## Questions & Answers 28 Sept.

Functional Programming 2017/18

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## Administrativia

#### Format of the exam

#### Similar to the previous exams in the web

- ► The exam is on paper
  - Some places (wrongly) state that it is digital
- ► Two types of questions
  - ▶ Open (80%): explain something or write some code
  - Multiple choice (20%): choose one answer
- ▶ There is a maximum amount of space per question
  - Only the things you write there count
  - Don't worry! There's way more space that you need!
- You cannot bring any notes to the exam
- You have to answer in English
  - You can bring a (mother tongue) English dictionary



#### Contents of the exam

#### Everything until today

- ► Basic types: lists, tuples, numbers
- User-defined data types
- Define functions by pattern matching
- Recursion on lists and other data types
- ► Define and use higher-order functions
- Write classes and instances
- ▶ Infer and check the type of an expression
- ▶ No: write functions using accumulators
- ▶ No: use functions to represent data

#### Contents of the exam

#### Do I need to know all the types by heart?

Writing and understanding type signatures is something you need to learn, and we need to test

- ➤ You have to know or deduce the type of simple functions such as (++), max, (==), and so forth
- ► Some higher-order functions are *very* important

In most cases you can deduce their type if you know what they do

#### Outcome of the exam

- You should expect your grades in about two weeks
- ▶ What happens if I fail the exam?
  - Nothing, your grade is the average with the final one
  - ▶ Remember,  $T = 0.3 \times \text{midterm} + 0.7 \times \text{final}$
  - ► *Reflect* on your mistakes and *act* to fix them

## **Q&A** session



## Interactive Q&A session

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- 1. I pose a question that somebody mailed me
- 2. Give you some time to think in groups
- 3. And then I explain the answer in full

## The most repeated question

More examples of type inference Let me answer some smaller questions before

#### In the previous lecture...

Monoids provide sane defaults:

```
lookup' = findWithDefault mempty
```

merge' = mergeWith mappend

What does "monoids provide sane defaults" mean?



#### Monoids provides defaults

- Whenever you have to:
  Combine elements of a type into one with the same type  $\Longrightarrow$  use mappend
  - ightharpoonup Have a default value for a type  $\implies$  use mempty

#### Monoids provides defaults

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#### Monoids provide *sane* defaults

- This is about how people normally use Monoid

  The Monoid instance for a class is only written when that type has a "natural" way to be combined
  - ► How to combine lists? Append them
  - ► How to combine Booleans? Conjunction or disjunction
  - In some cases you want to use this "natural" implementation in other places

Difference and/or relation between left- vs. right-bias and foldr vs. foldl

# Difference and/or relation between left- vs. right-bias and foldr vs. foldl

Not much, just "right" or "left" in their names

- ▶ foldr and foldl are about parenthesis and nesting
  - ightharpoonup foldr (+) 0 [1,2,3] = 1 + (2 + (3 + 0))
  - $\blacktriangleright$  fold1 (+) 0 [1,2,3] = ((0 + 1) + 2) + 3
- ▶ Bias is about choosing a value when there is a *conflict* 
  - E.g., when merging two values with the same key

What can we do with anonymous function / (lambda) abstractions? Is there something deep?

# What can we do with anonymous function / (lambda) abstractions? Is there something deep?

They are just a handier way to write (small) functions

```
g = map f ==> g = map (\x -> foo where f x = foo
```

They have a limitation: you cannot do case distinction

What is the difference between name@(...),  $\z \rightarrow ...$  and let x = ... in ...?

#### What is the difference between $name@(...), \z \rightarrow ...$ and let $x = \dots in \dots$ ?

In common: they introduce a new *name* into scope ▶ You can use that name in the . . . part

The difference lies in what they refer to let x = ... in ... gives a name to an expressionwhich is part of a bigger expression

```
unit (x, y) = let norm = sqrt(x*x + y*y)
               in (x/norm, y/norm)
```

- ▶ The others refer to the *argument* of a function
  - name@(...) always appear at the left of the = symbol

What is the difference between name@(...),  $z \rightarrow ...$  and let x = ... in ...?

With pattern matching we choose a branch in a function and access the components of a value

We can match also in an anonymous function!

▶ But we can only match *one* pattern

length  $(x:xs) = \dots$ 

```
norm (x,y) = \dots norm = \(x,y) \rightarrow \dots length [] = \dots length = \?? \rightarrow \dots
```

With name@(...) we give a name to the whole value and then we pattern match in its components

```
f lst0(x:xs) = ... -- 'lst' is the whole list -- 'x' is the head of 'lst' and 'xs' is its tail
```

## Enough waiting! We want to infer some types!

### What is the type of map . foldr?

```
General rule: if f :: A → B and e :: A, then f e :: B
Infix operator syntax comes to play here
map . foldr = (.) map foldr
```

▶ The function (.) takes two arguments, map and foldr

```
(.) :: (b -> c) -> (a -> b) -> a -> c

map :: (a -> b) -> [a] -> [b]

foldr :: (a -> b -> b) -> b -> [a] -> b
```

- 1. Introduce new names to disambiguate
  - ▶ I tend to use ?n to make it clear
  - Other people use Greek letters
  - ▶ I don't care, but make it clear in the exam

```
-- a, b and c in each type are unrelated

(.) :: (?b -> ?c) -> (?a -> ?b) -> ?a -> ?c

map :: (?d -> ?e) -> [?d] -> [?e]

foldr :: (?u -> ?v -> ?v) -> ?v -> [?u] -> ?v
```

- 1. Introduce new names to disambiguate
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map :: (?d -> ?e) -> [?d] -> [?e]

foldr :: (?u -> ?v -> ?v) -> ?v -> [?u] -> ?v
```

2. Write equations to fit the type in the function with the types of the arguments

#### 3. Solve the equations

Remember about the implicit parenthesis for ->

#### 4. Obtain the result type

▶ The remainder of the fn. without the given arguments

► Substitute unknowns for their values

This type works for any ?u and ?v

```
map . foldr :: (u -> v -> v) -> [v] -> [[u] -> v]
```

### How do I check that I am right?

Use the interpreter to ask for the type

The names a1 and a2 do not matter

But the *shape* of the type must be the same

## Rinse and repeat

What is the type of map (map map)?

The result of the inner map map is the arg. to the outer map

## Rinse and repeat

### What is the type of map (map map)?

The result of the inner map map is the arg. to the outer map

- 1. Introduce new names to disambiguate
  - ► Each map gets different names

- 2. Obtain the type of the inner map map
  - Pose and solve the equations

Obtain the result type

```
map map :: [?c] -> [?d]
= [?e -> ?f] -> [[?e] -> [?f]]
```

- 3. Obtain the type of the whole expression
  - ► Pose and solve the equations

Obtain the result type

```
map (map map) :: [?a] -> [?b]
= [[?e -> ?f]] -> [[[?e] -> [?f]]]
```

4. The type works for any ?e and ?f

```
map (map map)
:: [[a -> b]] -> [[[a] -> [b]]]
```