



LET'S DO A FUN PROBLEM!

Suppose you are given a list L of length n as input.

Given two indices l, r how do you find the sum of everything in between?

In other words, how do you find L[l] + L[l+1] + ... + L[r]?









LET'S MAKE IT HARDER

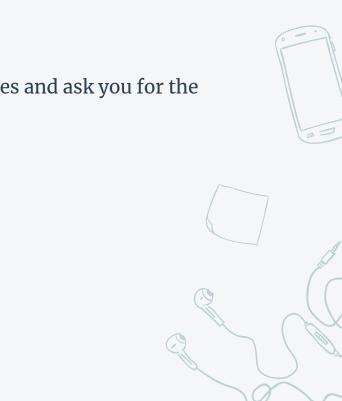
Suppose you are given a list L of length n as input.

Then you are given m queries that each give two indices and ask you for the sum of everything in between.

How can we answer all queries?









Prefix Sum Array

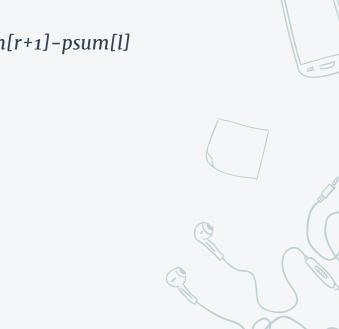
Idea: for each index i, keep track of L[o] + L[1] + ... + L[i-1] in another list (call it psum).

Now the sum of everything between l, r is simply psum[r+1]-psum[l]

(Be careful with defining psum[o] & psum[n]!)









That's pretty efficient...

In competitive programming we care about:

- Time constraint (given in terms of seconds)
- Memory constraint (given in terms of megabytes)



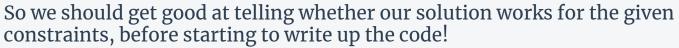
- 1 <= n <= 10∧5
- 1 <= m <= 1000
- $-10^9 <= L[i] <= 10^9$
- -0 <= 1, r < n



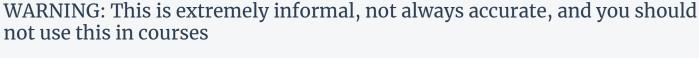




TIME COMPLEXITY



Rule of thumb: Assume your program can do \sim 3 * 10^8 operations in a second











- We don't care about the *exact* number of operations (an upper bound, shown using big O notation, is good enough)
- 2) We don't care about constants that much.
 - a) Doing 2 * n operations is about as fast as doing n or n/2 operations for really big values of n
 - Doing a few calculations here and there (outside loops) will not affect time complexity







WHAT IS THE TIME COMPLEXITY OF THE PREFIX ARRAY SOLUTION?

We can fill out psum using a single for loop over the list! aka O(n) operations.

```
psum[0] = 0
for i from 1 to n
    psum[i] = psum[i-1] + L[i]
(This is called pseudo-code. It's not always convenient to write out whole details of your program while adhering to syntax.)
```

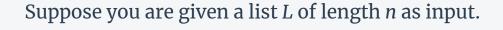
Then each query can be answered with O(1) since it's just calculating the difference of two *psums*.

So in total, O(n + n + m) to read the input, calculate psum, and read/answer queries, which is equal to O(n + m).





A HARDER VERSION?



Then you are given *m* queries. Each query can be one of these two types:

- 1) Gives two indices and asks you for the sum of everything in between
- Tells you to change the value of L[i] for some i

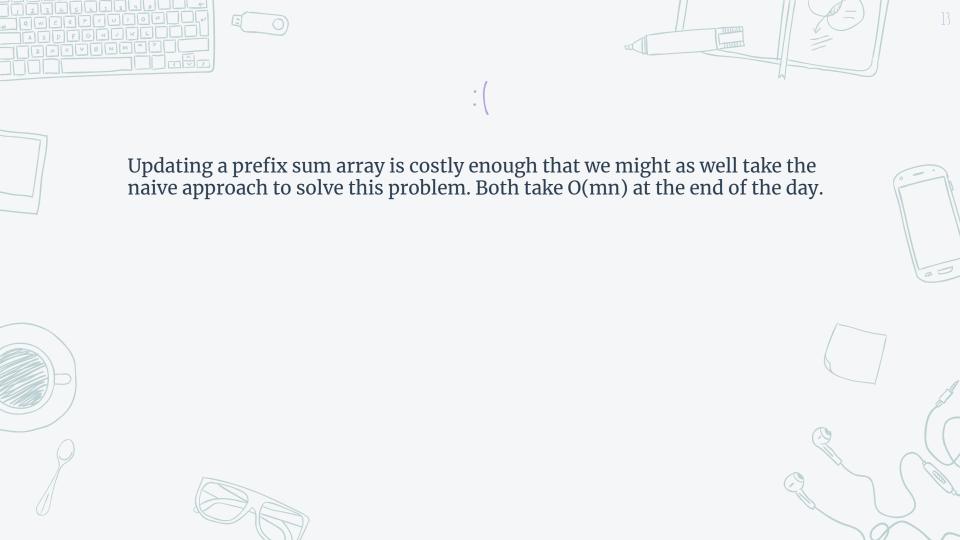


Why does our previous method fail?











