Deep Generative Language Models

DGM4NLP

Miguel Rios
University of Amsterdam

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Outline

1. Language Modelling
2. Variational Auto-encoder for Sentences

Recap Generative Models of Word Representation

Discriminative embedding models
word2vec

In the event of a chemical spill, most children know they should **evacuate** *as advised by people in charge.*

Place words in $\mathbb{R}^d$ as to answer questions like

"Have I seen this word in this context?"

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Place words in $\mathbb{R}^d$ as to answer questions like

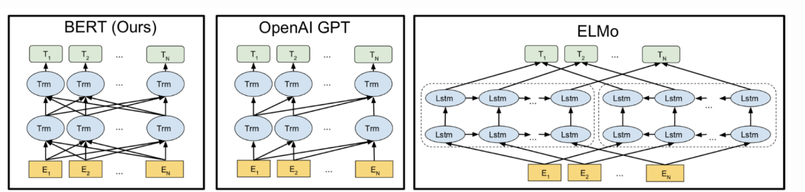
"Have I seen this word in this context?"

Fit a binary classifier

- positive examples
- negative examples

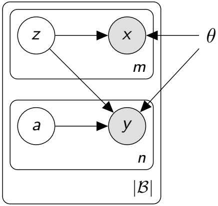
Recap Generative Models of Word Representation

- The models processes a sentence and outputs a word representation:



Recap Generative Models of Word Representation

quickly evacuate the area / deje el lugar rápidamente



$\boxed{X}$

$\boxed{Z}$

$\boxed{A}$

$\boxed{Z_a}$

$\boxed{Y}$

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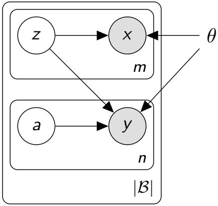

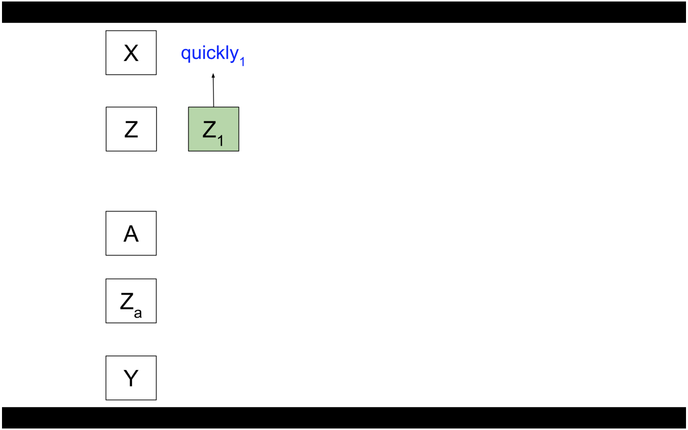

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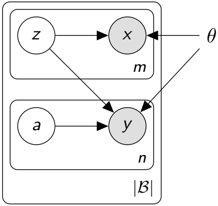

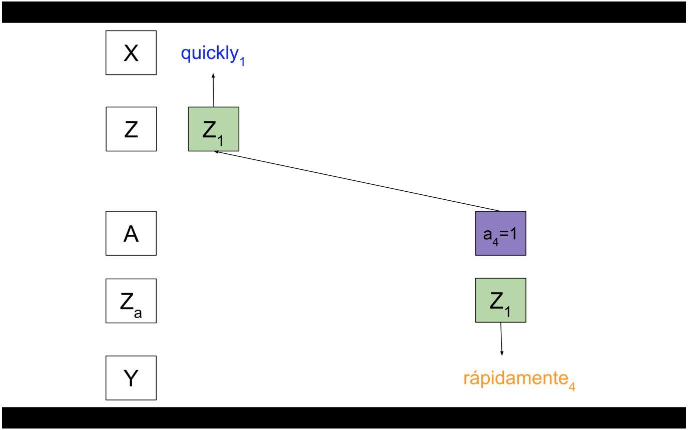

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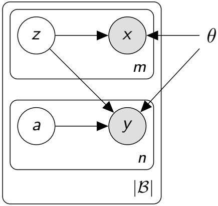

