Image Captioning with LSTMs

In the previous exercise you implemented a vanilla RNN and applied it to image captioning. In this notebook you will implement the LSTM update rule and use it for image captioning.

```
In [1]: # As usual, a bit of setup
        import time, os, json
        import numpy as np
        import matplotlib.pyplot as plt
        from cs682.gradient_check import eval_numerical_gradient, eval_numerical_gradi
        ent_array
        from cs682.rnn layers import *
        from cs682.captioning solver import CaptioningSolver
        from cs682.classifiers.rnn import CaptioningRNN
        from cs682.coco_utils import load_coco_data, sample_coco_minibatch, decode_cap
        tions
        from cs682.image_utils import image_from_url
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipyt
        %load_ext autoreload
        %autoreload 2
        def rel error(x, y):
            """ returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

Load MS-COCO data

As in the previous notebook, we will use the Microsoft COCO dataset for captioning.

```
In [2]: # Load COCO data from disk; this returns a dictionary
    # We'll work with dimensionality-reduced features for this notebook, but feel
    # free to experiment with the original features by changing the flag below.
    data = load_coco_data(pca_features=True)

# Print out all the keys and values from the data dictionary
    for k, v in data.items():
        if type(v) == np.ndarray:
            print(k, type(v), v.shape, v.dtype)
        else:
            print(k, type(v), len(v))
```

```
train_captions <class 'numpy.ndarray'> (400135, 17) int32
train_image_idxs <class 'numpy.ndarray'> (400135,) int32
val_captions <class 'numpy.ndarray'> (195954, 17) int32
val_image_idxs <class 'numpy.ndarray'> (195954,) int32
train_features <class 'numpy.ndarray'> (82783, 512) float32
val_features <class 'numpy.ndarray'> (40504, 512) float32
idx_to_word <class 'list'> 1004
word_to_idx <class 'dict'> 1004
train_urls <class 'numpy.ndarray'> (82783,) <U63
val_urls <class 'numpy.ndarray'> (40504,) <U63</pre>
```

LSTM

If you read recent papers, you'll see that many people use a variant on the vanilla RNN called Long-Short Term Memory (LSTM) RNNs. Vanilla RNNs can be tough to train on long sequences due to vanishing and exploding gradients caused by repeated matrix multiplication. LSTMs solve this problem by replacing the simple update rule of the vanilla RNN with a gating mechanism as follows.

Similar to the vanilla RNN, at each timestep we receive an input $x_t \in \mathbb{R}^D$ and the previous hidden state $h_{t-1} \in \mathbb{R}^H$; the LSTM also maintains an H-dimensional $\mathit{cell state}$, so we also receive the previous cell state $c_{t-1} \in \mathbb{R}^H$. The learnable parameters of the LSTM are an $\mathit{input-to-hidden}$ matrix $W_x \in \mathbb{R}^{4H \times D}$, a $\mathit{hidden-to-hidden}$ matrix $W_h \in \mathbb{R}^{4H \times H}$ and a $\mathit{bias vector } b \in \mathbb{R}^{4H}$.

At each timestep we first compute an activation vector $a \in \mathbb{R}^{4H}$ as $a = W_x x_t + W_h h_{t-1} + b$. We then divide this into four vectors $a_i, a_f, a_o, a_g \in \mathbb{R}^H$ where a_i consists of the first H elements of a, a_f is the next H elements of a, etc. We then compute the input gate $g \in \mathbb{R}^H$, forget gate $f \in \mathbb{R}^H$, output gate $o \in \mathbb{R}^H$ and block input $g \in \mathbb{R}^H$ as

$$i = \sigma(a_i) \qquad f = \sigma(a_f) \qquad o = \sigma(a_o) \qquad g = anh(a_g)$$

where σ is the sigmoid function and \tanh is the hyperbolic tangent, both applied elementwise.

Finally we compute the next cell state c_t and next hidden state h_t as

$$c_t = f \odot c_{t-1} + i \odot g$$
 $h_t = o \odot \tanh(c_t)$

where \odot is the elementwise product of vectors.

In the rest of the notebook we will implement the LSTM update rule and apply it to the image captioning task.

In the code, we assume that data is stored in batches so that $X_t \in \mathbb{R}^{N \times D}$, and will work with transposed versions of the parameters: $W_x \in \mathbb{R}^{D \times 4H}$, $W_h \in \mathbb{R}^{H \times 4H}$ so that activations $A \in \mathbb{R}^{N \times 4H}$ can be computed efficiently as $A = X_t W_x + H_{t-1} W_h$

LSTM: step forward

Implement the forward pass for a single timestep of an LSTM in the <code>lstm_step_forward</code> function in the file <code>cs682/rnn_layers.py</code>. This should be similar to the <code>rnn_step_forward</code> function that you implemented above, but using the LSTM update rule instead.

Once you are done, run the following to perform a simple test of your implementation. You should see errors on the order of e-8 or less.

