

Reference: Intro to Real Anolysis by Bontly and Shivbert

Abstract What is Real Analysis Rigorous Study of Real numbers, segunces series and

why the bolow examples are proflenation

- 9 What is the largest Red Number?
- @ what is the longest Natural Number?
- Axiom 1: O is a natural number i.e. 3 when is a furtien differentiable or bounded?

25=2+4+8. blindly do the Some

S= 1-1+1-1+1-1 (1-1) + (1-1) . - -S = (1-(1-1)-(1-1). -

the most very set amount once

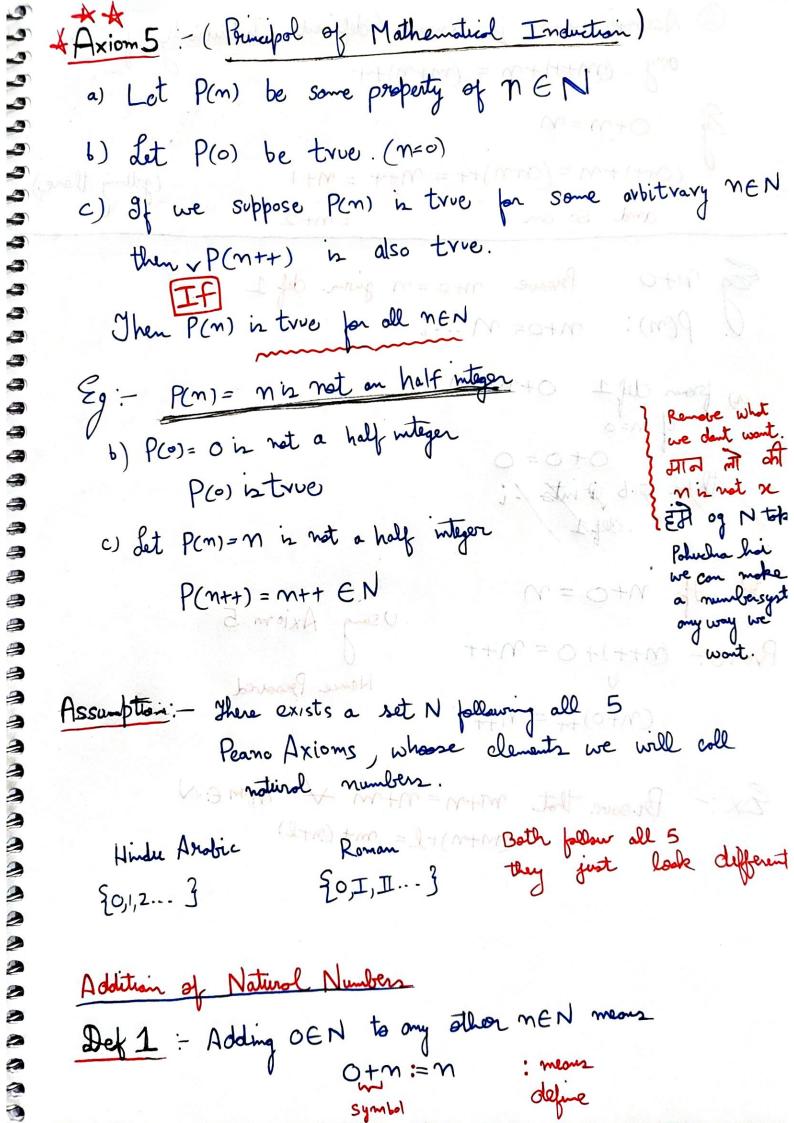
HXIOMZ: If MEN, then " U

Number systems In Sook Manysis N- Natural G-Rottonol of John Da for Amalyon R- Real to brings much C- Complex. Axiomatic Number System (Done by Peans)
Recent Peano axioms for system of Natural numbers graduals and Axiom1: O is a natural number ie OEN Axiom2: If nEN, then "the morement '++' of n, given by n++ belongs to N

Sq: OEN

Bosed on I and 2, let us say Eg: OEN N= {.... 3 where 1=0++EN 2 = (0++)++ EN OEN, OH= | EN, IH=OEN This is not wrong occ. to above 2. so we need more Axioms Axion 3: O is not minement of any Natural Number of m+n =) m++ n++ ond if m=n => m++= m++

Eg: N"= {0,0.5,1,1.5..} we will need more Axioms



Axiom 5 - (Principal of Mathematical Induction) a) Let P(n) be some property of n EN b) Let P(0) be true (n=0) c) If we suppose P(n) is true for some arbitrary MEN then P(n++) is also true. Then P(n) is true for all MEN Eg - P(n) = n is not on half integer b) P(0) = 0 is not a half integer we don't want. मान ले की Pco) istrue ni not x c) Let P(n)=n is not a half integer Est og Ntoke Pohedra hai we can make P(n++) = m++ EN a numbersyste ony way we Assumption: - There exists a set N following all 5 Peano Axioms, whose clements we will coll motivol numbers. Roman Both follow all 5 EO,I,I... 3 they just look different Hindu Arobic €0,I,I...} {0,1,2...} Addition of Natural Numbers Def 1 :- Adding OEN to any other MEN means : meons define

2) Assume m+n is known/defined intulively for ony (m++)+n = (m+m)++ & 0+m=m (getting there) (O++)+M=(O+M)++=M++=M+1 =M+2and so on Eg n+0 Prove n+0=n given def 1 p(n): m+0=m...ia) from def 1 0+n=m if n=0 0+0=0 then 506 or into /i out a 129 a true flow a Jan is 1 = 100 1 b) of n+0=n Using Axiom 5 Proove: (m++)+0=m++ Hence Proored (n+0)++ = n++ Ex:- Browe that m+n=n+m + n,m en (m+n)+l=m+(n+l)