

# BIAS

- Predicted values
  - Actual values
  - Error
- } diff
- ←

Irreducible error

Reducible

→ Optimize

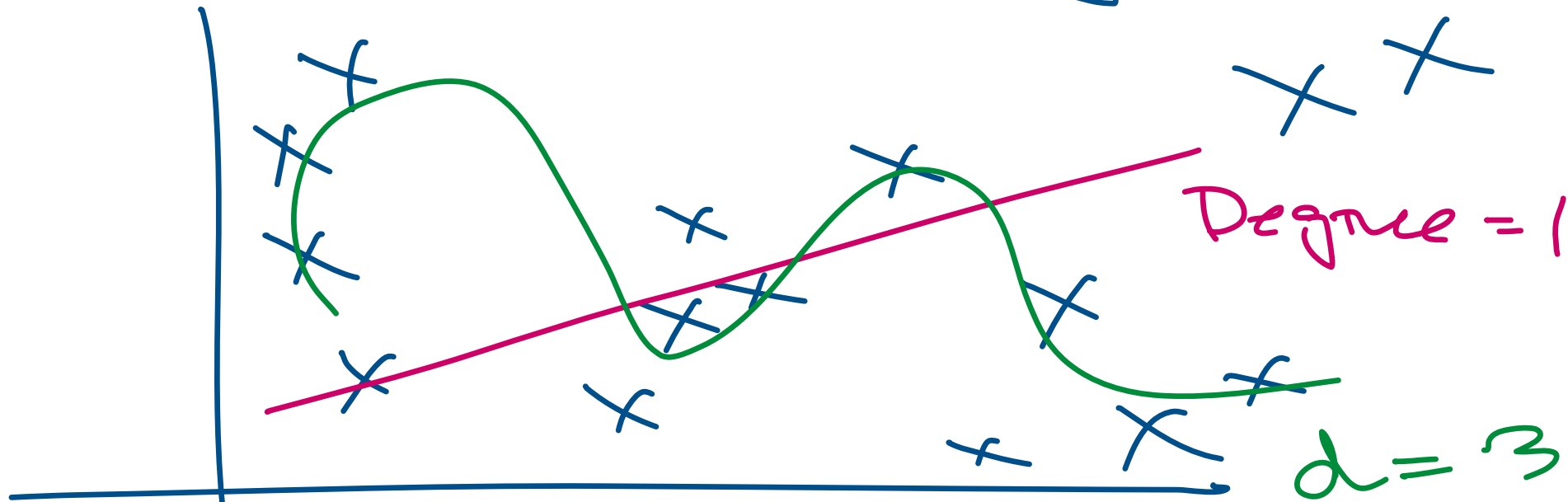
" { Bias  
Variance

# Bias

- Predicted vs. actual
- how far

- High/Low

High Bias  $\rightarrow$  Not good



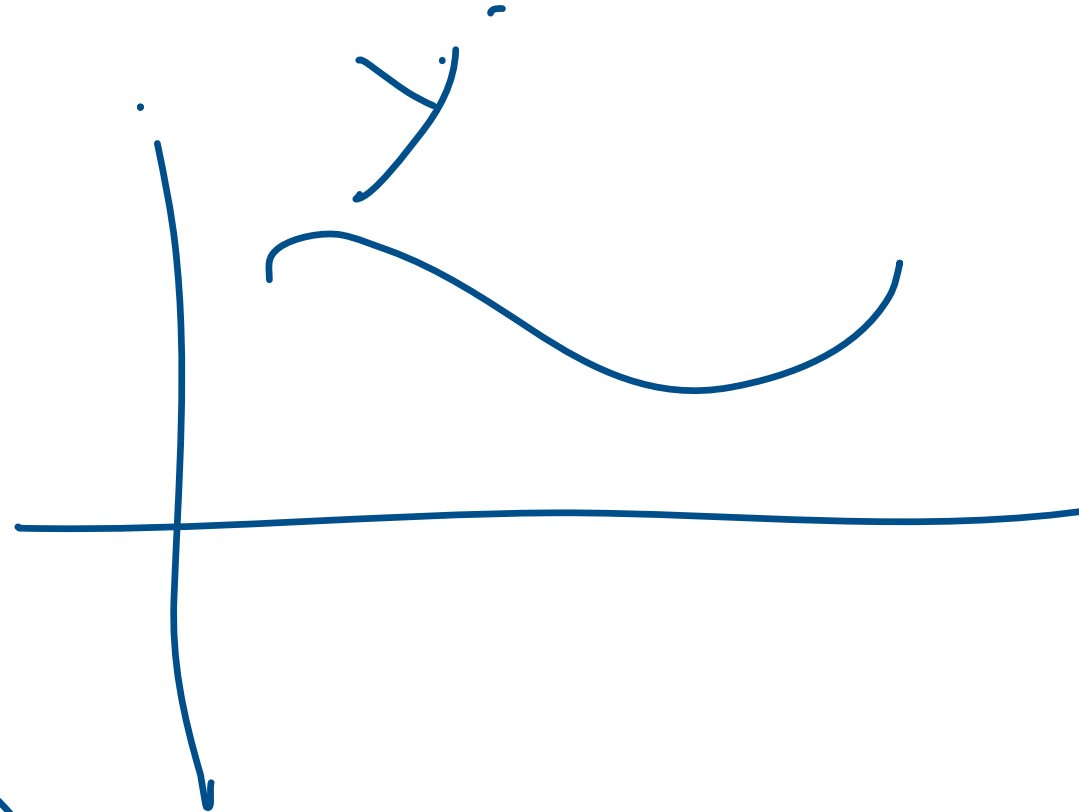
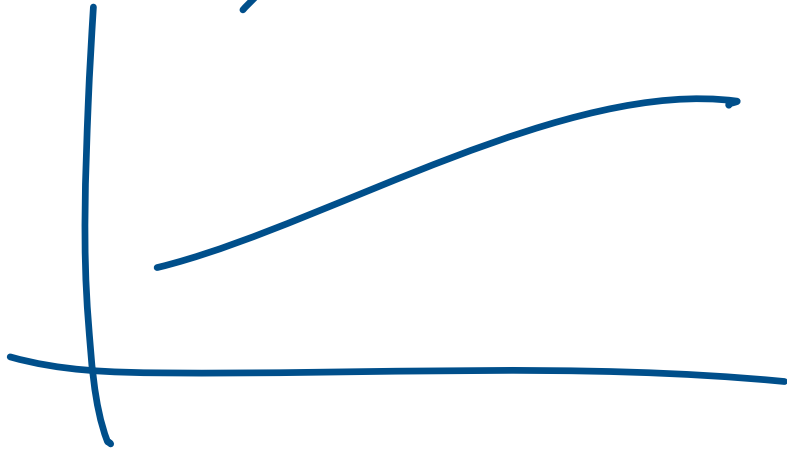
Low Bias  $\rightarrow$  Better