```
In [3]: N, D, H = 3, 4, 5
        x = np.linspace(-0.4, 1.2, num=N*D).reshape(N, D)
        prev h = np.linspace(-0.3, 0.7, num=N*H).reshape(N, H)
        prev c = np.linspace(-0.4, 0.9, num=N*H).reshape(N, H)
        Wx = np.linspace(-2.1, 1.3, num=4*D*H).reshape(D, 4*H)
        Wh = np.linspace(-0.7, 2.2, num=4*H*H).reshape(H, 4*H)
        b = np.linspace(0.3, 0.7, num=4*H)
        next_h, next_c, cache = lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)
        expected next h = np.asarray([
            [ 0.24635157, 0.28610883, 0.32240467, 0.35525807, 0.38474904],
            [ 0.49223563, 0.55611431, 0.61507696, 0.66844003, 0.7159181 ],
            [ 0.56735664, 0.66310127, 0.74419266, 0.80889665, 0.858299 ]])
        expected next c = np.asarray([
            [ 0.32986176, 0.39145139, 0.451556, 0.51014116, 0.56717407],
            [0.66382255, 0.76674007, 0.87195994, 0.97902709, 1.08751345],
            [ 0.74192008, 0.90592151, 1.07717006, 1.25120233, 1.42395676]])
        print('next_h error: ', rel_error(expected_next_h, next_h))
        print('next_c error: ', rel_error(expected_next_c, next_c))
```

next_h error: 5.7054131185818695e-09 next_c error: 5.8143123088804145e-09

LSTM: step backward

Implement the backward pass for a single LSTM timestep in the function <code>lstm_step_backward</code> in the file <code>cs682/rnn_layers.py</code>. Once you are done, run the following to perform numeric gradient checking on your implementation. You should see errors on the order of <code>e-7</code> or less.

```
In [4]: | np.random.seed(231)
        N, D, H = 4, 5, 6
        x = np.random.randn(N, D)
        prev h = np.random.randn(N, H)
        prev_c = np.random.randn(N, H)
        Wx = np.random.randn(D, 4 * H)
        Wh = np.random.randn(H, 4 * H)
        b = np.random.randn(4 * H)
        next_h, next_c, cache = lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)
        dnext_h = np.random.randn(*next_h.shape)
        dnext_c = np.random.randn(*next_c.shape)
        fx_h = lambda x: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
        fh_h = lambda h: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
        fc_h = lambda c: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
        fWx_h = lambda Wx: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
        fWh h = lambda Wh: 1stm step forward(x, prev h, prev c, Wx, Wh, b)[0]
        fb h = lambda b: lstm step forward(x, prev h, prev c, Wx, Wh, b)[0]
        fx c = lambda x: lstm step forward(x, prev h, prev c, Wx, Wh, b)[1]
        fh_c = lambda h: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
        fc_c = lambda c: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
        fWx_c = lambda Wx: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
        fWh c = lambda Wh: lstm step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
        fb_c = lambda b: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
        num_grad = eval_numerical_gradient_array
        dx num = num grad(fx h, x, dnext h) + num grad(fx c, x, dnext c)
        dh num = num grad(fh h, prev h, dnext h) + num grad(fh c, prev h, dnext c)
        dc num = num grad(fc h, prev c, dnext h) + num grad(fc c, prev c, dnext c)
        dWx num = num grad(fWx h, Wx, dnext h) + num grad(fWx c, Wx, dnext c)
        dWh num = num grad(fWh h, Wh, dnext h) + num grad(fWh c, Wh, dnext c)
        db_num = num_grad(fb_h, b, dnext_h) + num_grad(fb_c, b, dnext_c)
        dx, dh, dc, dWx, dWh, db = 1stm step backward(dnext h, dnext c, cache)
        print('dx error: ', rel_error(dx_num, dx))
        print('dh error: ', rel_error(dh_num, dh))
print('dc error: ', rel_error(dc_num, dc))
        print('dWx error: ', rel_error(dWx_num, dWx))
        print('dWh error: ', rel_error(dWh_num, dWh))
        print('db error: ', rel_error(db_num, db))
```

```
dx error: 6.141176401368906e-10
dh error: 3.3953235055372503e-10
dc error: 1.5221723979041107e-10
dWx error: 1.6933643922734908e-09
dWh error: 2.5561308517943814e-08
db error: 1.7349247160222088e-10
```

LSTM: forward

In the function <code>lstm_forward</code> in the file <code>cs682/rnn_layers.py</code>, implement the <code>lstm_forward</code> function to run an LSTM forward on an entire timeseries of data.

When you are done, run the following to check your implementation. You should see an error on the order of e-7 or less.

