

**Project Report**  
**ON**  
**“ORDERED DITHERING”**

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**2016-2017**

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# Chapter 1

## Introduction

### 1.1 Overview

Halftoning or analog halftoning is a process that simulates shades of gray by varying the size of tiny black dots arranged in a regular pattern. This technique is used in printers, as well as the publishing industry. If you inspect a photograph in a newspaper, you will notice that the picture is composed of black dots even though it appears to be composed of grays. This is possible because of the spatial integration performed by our eyes. Our eyes blend fine details and record the overall intensity<sup>1</sup>.

### 1.2 Digital Halftoning

Digital halftoning is similar to halftoning in which an image is decomposed into a grid of halftone cells. Elements (or dots that halftoning uses in simulates shades of grays) of an image are simulated by filling the appropriate halftone cells. The more number of black dots in a halftone cell, the darker the cell appears. For example, in Figure 4, a tiny dot located at the center is simulated in digital halftoning by filling the center halftone cell; likewise, a medium size dot located at the top-left corner is simulated by filling the four cells at the top-left corner. The large dot covering most of the area in the third image is simulated by filling all halftone cells.

### 1.3 Methods

Many image rendering technologies only have binary output. For example, printers can either fire a dot or not. Halftoning is a method for creating the illusion of continuous tone output with a binary device. Effective digital halftoning can substantially improve the quality of rendered images at minimal cost<sup>2</sup>.

### 1.4 Types

- Dithering
- Patterning
- Error Diffusion

#### 1.4.1 Dithering

Dithering is a color reproduction technique in which dots or pixels are arranged in such a way that allows us to perceive more colors than are actually used. This method of "creating" a large color palette with a limited set of colors is often used in computer images, television and the printing industry. The graphic illustrations below show how a full color image can be approximated by

using only a few colors. As magnification is increased, see how each color seen is broken down to a combination of the primary colors used in the dither pattern.

The technique used for generating digital halftoning images is dithering. Unlike patterning, dithering creates an output image with the same number of dots as the number of pixels in the source image. Dithering can be thought of as thresholding the source image with a dither matrix. The matrix is laid repeatedly over the source image. Wherever the pixel value of the image is greater than the value in the matrix, a dot on the output image is filled. A well-known problem of dithering is that it produces artifacts of patterns introduced by fixed thresholding matrices<sup>3</sup>.

## **1.5 Ordered Dithering**

Ordered dithering and cluster dithering are the fastest methods. They are effective for reducing the number of colors to 256 colors or less. Ordered dithering is the default dithering method when painting to a display device that is 256 colors or less.

These methods take advantage of the fact that the colors in most palettes are ordered so that similar shades are next to each other in the palette. Pixels used in dithering are taken from these adjacent colors to achieve the nearest shade. They place pixels from shades near to the original color to achieve a smoothing effect. Ordered dithering avoids blotches of color by adding to or subtracting from the nearest-color value of each pixel to ensure that adjacent pixels do not have exactly the same color. However, If the colors in the palette are not ordered, the results may be poor<sup>4</sup>.

# Chapter 2

## Project Description

### 2.1 MATLAB Implementation

Step 1:

The original image is fed into MATLAB to be processed upon.

Step 2:

The original image is cut into smaller blocks of 8x8 pixels.

Step 3:

The average value of graylevel of each block of 8x8 pixels is calculated.

Step 4:

A new block that holds number of pixels representing the average value of original block. This is the first part of the new image.

8x8 pixel block is represented by one value of graylevel.

Step 5:

Placed the dots according to designed dither matrix.

Step 6:

The desired result is obtained from this Ordered Dithering Technique.

newline Note: Some information of the original image is lost as the average value of 8x8 pixel blocks is considered.