# VARIANCE

Train  $\longrightarrow$  Test  
(Seen) (Unseen)

— how scattered

$$y' = mx'$$



$$x^2 + x^2 = 0$$

—



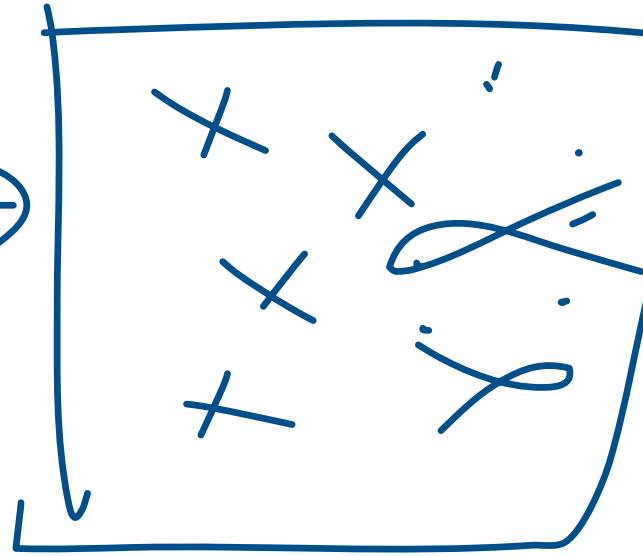
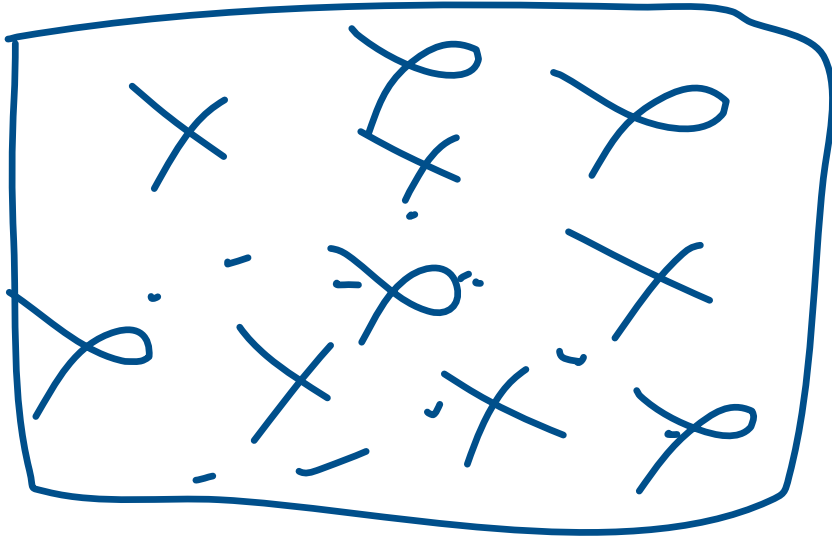
Train

