Active Learning

- We saw how to Learn 7/2(5) with TD learning.
- That was good for pussive learning.
 - In passive Leurning, we are given samples generaled by

policy 70

- Brown task is to find V2(5). To Learning is a model-free approach to Learn V2(5)'s.
- Active Learning: We want to be able to do more than that? We want to be able to update policy TC (i.e., the Sampling policy) so that not only we collect samples and learn the model, but also make decision that give us good rewards.

Active Learning

Active Reinforcement	Learning:	
Fi Actively Collecting	Learning: data, while we learn the model	
Problem model:		
Give don't know T	and R, and We choose the actions.	
Fi Goal: Learn the	optimal policy/actions.	

Active Learning

In active reinforcement learning, Learner makes the choices. Fundamental tradeaff: 42 exploration v.s. exploitation

Recall: To Estimate an Expectation, use Running Average of Samples

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X[R(s,a,s')+87/4K(s')

Can We Use Running Average to Estimate Optimal Values?

Now, we want to do active learning, Fire., Learning the optimal policy/value/q-value Can we use the same idea as in TD to find T(s)? Fi In other words, Can we use running averaging to find T(s)?

Let's revisit the recursion for optimal values, i.e. T(s): $\nabla T(s) = \max_{s} \sum_{s} T(s, a, s) [R(s, a, s') + \gamma V(s')]$ Main question: Is T(s) written in the above recursion an expectation? Yes 13 No 13 Why ?

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Can We Use Running Average to Estimate q-values?

Now, let's write the recursion for Q'(s,a) in terms of Q*

■ Nice!

Q-learning

R-learning: Sample-based q-value iteration.

We have: $Q^*(s,a) = Z T(s,a,s') [R(s,a,s') + \gamma \max_{a'} Q^*(s,a')]$

Thus, we can estimate the above expectation by

47 Whenever you receive a new sample from

a transition like (5, a, S', R15,a,S'),

43 By using running averaging you can uplate your estimate of Q*(5,a): Q_K+1(5,a) < (1-a) Q_K(5,a) + a[R(5,a,s')+ 7max Q(s'a')]

New Sample

Q-Learning Properties

Q-learning Converges to optimal quality, even if you're acting This is called off-policy learning. what it means is that in the limit it doesn't matter how you select the action. Regardless of action selection, you will Converge to the applicable q-values (hance optimal policy) in the limit. ■ But, 47 you have to explore enough (Needs to visit all states often enough) Fi you have to eventually make the learning rate small enough, but not decrease too quickly.

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Exploration vs. Exploitation

It's not a good idea to always exploit the action that you consider to be the best action you've seen so far.

You have to try many actions. You must explore.

They may not be good for you. But you won't know unless you try them.

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How to Explore

```
Several scheme for forcing exploration.

The random actions (E-greedy)
with E-greedy, we eventually explore the space shonce, find the optimal values
   But, il Keeps randomly cheusing actions even when the learning
   is done
42 Solutions: i) lower & over time ii) use exploration function
```

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i) Lower & Over Time

one option is to set E=1/2.

i.e., at time step t, with probability 1/2, act randomly with probability (1-t), act on optimal policy.

It does eventually converge, but 47 It can be slow

43 It explore all states with similar probability

ii) Exploration Functions

I den: to explore areas whose budness is not (yet) established, and eventually stop exploring

We can implement this idea by modifying our estimate of the q-values.

increase the estimate 4-values based on how unexplored they are:

- previously, new sample was: R(s, a, s') + y man Q(s', a')• With exploration function, we modify the new sample to R(s, a, s') + y man f(Q(s', a'), N(s', a')) a'

Exploration Functions, cont'd

- N(s',a'): # times we had seen the pair <math>(s',a') before $f(Q(s',a'),N(s',a')) = Q(s',a') + \frac{K}{N(s',a')}$ some constant reploration function
- 56, the update rule with exploration function will be

$$Q_{k+1}(s,a) \leftarrow (1-\alpha) Q_k(s,a) + \alpha \left[R(s,a,s') + \gamma \max_{a'} f(Q(s,a'), N(s,a')) \right]$$

- Note: This propagates the "bonus" back to states that lead
- to unknown states, as well.

Regret (not on exam)

- Regret is a measure of your total mistake cost.

 The difference between:
 - · Your (expected) reward, including youthful suboptimality
 - o and, optimal (expected) reward
- To minimize regret, you need to go beyond learning to be optimal. If It requires optimally learning to be optimal
- Eg: random exploration and exploration function both Converge to optimal Solution
 - 3 But random exploration has higher regret.