# Chapter 3

## Implementation

The following is the code implementing the Ordered Dithering Algorithm in MATLAB:

```

1 %#####
2 %#####
3 %##          Digital Image Processing HW1          ##
4 %##          Implementing the Find_S algorithm      ##
5 %##          Matlab R2016a was used                ##
6 %##          v9.0.0.341360                         ##
7 %#####
8 %#####
9
10
11 % [filename,pathname] = uigetfile({'*.png', '*.bmp', '*.jpg'; '*.*'}, 'File
    Selector');
12 [FileName, PathName, FilterIndex] = uigetfile('*.jpg', 'Select the Image file');
13
14 %if the user did not select a file set the file to be "1.jpg" in the folder
15 %"Images"
16 if isequal(FileName, 0)
17     PathName = 'Images\';
18     FileName = '1.jpg';
19 end
20
21 %dimension of the area that we are going to work with
22 n = 8;
23 %which Ordered Dithering matrix we want to use
24 %Order dithering matrices are stored in the properties of the ImgManager
25 %class
26 OrderedDitherMatrixNum = 2;
27 %load the original image to compare if we want to show them side by side,
28 %the original and the dithered
29 OriginalImg = imread(strcat(PathName, FileName));
30 %instantiate a new instance of the ImgManager class
31 ImgM = ImgManager();
32 %the full path of the image is the combination of both the path and the
33 %name of the image file
34 path = strcat(PathName, FileName);
35 %again load the image but this time through the ImgManager class which will
36 %convert it to gray scale image after it loads it, so this copy of the
37 %image is what we are going to use for processing
38 img = ImgM.load(path);
39 %call the function that dither the image
40 DitheredImg = ImgM.Dither(n, img, (n^2+1), OrderedDitherMatrixNum);
41
42 %show the image on the screen
43 hFig = figure(); %figure window
44 set(hFig, 'Position', [300 150 1200 800]); %resize window
45 imshow(DitheredImg); %show the image
46 % subplot(1,2,1), imshow(OriginalImg);

```

```

47 % subplot(1,2,2), imshow(DitheredImg);
48
49
50
51 %not used code, leaving it here just in case i need to reuse part of it
52 %=====
53 % subplot(1,2,1), imshow(img);
54 % subplot(1,2,2), imshow(DitheredImg);
55 % subplot(1,2,2), imshow(imcomplement(NewImage));
56 % imshow(NewImage);
57
58
59 % Dimentions(1:4) = size(DitherImg);
60 % NewImageWidth = Dimentions(1)*Dimentions(3);
61 % NewImageHeight = Dimentions(2)*Dimentions(4);
62 % NewImage = zeros(NewImageWidth, NewImageHeight);
63 % %convert from 4D matrix to 2D matrix that we can use to show the image
64 % for i=1:NewImageHeight
65 %     for j=1:NewImageWidth
66 %         NewImage(j,i) = DitherImg(ceil(j/n), ceil(i/n), max(mod(j, n), 1), max
        (mod(i, n), 1));
67 %     end
68 % end

```

Class ImgManager and Function DitheredImg is defined here:

```

1
2 classdef ImgManager<handle
3     %IMGMANAGER Summary of this class goes here
4     % Detailed explanation goes here
5
6     properties (Access = private)
7         OrderedDither;
8 %         ODDNum;
9     end
10
11     methods
12         %constructor
13         function obj = ImgManager()
14 %             obj.ODNum = 2;
15             obj.OrderedDither(1, :, :) = [6, 48, 14, 40, 8, 46, 16, 38; ...
16                                             64, 21, 51, 28, 60, 9, 53, 32; ...
17                                             13, 35, 1, 42, 10, 33, 3, 45; ...
18                                             56, 27, 58, 18, 50, 26, 59, 24; ...
19                                             7, 44, 9, 34, 2, 41, 12, 39; ...
20                                             62, 20, 49, 25, 57, 17, 52, 30; ...
21                                             15, 37, 4, 43, 11, 36, 5, 47; ...
22                                             54, 31, 61, 23, 55, 29, 63, 22];
23
24         %matrix 2
25         obj.OrderedDither(2, :, :) = [15, 62, 19, 34, 1, 50, 31, 46; ...
26                                         18, 35, 16, 63, 32, 47, 2, 49; ...
27                                         61, 14, 33, 20, 51, 4, 45, 30; ...
28                                         36, 17, 60, 13, 64, 29, 48, 3; ...
29                                         11, 58, 21, 40, 5, 52, 27, 44; ...
30                                         22, 37, 12, 59, 28, 41, 6, 53; ...
31                                         57, 10, 39, 24, 55, 8, 43, 26; ...
32                                         38, 23, 56, 9, 42, 25, 54, 7];
33
34         %convert image to grayscale then load it and return the loaded
35         %image
36         function handle = load(~, path)
37             if nargin < 2