ENTER DECOMPOSITION

Suppose you decomposed your array in the following way:

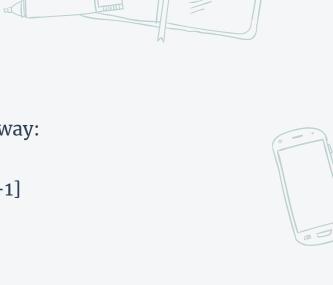
L[0],...,L[k-1], L[k],...,L[2k-1], ...,L[tk],...,L[n-1]

Creating buckets of size k.

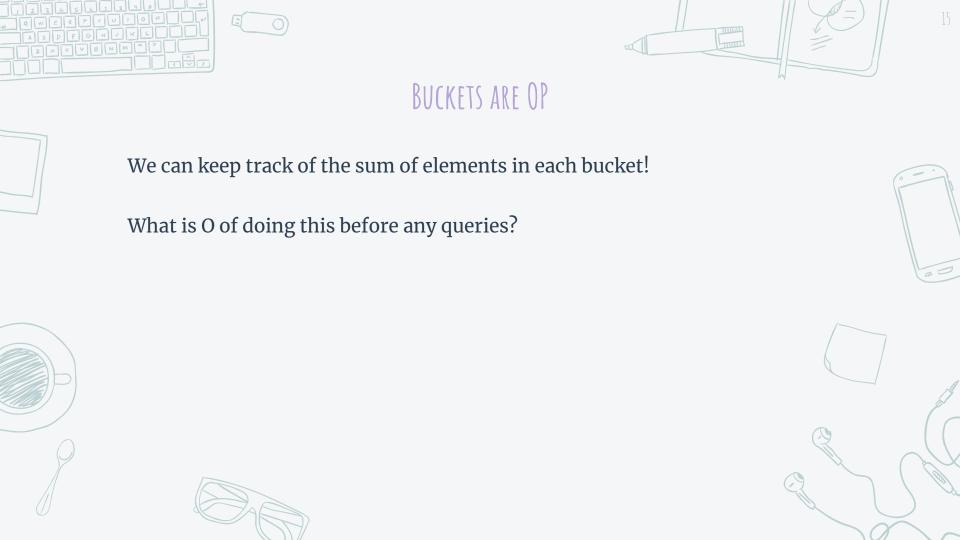
How many buckets in total?
What is the size of the last b

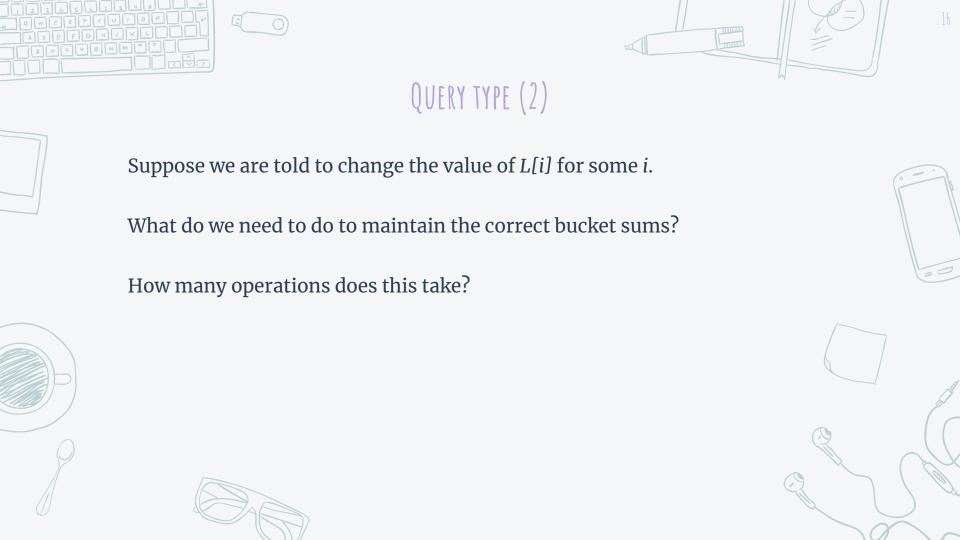
What is the size of the last bucket?