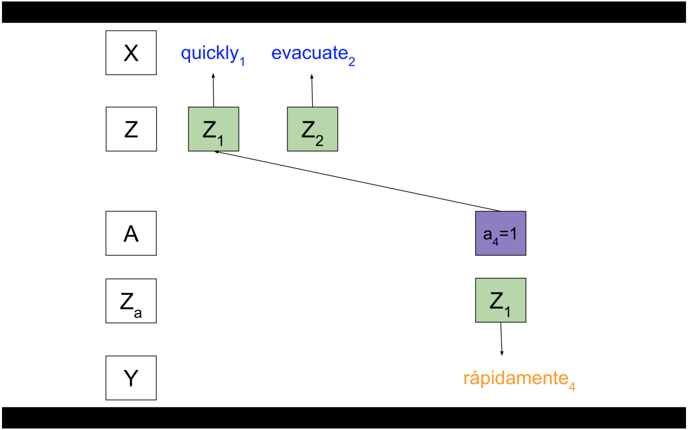

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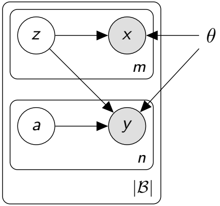

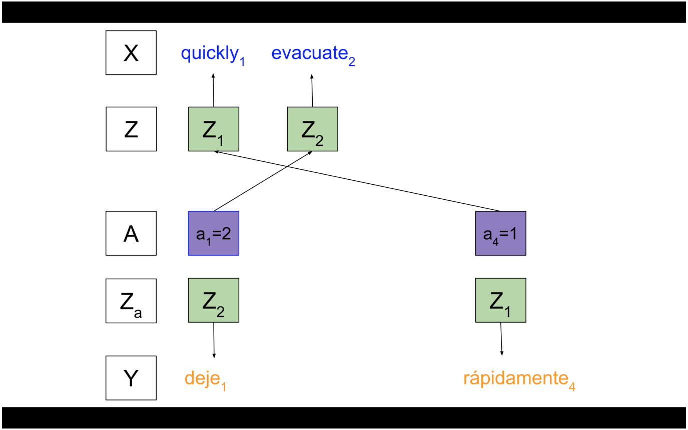

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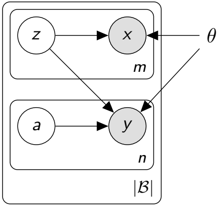

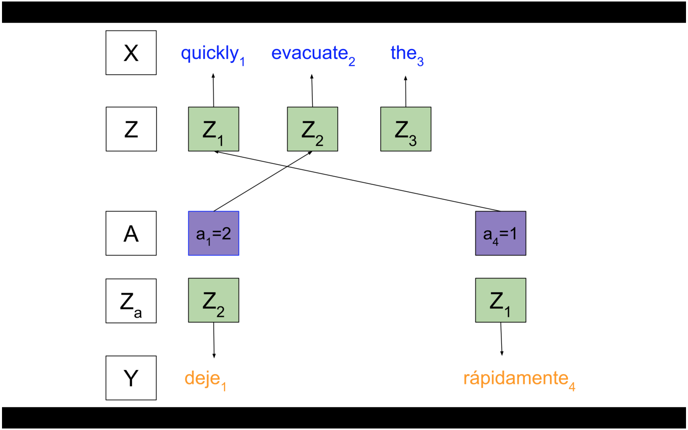

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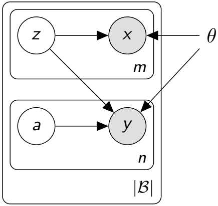

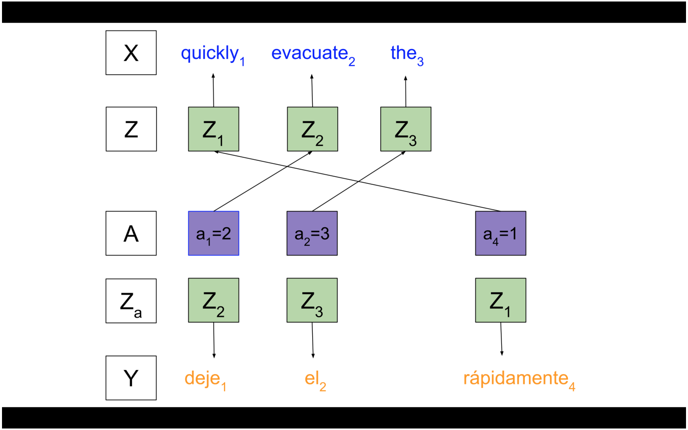

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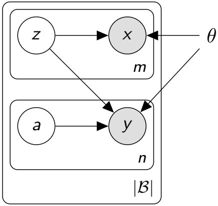