x x  
x  
x x x

Test

△ △ △  
△ △

High Variance



Low

variance

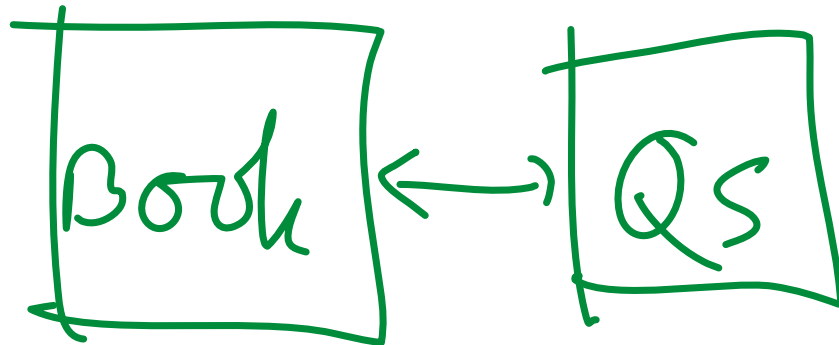
Generalization



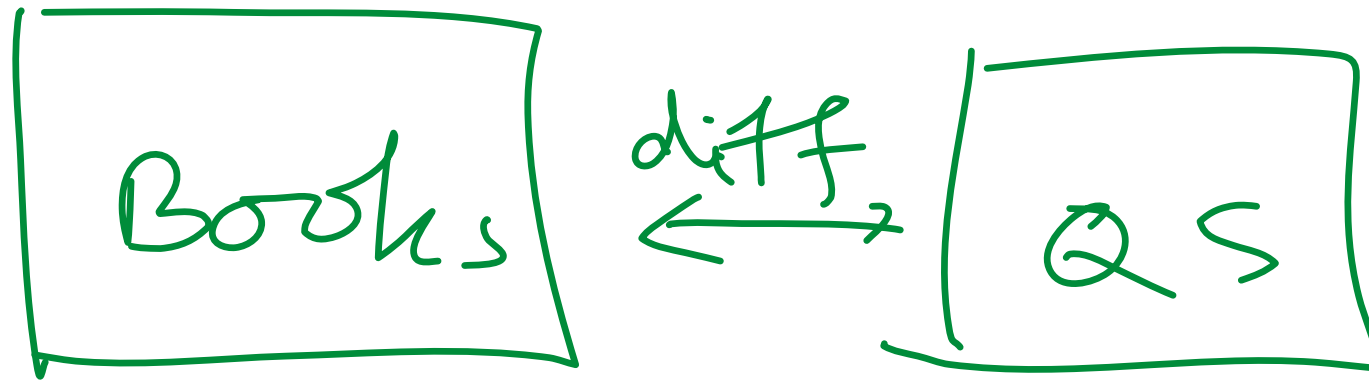
# Effects

① Math x  
Physics x

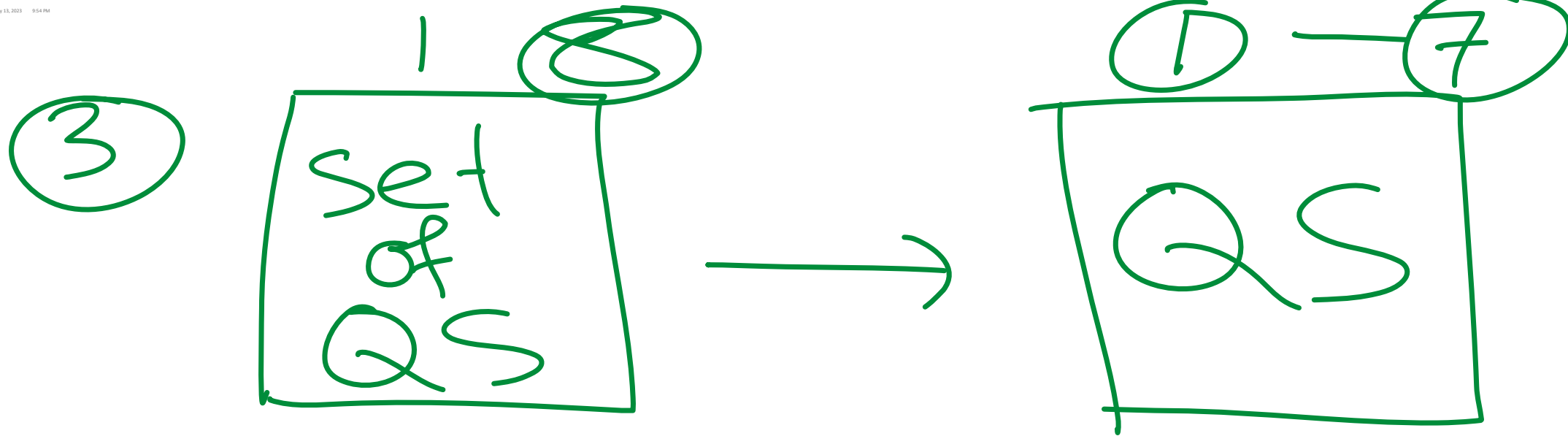
High bias



② Both



low bias, low variance



low bias

high variance

④ high bias  $\rightarrow$  0

low variance

Chemistry

QS

1) LB, LV → Best

LB — Bull's eye, good  