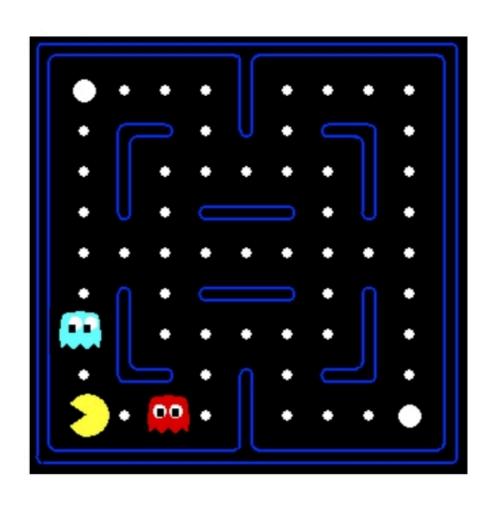
Approximat Q-Learning

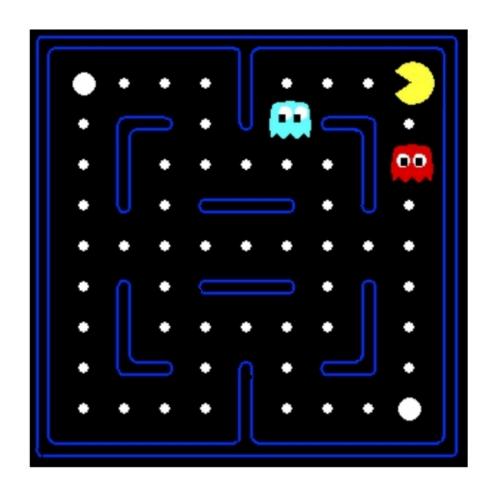
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■ Q-Learning Keeps a table of all q-values
In real life problem, we cannot possibly learn about every
Single State
  FI Too many state to visit them all
  43 Too many states to hold the q-tables in memory
1 We should generalize
 4) Learn about the small number of training states you encounter
during training.
 45 Generalize that knowledge to new similar states (similar to what we did in supervised learning)
```

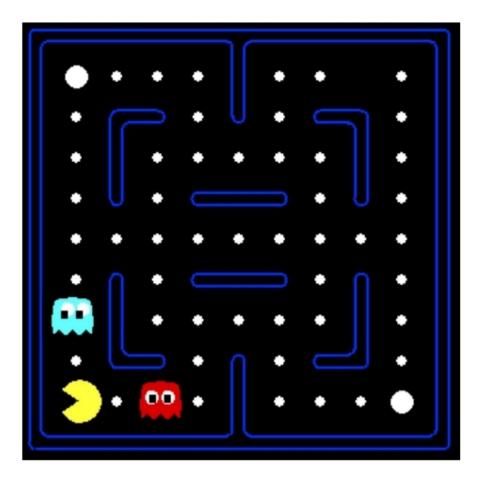
Approximate Q-Learning

Let's say we discover through experience that this state is bad: In naïve q-learning, we know nothing about this state:

Or even this one!







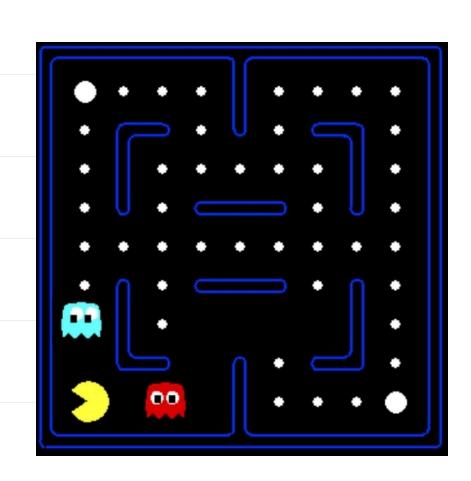
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Feature Based Representations

- Solution: Describe a state using a vector of features
- E.g.;
 - 43 Distance to closest ghest
 - 43 Distance to closest food
 - 4 Is pacmen in a tunnel? (0/1)
 - 43 etc.
- Similarly, we can represent q-states (5,a) with fentures.
 - FIE.g., action moves closer to food, etc.



Linear Value Function

■ Idea: approximate 4-value of (5,a) with a linear Combination of the features $Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + ... + w_d f_1(s,a)$ Foros: our experince is summed up in a few powerful numbers. Cons: States may share features, but could be very different ● you must have enogh features But wait. We are estimating some unknown target function as a linear combination of some feature 9 We saw this before: That's the beauty of ECE421. The loop is closed.