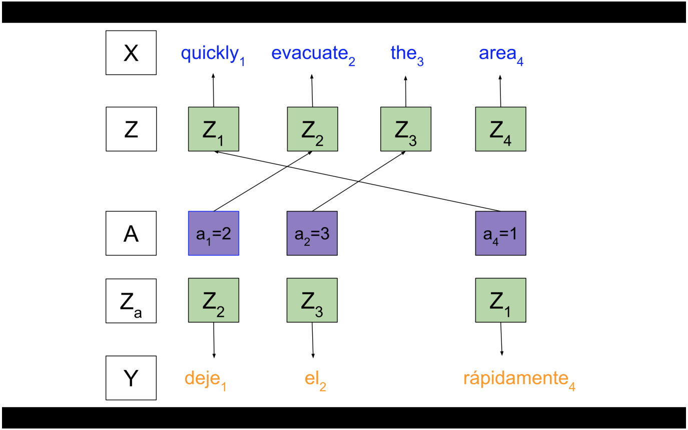

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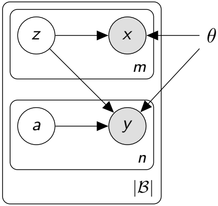

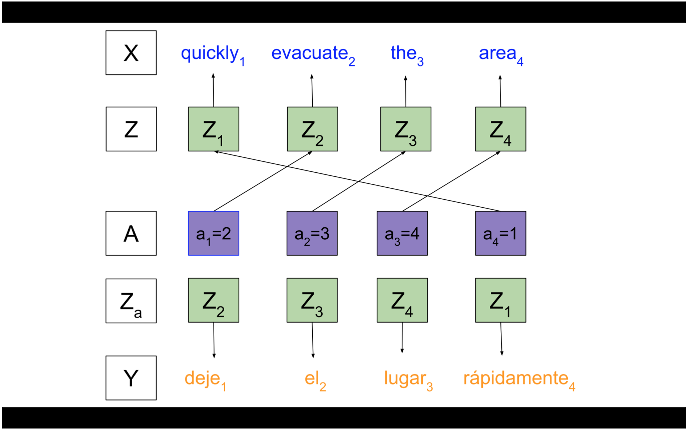

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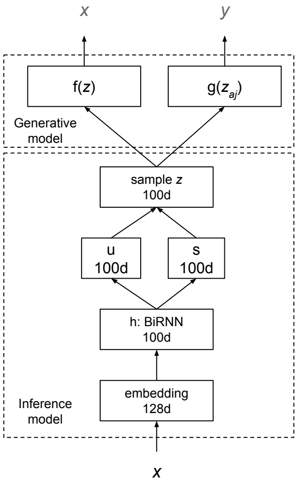

Introduction

- you know nothing, jon x

Introduction

- you know nothing, jon x
- ground control to major x

Introduction

- you know nothing, jon x
- ground control to major x
- the x

Introduction

- the quick brown x

Introduction

- the quick brown x
- the quick brown fox x

Introduction

- the quick brown x
- the quick brown fox x
- the quick brown fox jumps x

Introduction

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- the quick brown fox jumps over x

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Introduction

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- the quick brown fox jumps over the lazy dog

Definition

- Language models give us the probability of a sentence;

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- At a time step, they assign a probability to the next word.

Applications

- Very useful on different tasks:

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Applications

- Very useful on different tasks:
- Speech recognition;
- Spelling correction;
- Machine translation;
- LMs are useful in almost any tasks that deals with generating language.

Language Models

- N-gram based LMs;

Language Models

- N-gram based LMs;
- Log-linear LMs;

Language Models

- N-gram based LMs;
- Log-linear LMs;
- Neural LMs.

N-gram LM

- x is a sequence of words

N-gram LM

- x is a sequence of words
- $x = x_1, x_2, x_3, x_4, x_5$
  $=$ you, know, nothing, jon, snow

N-gram LM

- To compute the probability of a sentence

$$p(x) = p\left(x_1, x_2, \ldots, x_n\right) \tag{1}$$

[Jelinek and Mercer, 1980, Goodman, 2001]

N-gram LM

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$$p(x) = p\left(x_1, x_2, \ldots, x_n\right) \tag{1}$$

