

~~✓~~ Linear Regression

— Computational Complexity

— Gradient Descent

ession

mplicity

escent

Age

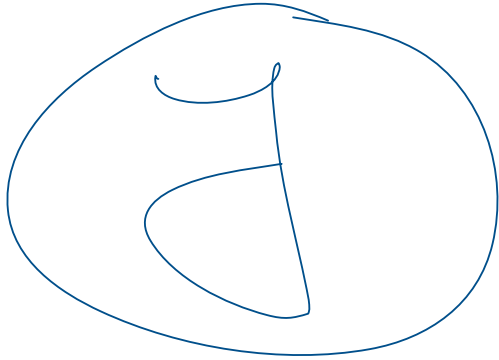
Country

Employer

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Features

Income



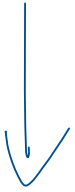
\hat{y}

\hat{y}

$=$

$$\underline{\underline{\theta_0}} + \underline{\theta_1} x_1 + \dots$$

model parameters



pred.

meten

$$+ \frac{\Theta_n x_n}{}$$



features

vectorised form

$$\hat{y} = h_{\theta}(x) = \underline{\underline{\theta^T x}}$$

hypothesis func

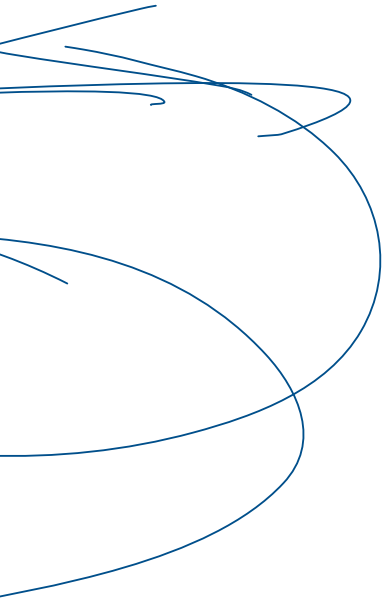
feature
vector

θ, x

tion

$$y = \underline{\underline{x^3 + 4x^2}}$$

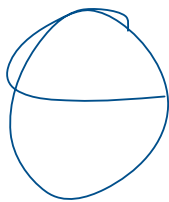
$$x y = \left(\theta_0 + \theta_1 x \right)$$



RMS E \rightarrow

$$\text{MSE}(x, h_0) = -$$

\hookrightarrow cost fun



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ction

Normal Equat

$$\hat{\theta} = (X^T X)$$



cost function optim

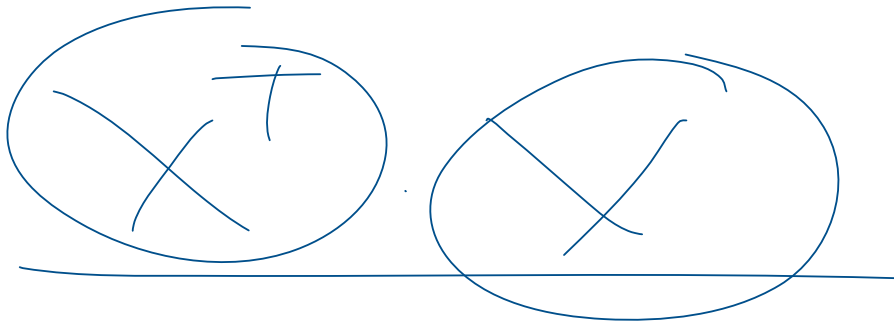
ion

$$-1$$
$$X^T y$$



$$i \geq e$$

Computational Comp



$[x, n]$

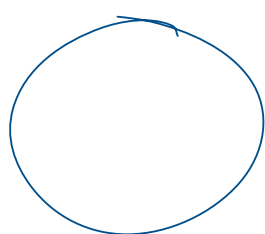
n^2

$(n+1)(n-1)$

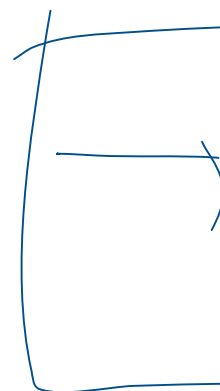
Complexity

$$\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

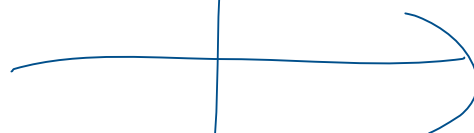
$$n+1)$$



(n^2)



