

# CSCD84: Artificial Intelligence

## Worksheet: Probability Review

### Q1

Suppose the variables  $A$  and  $B$  are Boolean variables (i.e.,  $A$  can have the value  $a$  or  $\neg a$ ) and  $A$  is independent of  $B$ . Determine the missing values in the joint distribution for  $P(A, B)$  below.

$P(\neg a, \neg b)$	0.1
$P(\neg a, b)$	0.3
$P(a, \neg b)$	
$P(a, b)$	

### Q2

Suppose  $A$ ,  $B$  and  $C$  are Boolean variables and that  $B$  is independent of  $C$  given  $A$ . Determine the missing values in the joint distribution for  $P(A, B, C)$  below.

$P(\neg a, \neg b, \neg c)$	0.01
$P(\neg a, \neg b, c)$	0.02
$P(\neg a, b, \neg c)$	0.03
$P(\neg a, b, c)$	
$P(a, \neg b, \neg c)$	0.01
$P(a, \neg b, c)$	0.1
$P(a, b, \neg c)$	
$P(a, b, c)$	

### Q3

Given that  $P(A | B) < P(A)$ . Show that  $P(B | A) < P(B)$ .