- We apply the chain rule:

$$p(x) = \prod_i p\left(x_i | x_1, \ldots, x_{i-1}\right) \tag{2}$$

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- We limit the history with a Markov order:
  $p(x_i | x_1, \ldots, x_{i-1}) \simeq p(x_i | x_{i-4}, x_{i-3}, x_{i-2}, x_{i-1})$

[Jelinek and Mercer, 1980, Goodman, 2001]

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$$\begin{aligned} P(x) =& P(\text{"you know nothing jon snow"}) \\ =& P(\text{"you"}) \cdot \\ & P(\text{"know"} \mid \text{"you"}) \cdot \\ & P(\text{"nothing"} \mid \text{"you know"}) \cdot \\ & P(\text{"jon"} \mid \text{"you know nothing"}) \cdot \\ & P(\text{"snow"} \mid \text{"you know nothing jon"}). \end{aligned}$$

N-gram LM

- We make a Markov assumption of conditional independence:

$$p\left(x_i \middle| x_1, \ldots, x_{i-1}\right) \simeq p\left(x_i \middle| x_{i-1}\right) \tag{4}$$

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- Laplace smoothing:

$$p_{\mathrm{add1}}\left(x_i | x_{i-1}\right) = \frac{\text{count}\left(x_{i-1}, x_i\right) + 1}{\text{count}\left(x_{i-1}\right) + V} \tag{6}$$

Log-linear LM

- $$p(y|x) = \frac{\exp \boldsymbol{w} \cdot \phi(x, y)}{\sum_{y' \in V_y} \exp w \cdot \phi\left(x, y'\right)} \tag{7}$$

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- w are the model parameters.

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- gappy n-gram features $x_{j-2} =$ the and $x_j =$ puppy.
- class features: x_j belongs to class ABC;
- gazetteer features: x_j is a place name;

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- With n-grams, there is no sharing at all
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- We can add arbitrary features
- We use Stochastic Gradient Descent (SGD)

Neural LM

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- log-linear models allow us to share weights through features
- maybe our history is still too limited, e.g. n-1 words
- we need to find useful features

Feed-forward NLM

- With NN we can exploit distributed representations to allow for statistical weight sharing.

[Bengio et al., 2003]

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- How does it work:
    1. each word is mapped to an embedding: an m-dimensional feature vector;
    2. a probability function over word sequences is expressed in terms of these vectors;
    3. we jointly learn the feature vectors and the parameters of the probability function.

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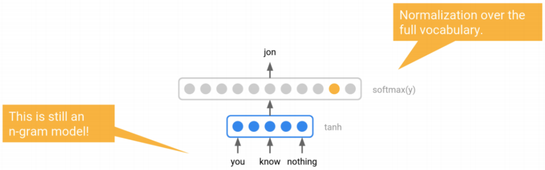
- With this, probability mass is naturally transferred from (1) to (2):
- The cat is walking in the bedroom.
- The dog is running in the room.
- Take-away message:
  The presence of only one sentence in the training data will increase the probability of a combinatorial number of neighbours in sentence space.

Feed-forward NLM

- FF-LM



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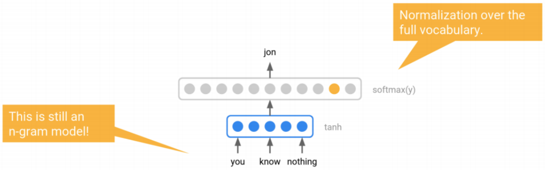

- $\boldsymbol{E}_{\text{you}}, \boldsymbol{E}_{\text{know}}, \boldsymbol{E}_{\text{nothing}} \in \mathbb{R}^{100}$

$$\begin{aligned} \boldsymbol{x} &= [\boldsymbol{E}_{\text{you}}; \boldsymbol{E}_{\text{know}}; \boldsymbol{E}_{\text{nothing}}] \in \mathbb{R}^{300} \\ \boldsymbol{y} &= \boldsymbol{W}_3 \tanh(\boldsymbol{W}_1 \boldsymbol{x} + \boldsymbol{b}_1) + \boldsymbol{W}_2 \boldsymbol{x} + \boldsymbol{b}_2 \end{aligned} \tag{8}$$

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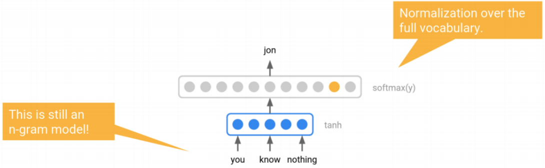