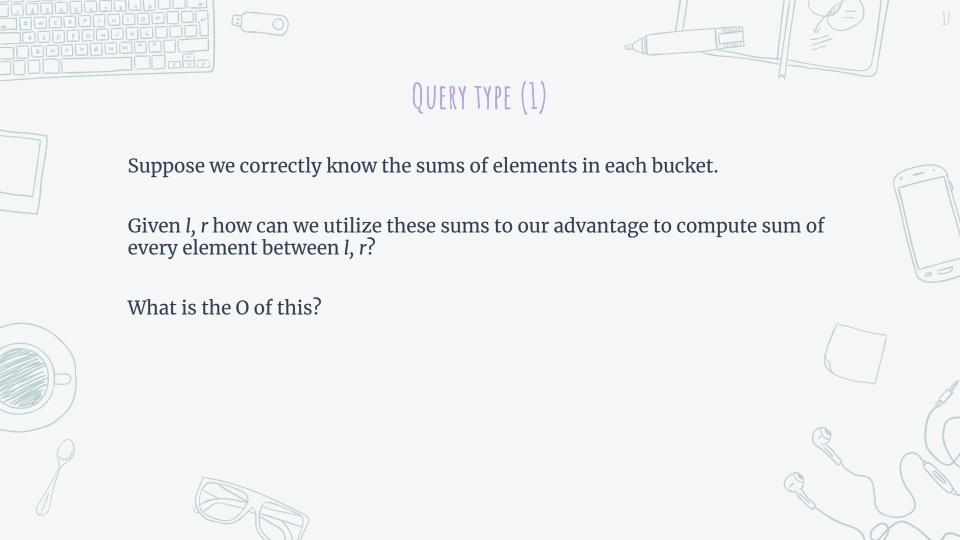


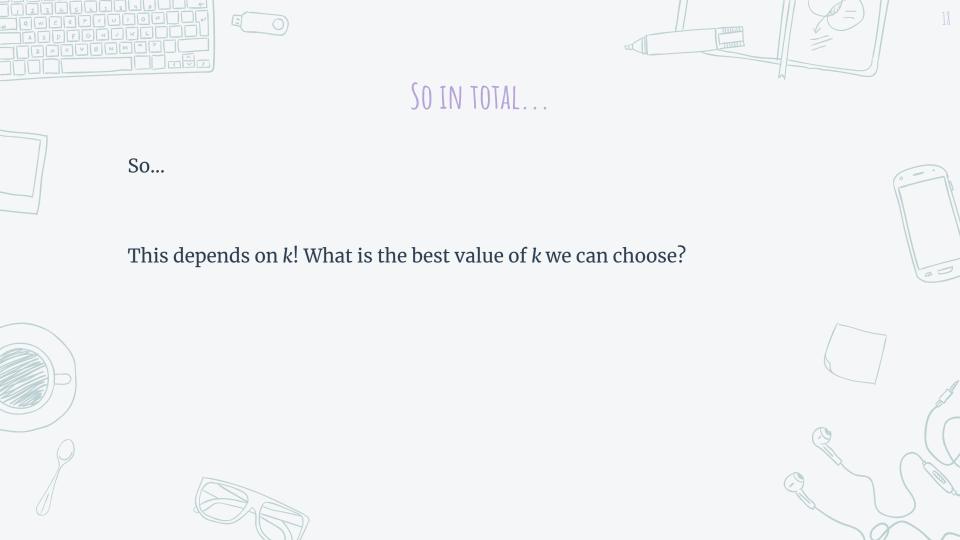


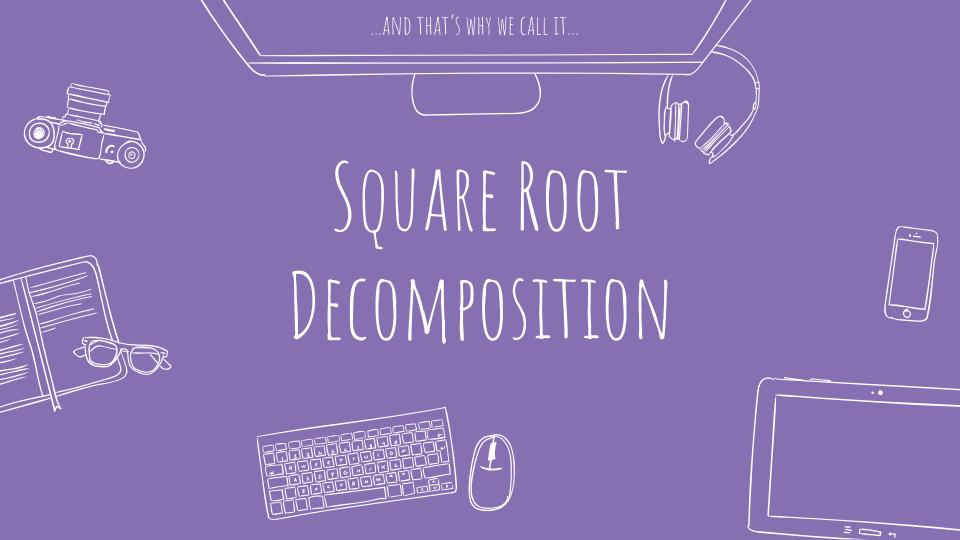


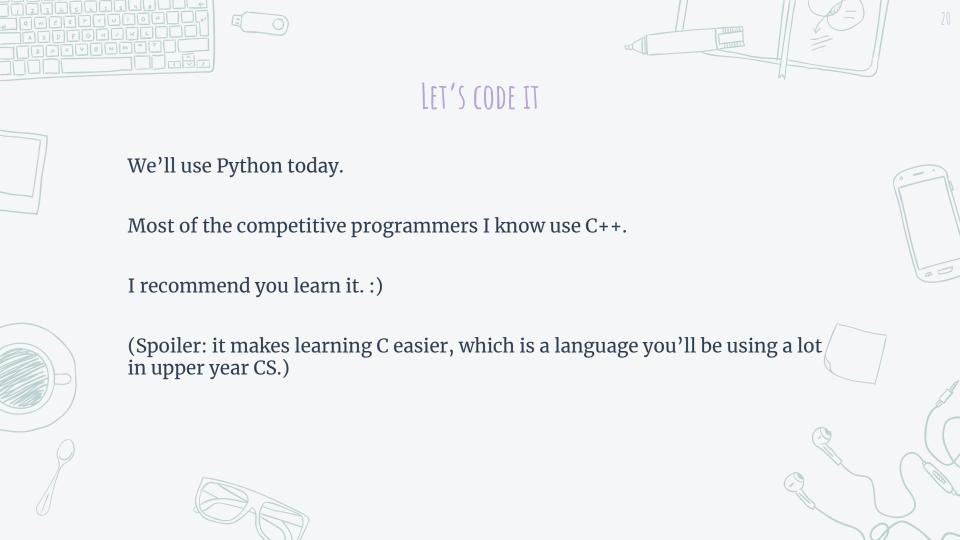


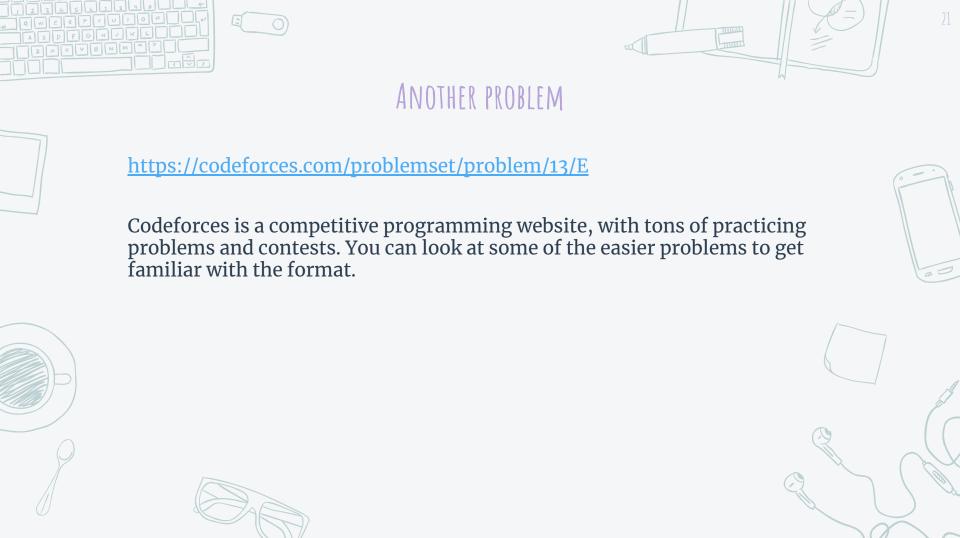














OTHER RESOURCES

Today's material: https://github.com/utmmcss/competitive-programming

Competitive programming handbook: https://cses.fi/book/book.pdf

GeeksforGeeks: https://www.geeksforgeeks.org/

MCSS Discord: https://discord.gg/wfJUZyXjfM

Feel free to reach out to me by email/discord if you have any questions about today's workshop!