in a manner which minimizes its costs.

$$\begin{aligned} \min_{\mathbf{u}} J_P(\pi_b, \pi_s) &= \sum_{t=1}^T \left[ \pi_b^{(t)} z_+^{(t)} + \pi_s^{(t)} z_-^{(t)} + \pi_{\text{bat}} |u^{(t)}| \right] \\ &= \pi_b^T \mathbf{z}_+ + \pi_s^T \mathbf{z}_- + \pi_{\text{bat}} \mathbf{1}^T |\mathbf{u}| \\ \text{s.t.} \quad & 0 \leq L\mathbf{u} \leq c \end{aligned}$$

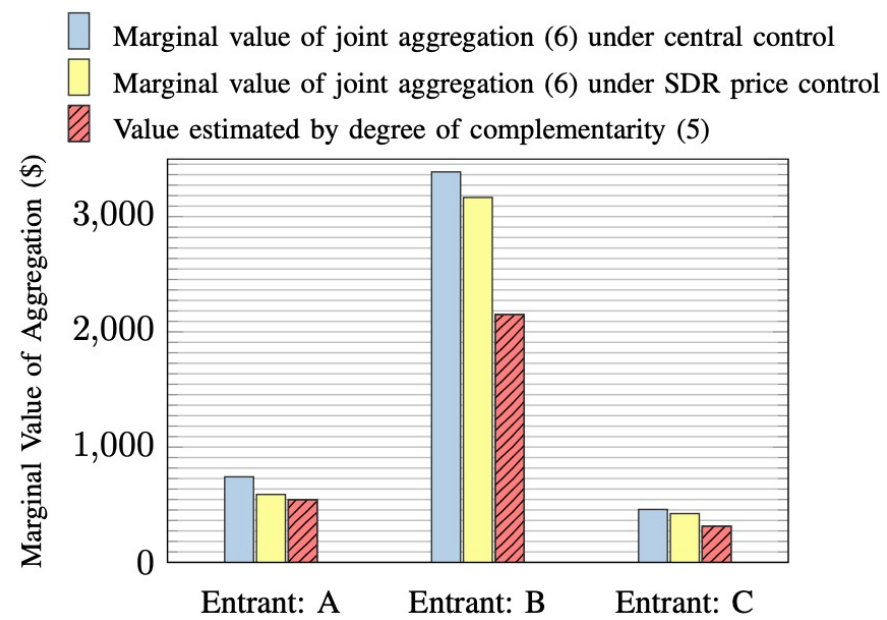
Model: Aggregations can be centrally controlled or use market mechanisms (like price) to reflect the trading balance. We focus on a centrally controlled aggregation, which also achieves the minimum possible social cost.

$$\begin{aligned} \min_{\mathbf{u}_i, i \in S} J_S &= \pi_b^T \left( \sum_{i \in S} \mathbf{z}_i \right)_+ + \pi_s^T \left( \sum_{i \in S} \mathbf{z}_i \right)_- + \pi_{\text{bat}} \mathbf{1}^T \left| \sum_{i \in S} \mathbf{u}_i \right| \\ \text{s.t.} \quad & 0 \leq L\mathbf{u}_i \leq c \mathbf{1} \forall i \in S \end{aligned}$$

**Result 1.** *In order to maximize social welfare, an aggregation should preferentially add a participant  $k$  that maximizes the degree of complementarity to the existing participants  $S$ , i.e. has an optimally complementary consumption curve. A lower bound on the degree of complementarity can be calculated as*

$$\frac{\pi_b^T - \pi_s^T}{2} \left( \left| \sum_{i \in S} \mathbf{z}_i^* \right| + |\mathbf{z}_k^*| - \left| \sum_{i \in S} \mathbf{z}_i^* + \mathbf{z}_k^* \right| \right) \quad (5)$$

where  $\mathbf{z}_i^*, \mathbf{z}_k^*$  are the optimal consumption curves for prosumers in the existing aggregation  $S$  and the new entrant  $k$  respectively.



This result can be used to analyze potential members for a prosumer aggregation and build an aggregation that achieves the highest social benefit. A profit seeking entity like a commercial DER aggregator can use this result to guarantee a minimum profit margin.

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