SVD



2

$O(m)$

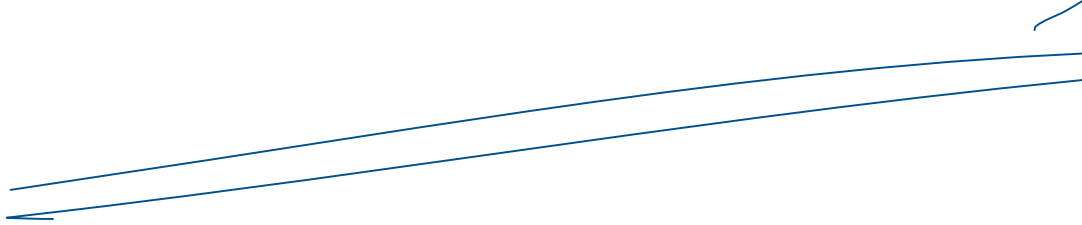
$$O(n^3)$$

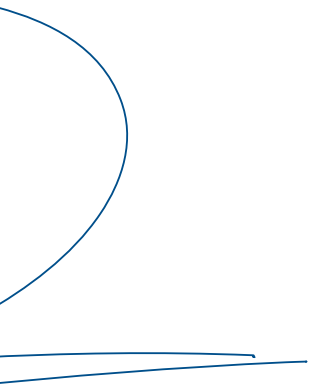
OK



$$4 \rightarrow O(n^2)$$

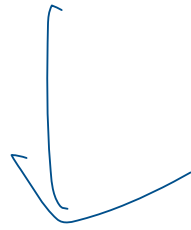
$$\begin{matrix} 8 \\ \cancel{16} \end{matrix} \rightarrow O(n^{2.4})$$





Gradient Desc

- minimize co



Parameter

ent

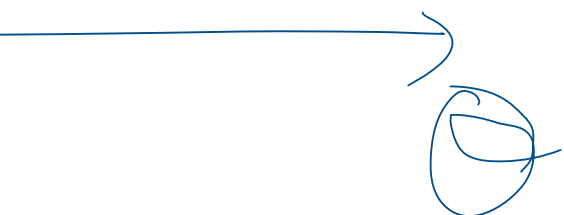
st June

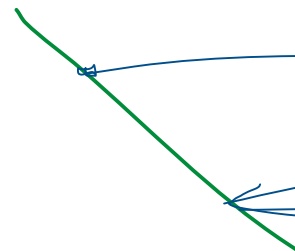
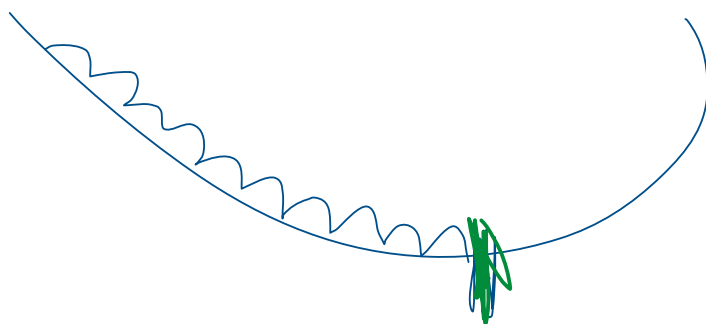
S