```
In [5]: N, D, H, T = 2, 5, 4, 3
    x = np.linspace(-0.4, 0.6, num=N*T*D).reshape(N, T, D)
    h0 = np.linspace(-0.4, 0.8, num=N*H).reshape(N, H)
    Wx = np.linspace(-0.2, 0.9, num=4*D*H).reshape(D, 4 * H)
    Wh = np.linspace(-0.3, 0.6, num=4*H*H).reshape(H, 4 * H)
    b = np.linspace(0.2, 0.7, num=4*H)

    h, cache = lstm_forward(x, h0, Wx, Wh, b)

expected_h = np.asarray([
    [[ 0.01764008,  0.01823233,  0.01882671,  0.0194232 ],
    [ 0.11287491,  0.12146228,  0.13018446,  0.13902939],
    [ 0.31358768,  0.33338627,  0.35304453,  0.37250975]],
    [[ 0.45767879,  0.4761092,   0.4936887,   0.51041945],
    [ 0.6704845,   0.69350089,   0.71486014,   0.7346449 ],
    [ 0.81733511,   0.83677871,   0.85403753,   0.86935314]]])

print('h error: ', rel_error(expected_h, h))
```

h error: 8.610537452106624e-08

LSTM: backward

Implement the backward pass for an LSTM over an entire timeseries of data in the function <code>lstm_backward</code> in the file <code>cs682/rnn_layers.py</code>. When you are done, run the following to perform numeric gradient checking on your implementation. You should see errors on the order of <code>e-8</code> or less. (For dWh , it's fine if your error is on the order of <code>e-6</code> or less).

```
In [6]: | from cs682.rnn layers import lstm forward, lstm backward
        np.random.seed(231)
        N, D, T, H = 2, 3, 10, 6
        x = np.random.randn(N, T, D)
        h0 = np.random.randn(N, H)
        Wx = np.random.randn(D, 4 * H)
        Wh = np.random.randn(H, 4 * H)
        b = np.random.randn(4 * H)
        out, cache = lstm_forward(x, h0, Wx, Wh, b)
        dout = np.random.randn(*out.shape)
        dx, dh0, dWx, dWh, db = lstm_backward(dout, cache)
        fx = lambda x: lstm_forward(x, h0, Wx, Wh, b)[0]
        fh0 = lambda h0: lstm_forward(x, h0, Wx, Wh, b)[0]
        fWx = lambda Wx: lstm forward(x, h0, Wx, Wh, b)[0]
        fWh = lambda Wh: lstm forward(x, h0, Wx, Wh, b)[0]
        fb = lambda b: lstm_forward(x, h0, Wx, Wh, b)[0]
        dx_num = eval_numerical_gradient_array(fx, x, dout)
        dh0_num = eval_numerical_gradient_array(fh0, h0, dout)
        dWx_num = eval_numerical_gradient_array(fWx, Wx, dout)
        dWh num = eval numerical gradient array(fWh, Wh, dout)
        db_num = eval_numerical_gradient_array(fb, b, dout)
        print('dx error: ', rel_error(dx_num, dx))
        print('dh0 error: ', rel_error(dh0_num, dh0))
        print('dWx error: ', rel_error(dWx_num, dWx))
        print('dWh error: ', rel_error(dWh_num, dWh))
        print('db error: ', rel error(db num, db))
```

dx error: 4.82504980953228e-09 dh0 error: 7.500898788574784e-09 dWx error: 1.751994908422919e-09 dWh error: 1.085376964509146e-06 db error: 7.427550110055494e-10

INLINE QUESTION

Recall that in an LSTM the input gate i, forget gate f, and output gate o are all outputs of a sigmoid function. Why don't we use the ReLU activation function instead of sigmoid to compute these values? Explain.

ANSWER:

Using the sigmoid funtion for the gates means that each entry of each of the gates is allowed to vary smoothly between 0 and 1. On the other hand, using the ReLU function as gates means that each of the entries of the gates are restricted to either 0 or 1, and nothing in between. Therefore, using the sigmoid allows for a much wider range of gate values as compared to the ReLU.

The advantage of this increased flexibility is that our model can learn more complex models of the input data, and hence, make better test results.

LSTM captioning model

Now that you have implemented an LSTM, update the implementation of the loss method of the CaptioningRNN class in the file cs682/classifiers/rnn.py to handle the case where self.cell_type is lstm. This should require adding less than 10 lines of code.

Once you have done so, run the following to check your implementation. You should see a difference on the order of e-10 or less.

