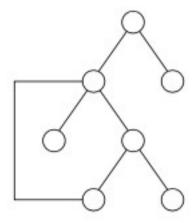
Homework exercises should be done individually (You should write the solution by yourself). Solutions must be prepared in python programming language and submitted electronically before 11.59 pm on Sunday, January 3. No credit will be given to solutions obtained verbatim from the Internet or other sources. To get full credit for each question, you need to provide a brief explanation of your codes and the efficiency analysis with comments.

**3.** Consider a loop tree which is an undirected wighted graph formed by taking a binary tree and adding an edge from exactly one of the leaves to another node in the tree as follows:



Let n be the number of vertices in a loop tree. How long does it take Prim's or Kruskal's algorithms to find the minimum spanning tree in terms of n?

Devise a more efficient algorithm that takes an nxn adjacency weighted matrix as input, and finds the minimum spanning tree of a loop tree.