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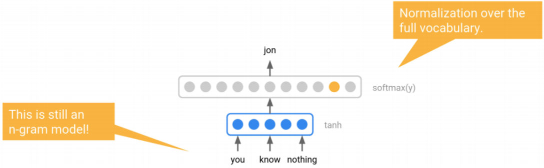

- The non-linear activation functions perform feature combinations that a linear model cannot do;

Feed-forward NLM

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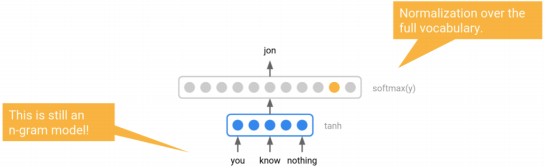

- The non-linear activation functions perform feature combinations that a linear model cannot do;
- End-to-end training on next word prediction.

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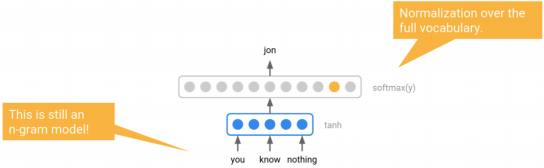

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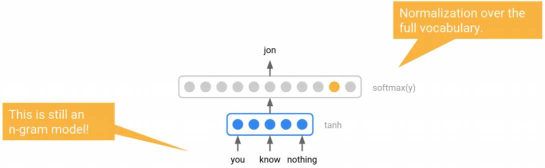

- We now have much better generalisation, but still a limited history/context.

Feed-forward NLM

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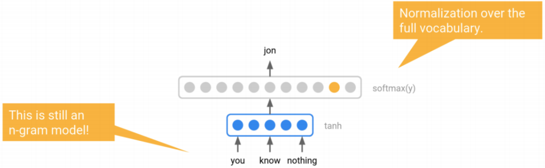

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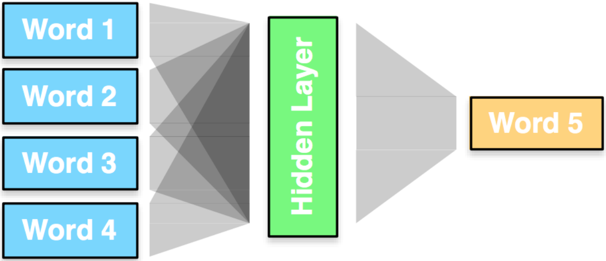

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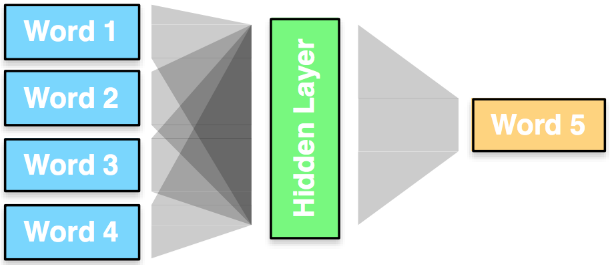

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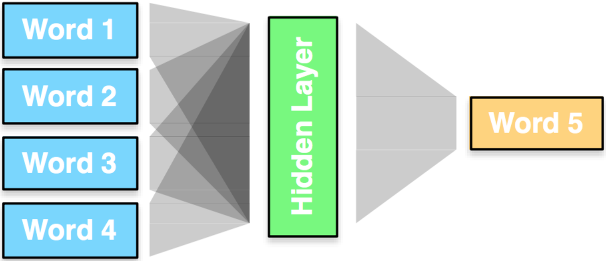

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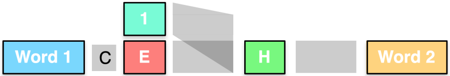
RNN NLM

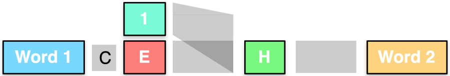
- RNN-LM



[Mikolov et al., 2010]

RNN NLM

- RNN-LM



- Start: predict second word from first

[Mikolov et al., 2010]

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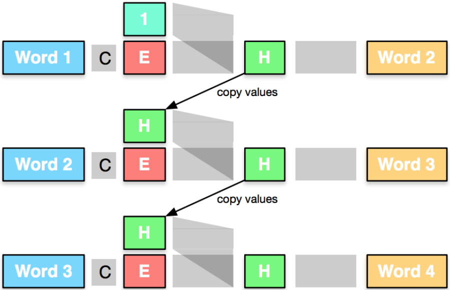

1
Word 1
C
E
H
Word 2
copy values
H
Word 2
C
E
H
Word 3
copy values
H
Word 3
C
E
H
Word 4

Outline

Sen VAE

- Model observations as draws from the marginal of a DGM.