pred

LV — No scattered data points  
close to each other





i) LB, HV  $\rightarrow$  Accurate, but

LB - (i) Inconsistent

HV - Data points are  
scattered

iii) HB, LV  $\rightarrow$  Consistent  
but inaccurate

HB — poor prediction

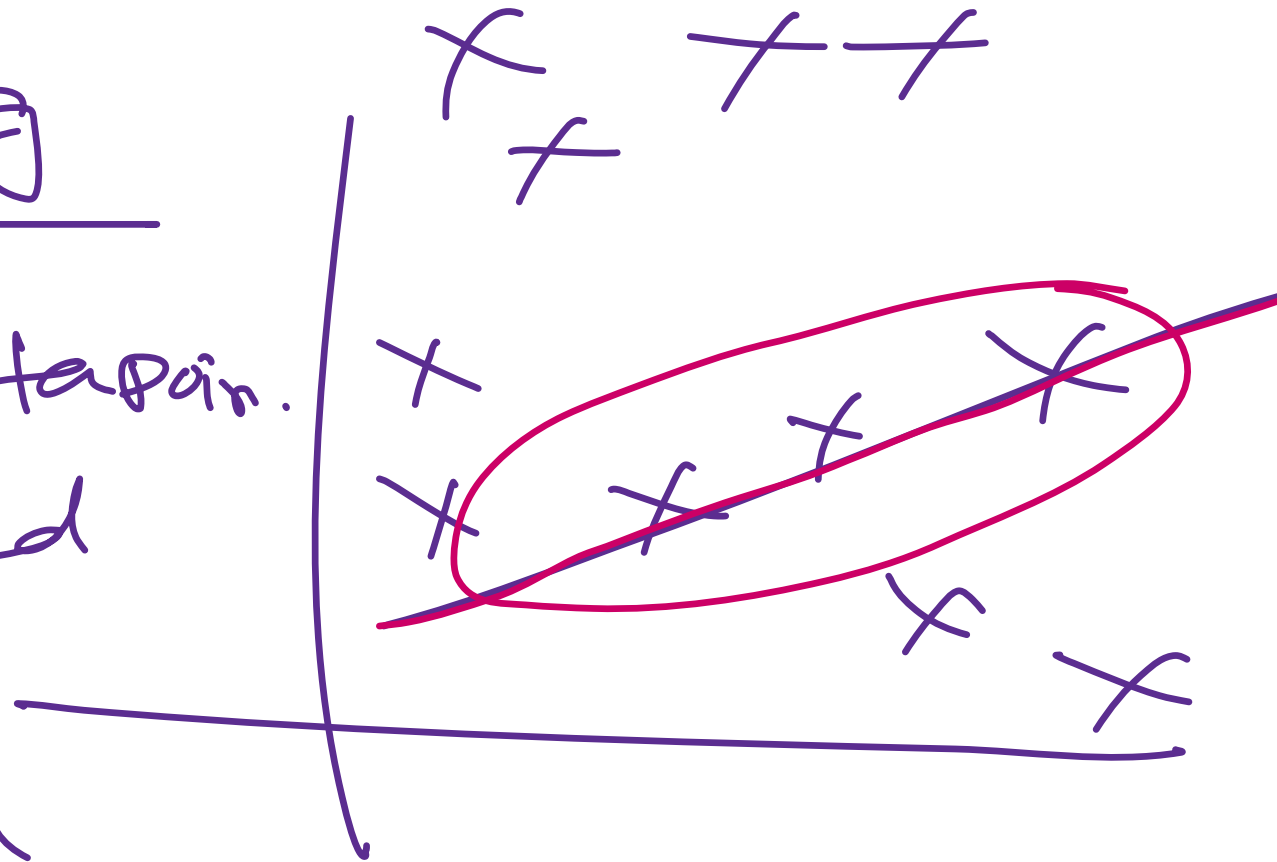
LV — pred data points far away

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iv) HB, HW  $\rightarrow$  X X