```
In [7]: N, D, W, H = 10, 20, 30, 40
        word_to_idx = {'<NULL>': 0, 'cat': 2, 'dog': 3}
        V = len(word_to_idx)
        T = 13
        model = CaptioningRNN(word_to_idx,
                   input dim=D,
                  wordvec dim=W,
                  hidden dim=H,
                   cell_type='lstm',
                  dtype=np.float64)
        # Set all model parameters to fixed values
        for k, v in model.params.items():
          model.params[k] = np.linspace(-1.4, 1.3, num=v.size).reshape(*v.shape)
        features = np.linspace(-0.5, 1.7, num=N*D).reshape(N, D)
        captions = (np.arange(N * T) % V).reshape(N, T)
        loss, grads = model.loss(features, captions)
        expected_loss = 9.82445935443
        print('loss: ', loss)
        print('expected loss: ', expected_loss)
        print('difference: ', abs(loss - expected_loss))
```

loss: 9.82445935443226 expected loss: 9.82445935443 difference: 2.261302256556519e-12

Overfit LSTM captioning model

Run the following to overfit an LSTM captioning model on the same small dataset as we used for the RNN previously. You should see a final loss less than 0.5.

```
In [8]: np.random.seed(231)
        small_data = load_coco_data(max_train=50)
        small_lstm_model = CaptioningRNN(
                   cell_type='lstm',
                   word_to_idx=data['word_to_idx'],
                   input_dim=data['train_features'].shape[1],
                   hidden_dim=512,
                   wordvec_dim=256,
                   dtype=np.float32,
        small_lstm_solver = CaptioningSolver(small_lstm_model, small_data,
                    update_rule='adam',
                    num_epochs=50,
                    batch_size=25,
                    optim_config={
                      'learning_rate': 5e-3,
                    },
                    1r decay=0.995,
                    verbose=True, print_every=10,
        small_lstm_solver.train()
        # Plot the training losses
        plt.plot(small_lstm_solver.loss_history)
        plt.xlabel('Iteration')
        plt.ylabel('Loss')
        plt.title('Training loss history')
        plt.show()
```

11/23/2019 LSTM_Captioning

```
(Iteration 1 / 100) loss: 79.551150

(Iteration 11 / 100) loss: 43.829099

(Iteration 21 / 100) loss: 30.062610

(Iteration 31 / 100) loss: 14.020070

(Iteration 41 / 100) loss: 6.005386

(Iteration 51 / 100) loss: 1.849711

(Iteration 61 / 100) loss: 0.642087

(Iteration 71 / 100) loss: 0.282384

(Iteration 81 / 100) loss: 0.236188

(Iteration 91 / 100) loss: 0.130116
```



LSTM test-time sampling

Modify the sample method of the CaptioningRNN class to handle the case where self.cell_type is lstm . This should take fewer than 10 lines of code.

When you are done run the following to sample from your overfit LSTM model on some training and validation set samples. As with the RNN, training results should be very good, and validation results probably won't make a lot of sense (because we're overfitting).

```
In [9]: for split in ['train', 'val']:
    minibatch = sample_coco_minibatch(small_data, split=split, batch_size=2)
    gt_captions, features, urls = minibatch
    gt_captions = decode_captions(gt_captions, data['idx_to_word'])

sample_captions = small_lstm_model.sample(features)
    sample_captions = decode_captions(sample_captions, data['idx_to_word'])

for gt_caption, sample_caption, url in zip(gt_captions, sample_captions, urls):
    plt.imshow(image_from_url(url))
    plt.title('%s\n%s\nGT:%s' % (split, sample_caption, gt_caption))
    plt.axis('off')
    plt.show()
```

11/23/2019 LSTM_Captioning

train
a man standing on the side of a road with bags of luggage <END>
GT:<START> a man standing on the side of a road with bags of luggage <END>



train
a man <UNK> with a bright colorful kite <END>
GT:<START> a man <UNK> with a bright colorful kite <END>



val
a person <UNK> with a <UNK> of a <UNK> <END>
GT:<START> a sign that is on the front of a train station <END>



11/23/2019 LSTM_Captioning

val a cat is <UNK> and a <UNK> <END> GT:<START> a car is parked on a street at night <END>

