# Questions & Answers 27 Sept.

Functional Programming 2018/19

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## Administrativia

#### Format of the exam

### Similar to the previous exams in the web

- ► The exam is on paper
  - Some places (wrongly) state that it is digital
- Two types of questions
  - ▶ Open (85%): explain something or write some code
  - Multiple choice (15%): choose one answer
- ▶ There is a maximum amount of space per question
  - Only the things you write there count
  - Don't worry! There's way more space that you need!
- You cannot bring any notes to the exam
- You have to answer in English
  - You can bring a (mother tongue) English dictionary



#### Contents of the exam

#### Everything until today

- Basic types: lists, tuples, numbers
- User-defined data types
- Define functions by pattern matching
- Recursion on lists and other data types
- Define and use higher-order functions
- Write classes and instances
- Infer and check the type of an expression
- ▶ **No**: write functions using accumulators
- No: use functions to represent data



#### Contents of the exam

### Do I need to know all the types by heart?

Writing and understanding type signatures is something you need to learn, and we need to test

- You have to know or deduce the type of simple functions such as (++), max, (==), and so forth
- ► Some higher-order functions are *very* important

In most cases you can deduce their type if you know what they do



#### Outcome of the exam

- You should expect your grades in about two weeks
- What happens if I fail the exam?
  - Nothing, your grade is the average with the final one
  - Remember,  $T = 0.3 \times \text{midterm} + 0.7 \times \text{final}$
  - Reflect on your mistakes and act to fix them

# **Q&A** session

# The most repeated question

More examples of type inference

Let me answer some smaller questions before

Difference between (:) and (++)

#### Difference between (:) and (++)

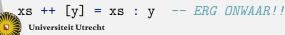
Let us look at the types:

- ▶ (:) puts an *element* in front of a *list*
- ▶ (++) puts a *list* in front of a *list*

Remember the following equivalence:

$$[x] ++ ys = x : ys$$

But the following is not even well-typed:



#### Difference between foldr and foldl



#### Difference between foldr and foldl

Not much, just "right" or "left" in their names

foldr and foldl are about parenthesis and nesting

```
\blacktriangleright foldr (+) 0 [1,2,3] = 1 + (2 + (3 + 0))
```

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\triangleright foldr (+) 0 [1,2,3] = 1 + (2 + (3 + 0))
```

$$\blacktriangleright$$
 fold1 (+) 0 [1,2,3] = ((0 + 1) + 2) + 3

Several people asked me about applyAll as a fold

- ▶ Unfortunately, we do not have the time :(
- ▶ I am available tomorrow from 8.30 to 16.30, at BBG-5.70
- ▶ I am **not** available on Monday

What can we do with anonymous function / (lambda) abstractions? Is there something deep?



# What can we do with anonymous function / (lambda) abstractions? Is there something deep?

They are just a handier way to write (small) functions

```
g = map f ==> g = map (\x -> foo)
where f x = foo
```

They have a limitation: you cannot do case distinction

We do **not** enforce a particular style about this



## When do we use \_ instead of a name?

- 1. We use it in patterns
  - ► At the left of = or ->
- 2. When we do not care about a value
  - When it is not used to the right of = or ->

What is the difference between  $name@(...), \z \rightarrow ...$  and let x = ... in ...?

```
What is the difference between name@(...), z \rightarrow ... and let x = ... in ...?
```

**In common**: they introduce a new *name* into scope

You can use that name in the . . . part

The difference lies in what they refer to

▶ let x = ... in ... gives a name to an expression which is part of a bigger expression

- ▶ The others refer to the *argument* of a function
  - name@(...) always appear at the left of the = symbol



```
What is the difference between name@(...), \z \rightarrow ... and let x = ... in ...?
```

With pattern matching we choose a branch in a function and access the components of a value

- We can match also in an anonymous function!
  - But we can only match one pattern