rate

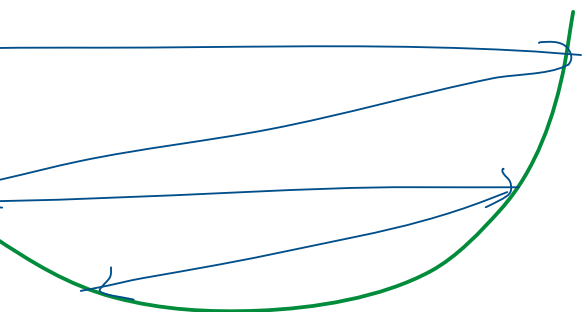
err



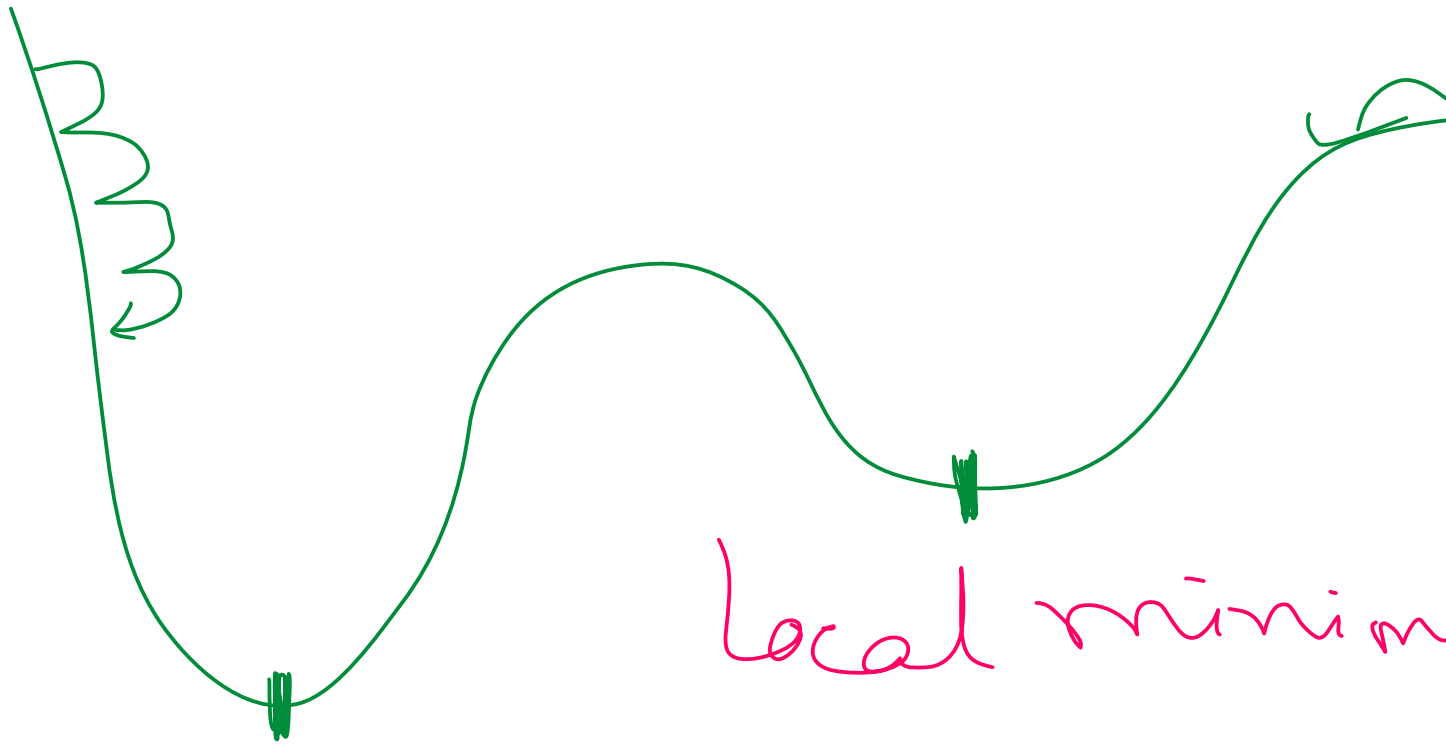


Computational
time $\uparrow\uparrow$

$\pi \uparrow \uparrow$



~~phinkal
soln~~



Global minimum

local minimum

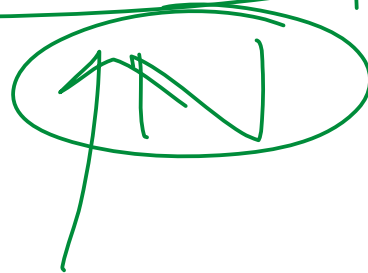


convex \rightarrow global
min

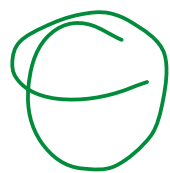
el

mm

Batch GD



Pantial down



ivative

$$MSE(\theta) =$$

$$\begin{pmatrix} \frac{\partial}{\partial \theta} \\ \frac{\partial}{\partial \theta} \\ \vdots \end{pmatrix}$$

- Smoother

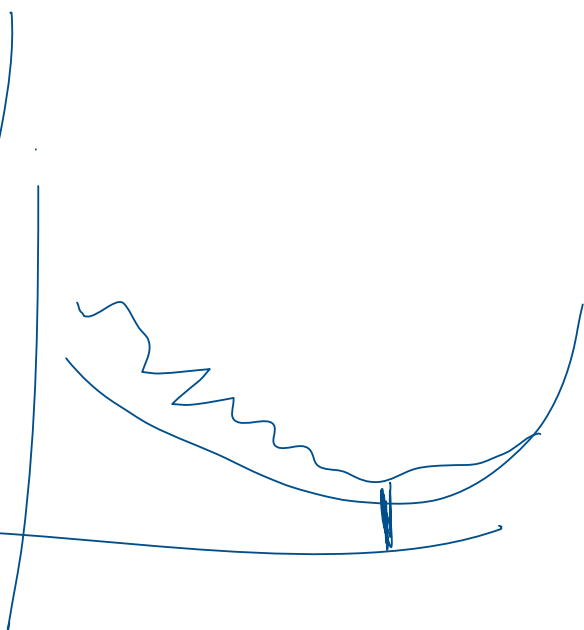
with

$$\begin{pmatrix} \theta_0 \text{ MSE} \\ \theta_1 \text{ MSE} \end{pmatrix}$$

ve

Stochastic GD

- an example
- feed it NN
- calc gradients
- up date weights



en t

sh fs

→ never reaches

minima.

→ vectorized impl

→ larger data

→ faster converg

is
presentation
set
ge

ex

Mini-Batch AD

→ fixed

- a mini-batch p
- Feed
- Mean of gradient
- update

4

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rich

t