# Underfitting

- major datapoints not covered
- scattered
- accuracy  $\downarrow \downarrow$





- low var, high bias  
- Training accuracy  $\rightarrow$  65%

- Testing "  $\rightarrow$  50%  
Truth - Pred

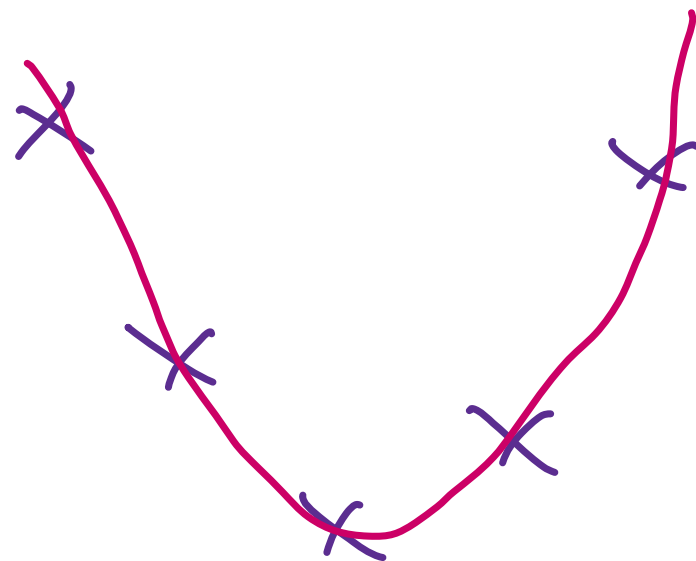
$T_{\text{train}} > T_{\text{test}}$



# Overfitting

Train 95%

Test 70%



1

- High Variance

Train  
 X X X  