Your welcome!

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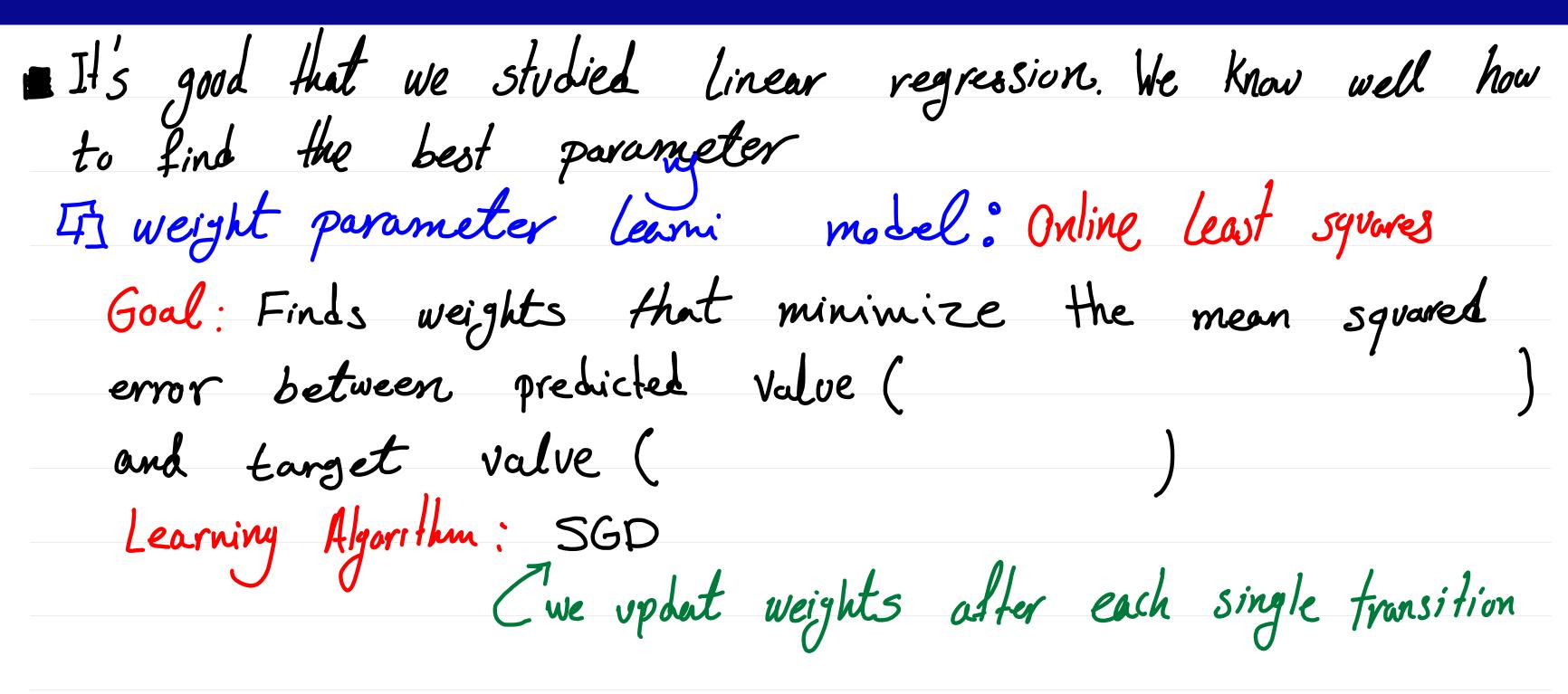
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Approximate Q-Learning

= Q-learning: Q(s,a) \ Q(s,a) + \(\int \Q(s,a) - (R(s,a,s') + \gamma \are \Q(s',a'))\) It we use a table to keep track of 9-values of (5,a) pairs Q-Learning with linear Value function: If we have features (f, (s,a), fz(s,a), ...) and weight (w,, wz,...) 43 We must learn the weight with which we can approximate the values "best". • What does "best mean" * It should minimize the error between prediction and observation/sample.

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Approximate Q-Learning and Onlin Least Squares



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Approximate Q-Learning and Online Least Squares

■ SGD:
$$w_i \leftarrow w_i - \eta \nabla_{\underline{w}} e_n$$

$$e_n(\underline{w}) =$$

Homework: Interpret Q-Learning as an Online Least Squares problem

In Q-learning, we saw the update

Q(s,a) \(-Q(s,a) - \alpha \big(Q(s,a) - (R(s,a,s') + \gamma \text{merx} Q(s,a')) \big].

Use online Least squares to justify this update rule.

[Hint: It's online least squares. So, you have a linear regression model. Clearly, Specify the linear function]

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