```

```

38     path = 'Images/1.jpg';
39     end
40     handle = rgb2gray(imread(path));
41 end
42
43 %this function halftone an image using an ordered dither algorithm
44 function DitheredImg = Dither(obj, areaDimension, ReadyImg,
45     Brightnesslevels, Order)
46     %check the number of arguments and fill the missing parameters
47     %with default values
48     if nargin < 2
49         areaDimension = [1, 1];
50     end
51     if nargin < 3
52         ReadyImg = obj.load('Images/1.jpg');
53     end
54     if nargin < 4
55         Brightnesslevels = 65;
56     end
57     if nargin < 5
58         Order = 1;
59     end
60 %
61     ReadyImg = obj.load(Img);
62     %get width and height
63     [width, height] = size(ReadyImg);
64     FullSegments = [fix(width/areaDimension) fix(height/areaDimension)];
65     LeftOver = [mod(width, areaDimension), mod(height, areaDimension)];
66
67     %determine the number of segments of the image, if it is an image
68     %with dimensions which are multiplication of 8 then there would
69     %be no leftovers at the edges
70     if(LeftOver(1) ~= 0)
71         w = FullSegments(1)+1;
72     else
73         w = FullSegments(1);
74     end
75     if(LeftOver(2) ~= 0)
76         h = FullSegments(2)+1;
77     else
78         h = FullSegments(2);
79     end
80     %initialize the matrix to store the dithered image values
81     ImageSegmentsValues = zeros(w, h);
82     ZerOneMatrix = zeros(w, h, areaDimension, areaDimension);
83
84     %for each column and each row
85     for i=1:FullSegments(2)
86         for j=1:FullSegments(1)
87             AllValuesInCurrentImageSegment = obj.readImgPartValues(
88                 ReadyImg, ((j-1)*areaDimension)+1, ((i-1)*areaDimension)
89                 +1, areaDimension);
90             %fill in number of dots that we want to show per segment.
91             %example we want 65 level of brightness, and the mean of
92             %values was 255 (completely white)
93             %65-1 = round((255+1) / (256/(65-1))) =
94             %64 = round(256 / (256/64)) =
95             %64 = round(256 / 4) =
96             %64 = round(64) =
97             %64 - 64 = 0 (so we are going to fill no dots at all)
98             ImageSegmentsValues(j, i) = (Brightnesslevels -1) - round((
99                 mean(mean(AllValuesInCurrentImageSegment))+1) / (256/(
100                     Brightnesslevels -1)));
101             ZerOneMatrix(j,i, :, :) = obj.getzeromatrix(

```



```

    ImageSegmentsValues(j, i), obj.OrderedDither(Order, :, :),
    areaDimension, areaDimension);
96     end
97     %deal with the leftover on the most right column if
98     %exist
99     if (LeftOver(1) ~= 0)
100         AllValuesInCurrentImageSegmentLeftOver = obj.
            readImgPartValues(ReadyImg, (FullSegments(1)*
            areaDimension)+1, ((i-1)*areaDimension)+1, LeftOver(1),
            areaDimension);
101         ImageSegmentsValues(FullSegments(1)+1, i) = (
            Brightnesslevels -1) - round((mean(mean(
            AllValuesInCurrentImageSegmentLeftOver))+1) / (256/(
            Brightnesslevels -1)));
102         ZerOneMatrix(FullSegments(1)+1,i, :, :) = obj.getzero1matrix(
            ImageSegmentsValues(FullSegments(1)+1, i), obj.
            OrderedDither(Order, :, :));
103     end
104     end
105     %deal with the leftover on the bottom row
106     if (LeftOver(2) ~= 0)
107         for k=1:FullSegments(1)
108             AllValuesInCurrentImageSegmentLeftOver = obj.
                readImgPartValues(ReadyImg, ((k-1)*areaDimension)+1,
                FullSegments(2)+1, areaDimension, LeftOver(2));
109             ImageSegmentsValues(FullSegments(1)+1, i) = (
                Brightnesslevels -1) - round((mean(mean(
                AllValuesInCurrentImageSegmentLeftOver))+1) / (256/(
                Brightnesslevels -1)));
110             ZerOneMatrix(k, FullSegments(2)+1, :, :) = obj.getzero1matrix(
                ImageSegmentsValues(k, FullSegments(2)+1), obj.
                OrderedDither(Order, :, :));
111         end
112     end
113
114     %deal with the bottom right corner
115     if (LeftOver(1)>0 && LeftOver(2)>0)
116
117     end
118     TempMatrix = obj.Get2Dfrom4D(ZerOneMatrix, areaDimension);
119     DitheredImg = TempMatrix(1:width, 1:height)*255;
120 end
121
122 %this function gets return a matrix from the mean values of a part
123 %of the image, the matrix only have 0s and 1s, which then can be
124 %used to generate each part of the new dithered image
125 function DotZero1Matrix = getzero1matrix(obj, BrightnessValue, matrix, n
, m)
126 %deal with missing arguments
127 if nargin < 2
128     BrightnessValue = 65;
129 end
130 if nargin < 3
131     matrix = obj.OrderedDither(1, :, :);
132 end
133 if nargin < 4
134     n = 8;
135 end
136 if nargin < 5
137     m = n;
138 end
139
140 DotZero1MatrixTemp = ones(size(matrix));
141 for i=1:(BrightnessValue-1)

