

# Assignment 4

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**Abstract**—This document solves a question based on triangle. similarly,

All the codes for the figure in this document can be found at

[https://github.com/utkarshsurwade/Matrix\\_Theory\\_EE5609/tree/master/Assignment4](https://github.com/utkarshsurwade/Matrix_Theory_EE5609/tree/master/Assignment4)

$$(\mathbf{A} - \mathbf{C}) + (\mathbf{C} - \mathbf{E}) = (\mathbf{A} - \mathbf{E}) \quad (2.0.4)$$

$$\therefore (\mathbf{C} - \mathbf{E}) = (\mathbf{A} - \mathbf{E}) - (\mathbf{A} - \mathbf{C}) \quad (2.0.5)$$

$$\therefore (\mathbf{C} - \mathbf{E}) = \frac{1}{2}(\mathbf{A} - \mathbf{B}) - (\mathbf{A} - \mathbf{C}) \quad (2.0.6)$$

Since  $AB = AC$   
 $\therefore (AB)^2 = (AC)^2$

## 1 PROBLEM

E and F are respectively the mid-points of equal sides AB and AC of  $\triangle ABC$ . Show that  $BF = CE$ .

## 2 SOLUTION

$$\therefore \|(\mathbf{A} - \mathbf{B})\|^2 = \|(\mathbf{A} - \mathbf{C})\|^2 \quad (2.0.7)$$

$$\begin{aligned} \|(\mathbf{A} - \mathbf{B})\|^2 + \frac{1}{4} \|(\mathbf{A} - \mathbf{C})\|^2 - (\mathbf{A} - \mathbf{C})^T (\mathbf{A} - \mathbf{B}) &= \\ \|(\mathbf{A} - \mathbf{C})\|^2 + \frac{1}{4} \|(\mathbf{A} - \mathbf{B})\|^2 - (\mathbf{A} - \mathbf{B})^T (\mathbf{A} - \mathbf{C}) & \end{aligned} \quad (2.0.8)$$

$$\left(\frac{1}{2}(\mathbf{A} - \mathbf{C}) - (\mathbf{A} - \mathbf{B})\right)^2 = \left(\frac{1}{2}(\mathbf{A} - \mathbf{B}) - (\mathbf{A} - \mathbf{C})\right)^2 \quad (2.0.9)$$

$$\|(\mathbf{B} - \mathbf{F})\|^2 = \|(\mathbf{C} - \mathbf{E})\|^2 \quad (2.0.10)$$

$$\therefore \|\mathbf{B} - \mathbf{F}\| = \|\mathbf{C} - \mathbf{E}\| \quad (2.0.11)$$

Hence, BF is equal to CE

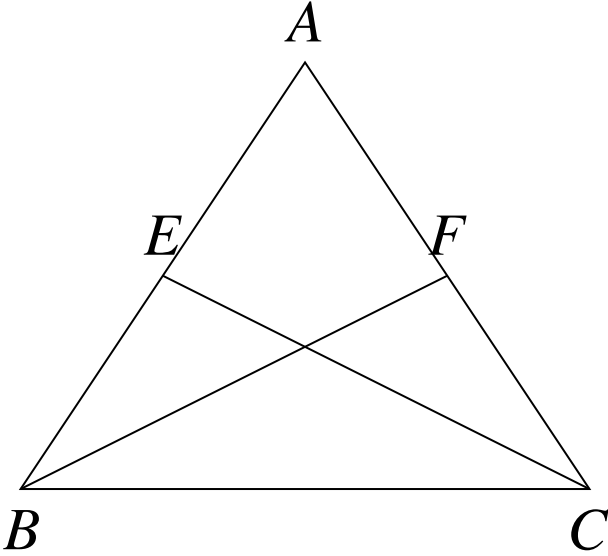


Fig. 1: Isosceles Triangle with mid-points E and F on equal sides

According to figure:

$$(\mathbf{A} - \mathbf{B}) + (\mathbf{B} - \mathbf{F}) = (\mathbf{A} - \mathbf{F}) \quad (2.0.1)$$

$$\therefore (\mathbf{B} - \mathbf{F}) = (\mathbf{A} - \mathbf{F}) - (\mathbf{A} - \mathbf{B}) \quad (2.0.2)$$

$$\therefore (\mathbf{B} - \mathbf{F}) = \frac{1}{2}(\mathbf{A} - \mathbf{C}) - (\mathbf{A} - \mathbf{B}) \quad (2.0.3)$$