```
norm (x,y) = \dots norm = \(x,y) \rightarrow \dots
length [] = \dots length = \?? \rightarrow \dots
```

With name@(...) we give a name to the whole value and then we pattern match in its components

```
f lst@(x:xs) = ... -- 'lst' is the whole list

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```

## What is the difference between (.) and parentheses?



### What is the difference between (.) and parentheses?

- ▶ We use parentheses to delineat *values* 
  - Think about arguments and return values
- ▶ When we use (.) we think at the level of *functions* 
  - ▶ We never "touch" the values involved

We drop the xs because we are talking about functions



#### When can I "drop" arguments?

Rule 1: you can drop the last argument if it is also the last argument in the right-hand side

```
parseTable xs = map words xs
-- becomes
parseTable = map words
```

## When can I "drop" arguments?

Rule 1: you can drop the last argument if it is also the last argument in the right-hand side

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parseTable xs = map words xs
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Rule 2: you can drop the last argument if you can express the right-hand side as a composition of functions

```
f xs = map (x \rightarrow x * 2) (filter even xs)

-- becomes

f = map (*2) . filter even
```



#### When can I "drop" arguments?

In general, composition only works with one argument

- ► Rule 2 applies at most once
- ▶ You can use uncurry and put arguments in a tuple



#### When do I have variables in a data?

In other words, what is the difference between?

```
data Point1 = Pt1 Float Float
data Point2 a = Pt2 a a
```

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In other words, what is the difference between?

```
data Point1 = Pt1 Float Float
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```

- ▶ The second defines a *polymorphic* type
  - ▶ You can write Point2 Float, Point2 Int...
- Useful for "container" types
  - Lists, trees, Maybes

# Enough waiting! We want to infer some types!

What is the type of map . foldr?

```
General rule: if f :: A -> B and e :: A, then f e :: B
```

Infix operator syntax comes to play here

- ▶ map . foldr = (.) map foldr
- The function (.) takes two arguments, map and foldr

```
(.) :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow c
```



#### 1. Introduce new names to disambiguate

- ▶ I tend to use ?n to make it clear
- Other people use Greek letters
- ▶ I don't care, but make it clear in the exam

```
-- a, b and c in each type are unrelated
(.) :: (?b -> ?c) -> (?a -> ?b) -> ?a -> ?c
```

map :: (?d -> ?e) -> [?d] -> [?e]

foldr ::  $(?u \rightarrow ?v \rightarrow ?v) \rightarrow ?v \rightarrow [?u] \rightarrow ?v$ 

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```
-- a, b and c in each type are unrelated
(.) :: (?b \rightarrow ?c) \rightarrow (?a \rightarrow ?b) \rightarrow ?a \rightarrow ?c
map :: (?d -> ?e) -> [?d] -> [?e]
foldr :: (?u -> ?v -> ?v) -> ?v -> [?u] -> ?v
```

2. Write equations to fit the type in the function with the types of the arguments



#### 3. Solve the equations

Remember about the implicit parenthesis for ->



#### 4. Obtain the result type

▶ The remainder of the fn. without the given arguments

Substitute unknowns for their values

This type works for any ?u and ?v

map . foldr :: 
$$(u \rightarrow v \rightarrow v) \rightarrow [v] \rightarrow [[u] \rightarrow v]$$

## How do I check that I am right?

Use the interpreter to ask for the type

The names a1 and a2 do not matter

▶ But the *shape* of the type must be the same



# Rinse and repeat

What is the type of map (map map)?

The result of the inner map map is the arg. to the outer map

# Rinse and repeat

## What is the type of map (map map)?

The result of the inner map map is the arg. to the outer map

- 1. Introduce new names to disambiguate
  - Each map gets different names

- 2. Obtain the type of the inner map map
  - Pose and solve the equations

Obtain the result type

- 3. Obtain the type of the whole expression
  - Pose and solve the equations

Obtain the result type

4. The type works for any ?e and ?f

```
map (map map)
:: [[a -> b]] -> [[[a] -> [b]]]
```