 X X

-

Test  
 0  
 X ~~X~~  
 0 0 0 0

- Low bias

Optimality	
Training	acc ↑
Testing	↓ ↑

# Bias - Variance

## Tradeoff

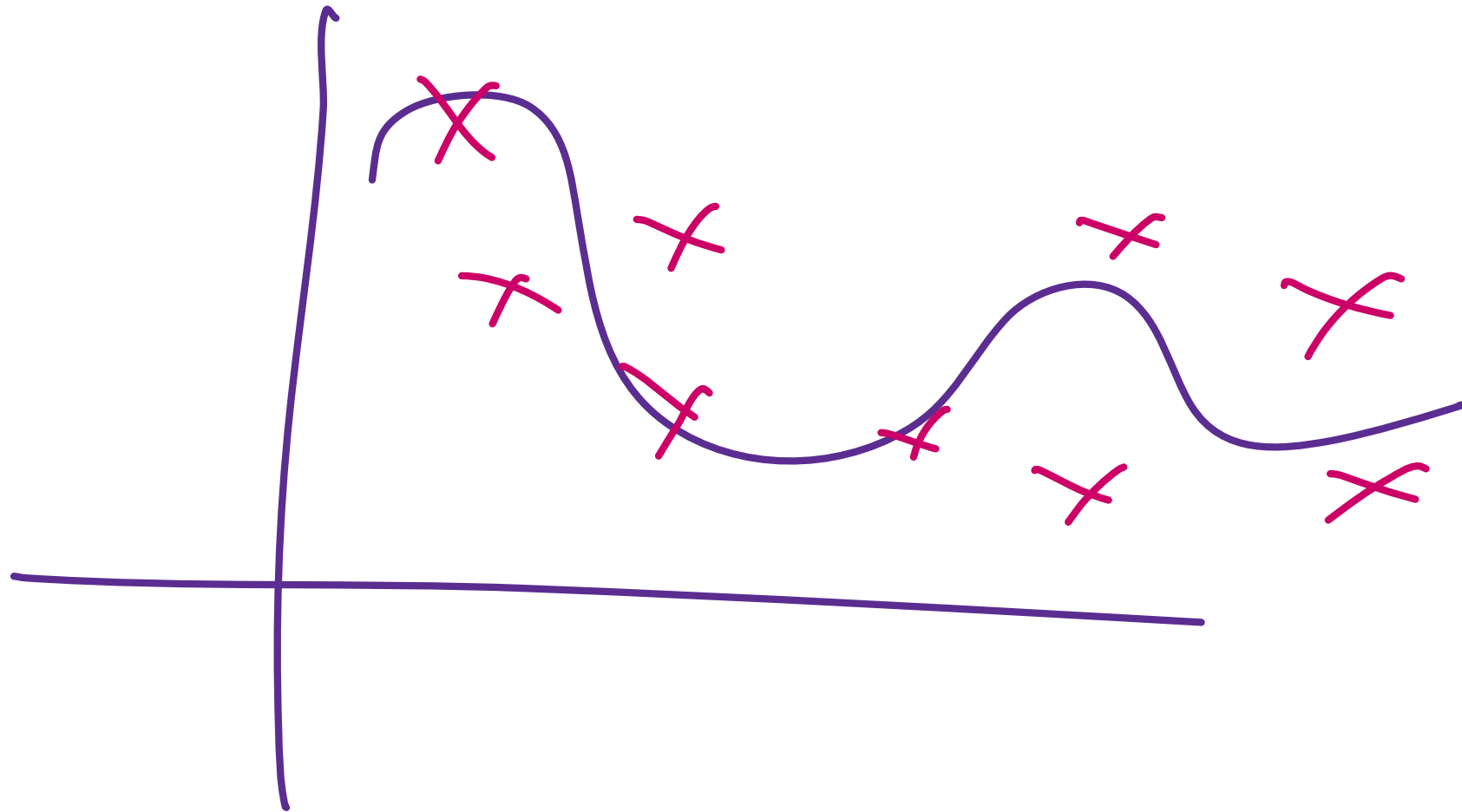
LV

| B

✓ ✓

LD

# RMS E



Under

- Model Simple

- High bias

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Over

- Complicated

- Low bias

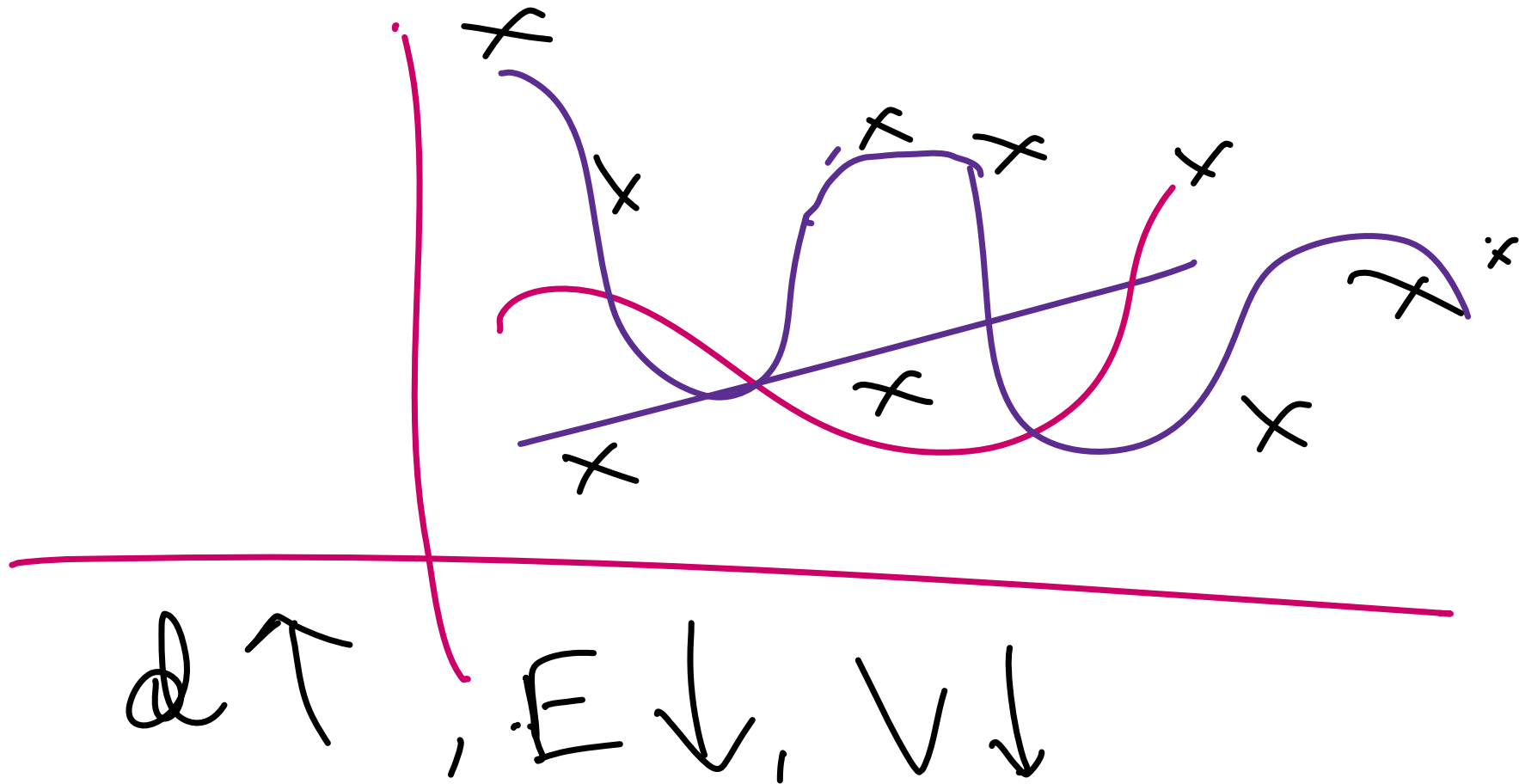
High var:

Balance

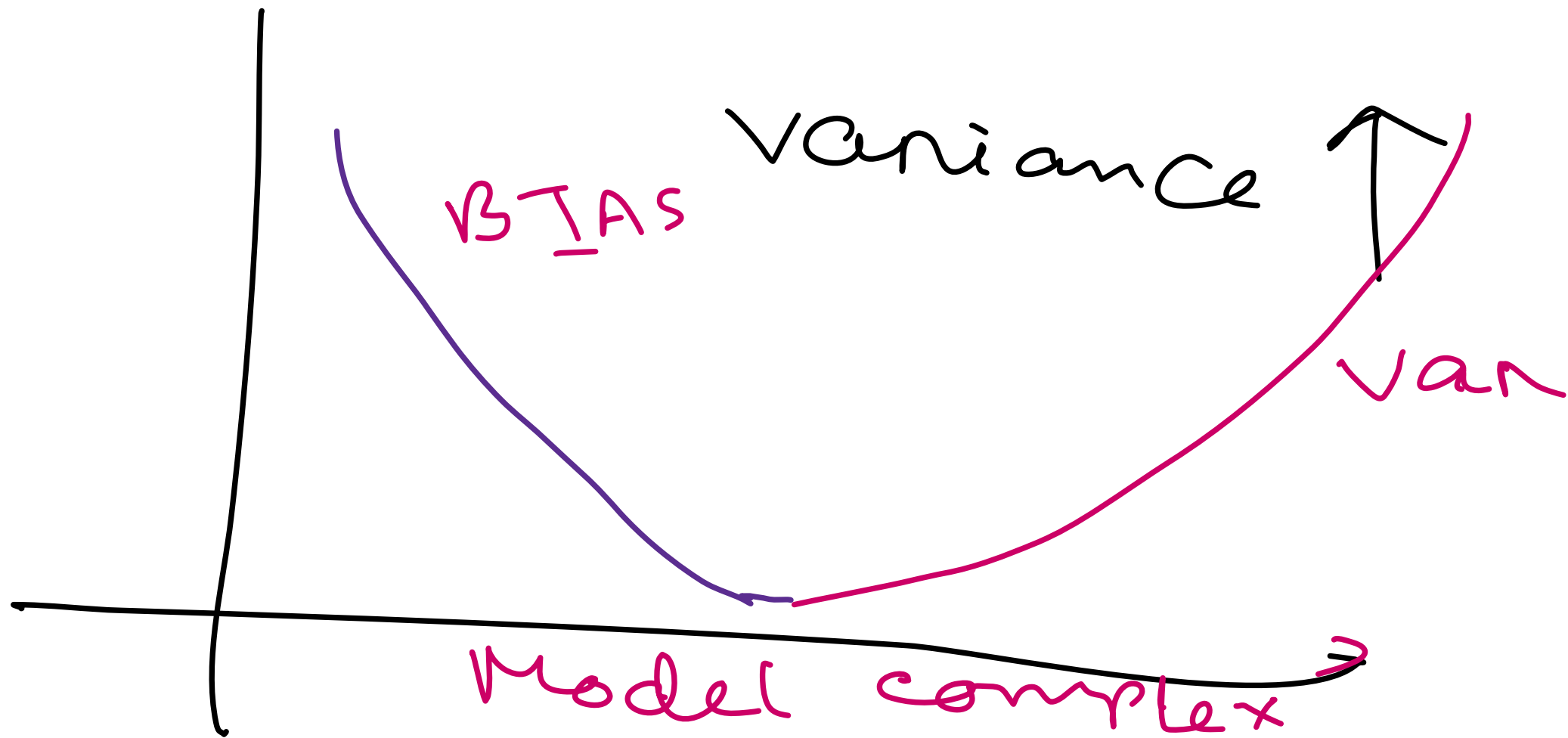




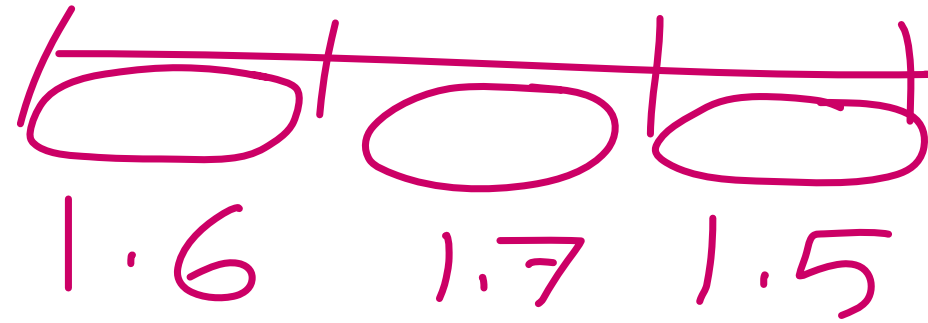
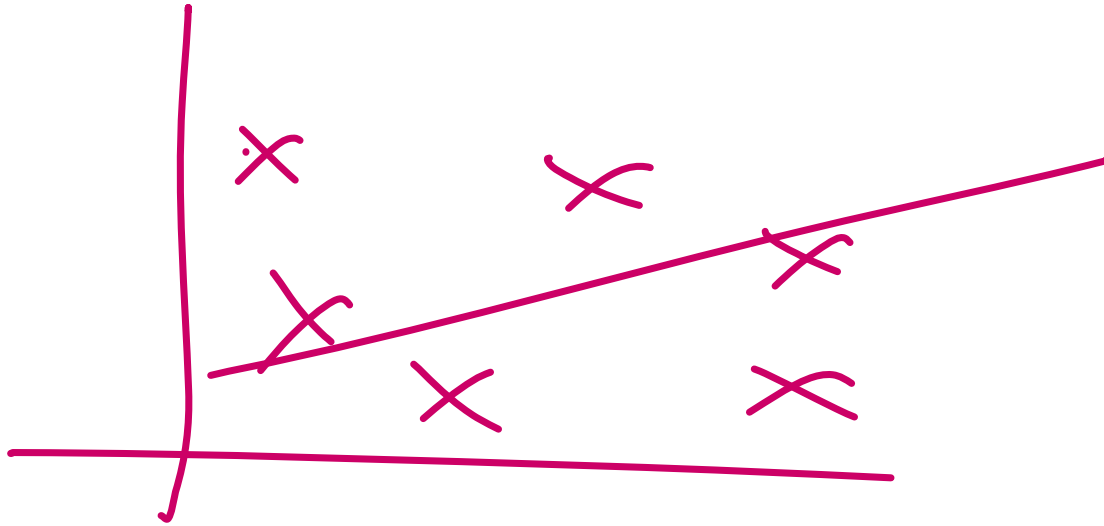
- degree of polynomial