```

```

142         DotZero1MatrixTemp(find(matrix == i, 1)) = 0;
143     end
144     DotZero1Matrix = DotZero1MatrixTemp(1, 1:n, 1:m);
145 end
146
147 %this function return a part of an image
148 function values = readImgPartValues(obj, img, x, y, n, m)
149     if nargin < 3
150         x = 1;
151     end
152     if nargin < 4
153         y = x;
154     end
155     if nargin < 5
156         n = 1;
157     end
158     if nargin < 6
159         m = n;
160     end
161
162     [width, height] = size(img);
163     NumDotsX = n;
164     NumDotsY = m;
165
166     %is the starting point inside the image
167     if x<=width && y<=height
168         %does the area that we want extend beyond the edges of
169         %the images if yes then only read from x,y to the edges
170         if (x+n > width)
171             NumDotsX = width - x;
172         end
173         if (y+n > height)
174             NumDotsY = height - y;
175         end
176         %return the values of all the pixels that we want to read
177         values = img(x:(x+NumDotsX), y:(y+NumDotsY));
178     else
179         'error: x or y is outside of image'
180         values = 0;
181     end
182 end
183
184 %convert 4d matrix to 2D
185 function Matrix2D = Get2Dfrom4D(obj, Matrix4D, n)
186     if nargin < 3
187         n = 8;
188     end
189     Dimensions(1:4) = size(Matrix4D);
190     width = Dimensions(1)*Dimensions(3);
191     height = Dimensions(2)*Dimensions(4);
192     Matrix2D = zeros(width, height);
193     for i=1:height
194         for j=1:width
195             Matrix2D(j,i) = Matrix4D(ceil(j/n), ceil(i/n), max(mod(j, n),
196                 1), max(mod(i, n), 1));
197         end
198     end
199 end
200 end
201
202 %
203 ZerOneMatrix = zeros(FullSegments(1), FullSegments(2), area,
    area);

```

```

204 %           for i=1:FullSegments(2)
205 %           for j=1:FullSegments(1)
206 %               AllValuesInCurrentImageSegment = obj.readImgPartValues(
ReadyImg, ((j-1)*area)+1, ((i-1)*area)+1, area);
207 %
208 %               %fill in number of dots that we want to show per
segment.
209 %               %example we want 65 level of brightness, and the mean
of values was 255 (completely white)
210 %               %(65-1) - round((255+1) / (256/(65-1))) =
211 %               %64 - round(256 / (256/64)) =
212 %               %64 - round(256 / 4) =
213 %               %64 - round(64) =
214 %               %64 - 64 = 0 (so we are going to fill no dots at all)
215 %               ImageSegmentsValues(j, i) = (Brightnesslevels -1) -
round((mean(mean( AllValuesInCurrentImageSegment))+1) / (256/(
Brightnesslevels -1))));
216 % %           ZerOneMatrix(j,i, :, :) = obj.getzero1matrix(
ImageSegmentsValues(j, i));
217 %           ZerOneMatrix(j,i, :, :) = obj.getzero1matrix(
ImageSegmentsValues(j, i), obj.OrderedDither(2, :, :));
218 %           end
219 %       end
220 %       DitheredImg = 255*ZerOneMatrix;
221
222 ans =
223
224   ImgManager with no properties.
225
226
227
228
229 Published with MATLAB R2016a

```



## **Chapter 4**

### **Results**







# References

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