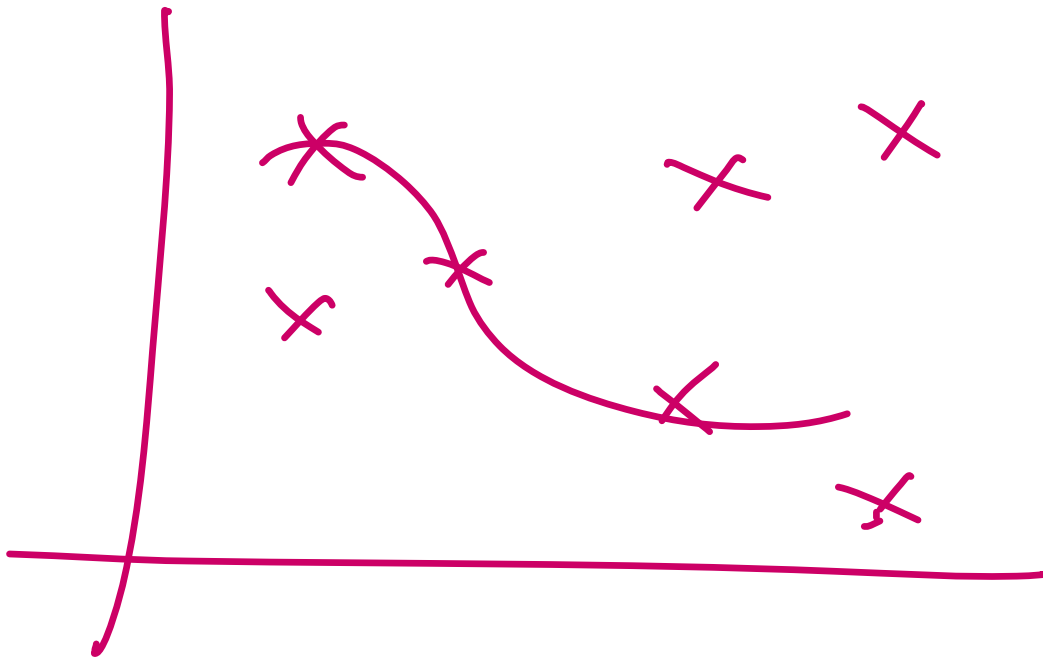
$P \uparrow \uparrow \uparrow$  , bias  $\downarrow \downarrow$



- Model — Very simple X  
              \ Super " X



$$r = n \approx n = 51.5\%$$

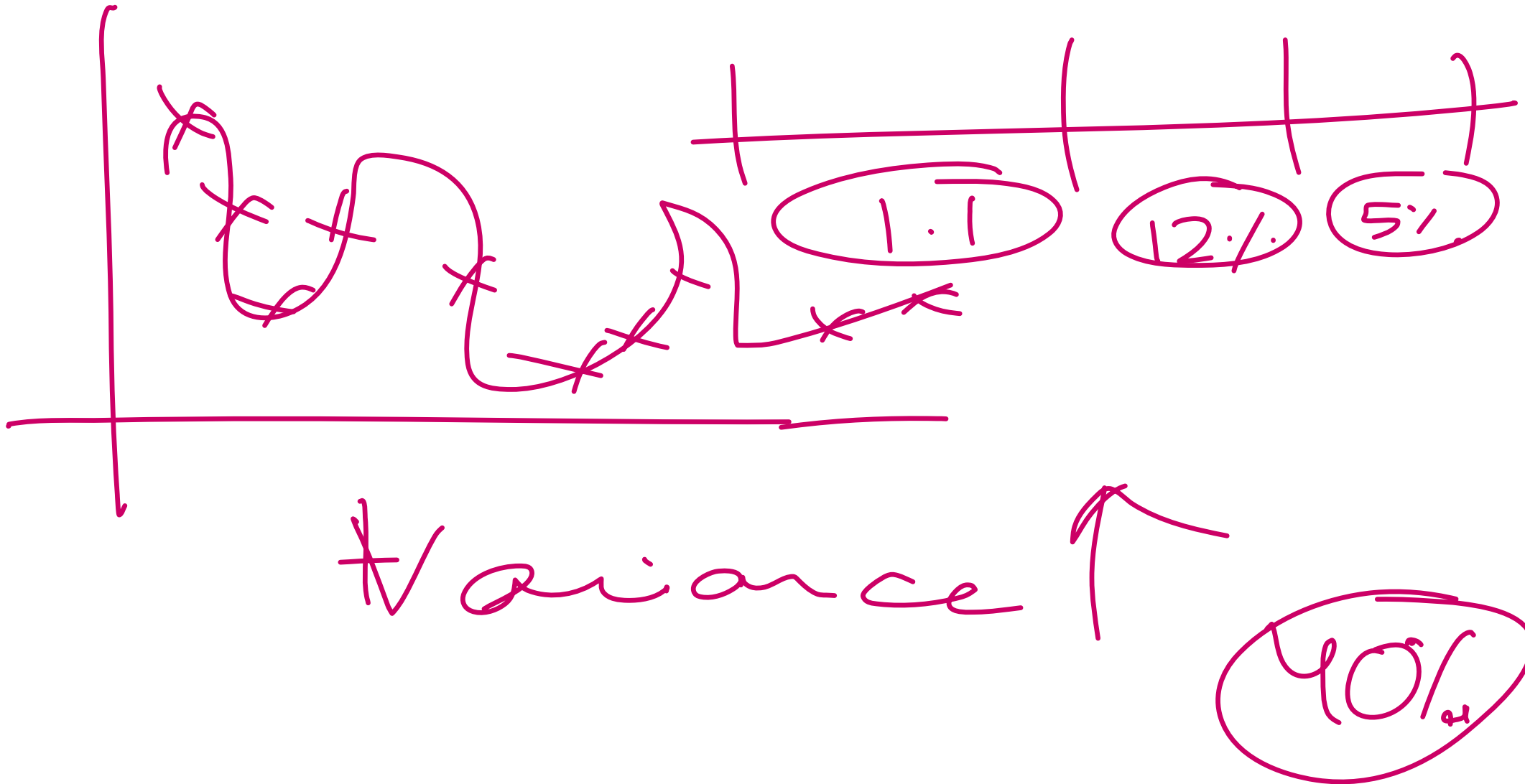


Not generalized

low Bias  
High Variance

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