[Bowman et al., 2015]

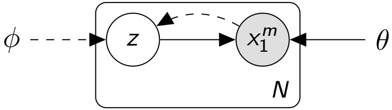
Sen VAE

- Model observations as draws from the marginal of a DGM.
- An NN maps from a latent sentence embedding $z \in R^{dz}$ to a distribution $p(x|z, \theta)$ over sentences,

$$\begin{aligned} p(x|\theta) &= \int p(z)p(x|z,\theta)\mathrm{d}z \\ &= \int \mathcal{N}(z|0,I) \prod_{i=1}^{|x|} \text{Cat}\left(x_i|f\left(z, x_{<i};\theta\right)\right) \mathrm{d}z \end{aligned} \tag{9}$$

[Bowman et al., 2015]

Sen VAE



Generative model

- $Z \sim \mathcal{N}(0, I)$
- $X_i | z, x_{<i} \sim \mathrm{Cat}(f_\theta(z, x_{<i}))$

Inference model

- $Z \sim \mathcal{N}(\mu_\phi(x_1^m), \sigma_\phi(x_1^m)^2)$

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- $p(x|\theta)$ is the marginal likelihood.
- We train the model to assign high (marginal) probability to observations like a LMs.
- However the model uses a latent space to exploit neighbourhood and smoothness in latent space to capture regularities in data space.
  For example, it may group sentences according to certain e.g. lexical choices, syntactic complexity, lexical semantics, etc...

Approximate Inference

- The model has a diagonal Gaussian distribution as variational posterior:
$q_\phi(z|x) = \mathcal{N}\left(z|\mu_\phi(x), \operatorname{diag}\left(\sigma_\phi(x)\right)\right)$

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- With reparametrisation:
  $z = h_\phi(\epsilon, x) = \mu_\phi(x) + \sigma_\phi(x) \odot \epsilon, \qquad \text{where } \epsilon \sim \mathcal{N}\left(0, \mathbf{I}\right) f$

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- Analytical KL:
  $\mathrm{KL}\left[q_\phi(z|x) \| p_\theta(z)\right] =$
  $\frac{1}{2} \sum_{d=1}^{\mathrm{D}_z} \left(-\log \sigma_\phi^2(x) - 1 + \sigma_\phi^2(x) + \mu_\phi^2(x)\right)$

Approximate Inference

- We jointly estimate the parameters of both generative and inference by maximising a lowerbound on the log-likelihood function (ELBO):

$$\mathcal{L}(\theta, \phi|x) = \mathbb{E}_{q(z|x,\phi)}[\log p(x|z, \theta)]. \\ - \mathrm{KL}(q(z|x, \phi)|p(z)) \tag{10}$$

Architecture

- Gaussian Sen VAE parametrises a categorical distribution over the vocabulary for each given prefix, and, it conditions on a latent embedding:
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f\left(z, x_{<i}; \theta\right) &= \operatorname{softmax}\left(\mathbf{s}_i\right) \\
\mathbf{e}_i &= \operatorname{emb}\left(x_i; \theta_{\text{emb}}\right) \\
\mathbf{h}_0 &= \tanh\left(\operatorname{affine}\left(z; \theta_{\text{ init }}\right)\right) \\
\mathbf{h}_i &= \operatorname{GRU}\left(\mathbf{h}_{i-1}, \mathbf{e}_{i-1}; \theta_{\text{gru}}\right) \\
\mathbf{s}_i &= \operatorname{affine}\left(\mathbf{h}_i; \theta_{\text{out}}\right)
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- The model might achieve a high ELBO without using information from z
- RNN LM is strong decoder because they condition on all previous context when generating a word

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- Word Dropout, by dropping a percentage of the input at random, the decoder has to rely on the latent variable to fill in the missing gaps.
- Freebits because it allows encoding the first r nats of information for free.
  $\max(r, \mathrm{KL}(q_\phi(z|x) \| p(z)))$

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\approx \frac{1}{S}\sum_{s=1}^{S} \frac{p\left(z^{(s)},x|\theta\right)}{q\left(z^{(s)}|x\right)} \text{ where } z^{(s)} \sim q(z|x)
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- Perplexity PPL: the exponent of average per-word entropy, given N i.i.d. sequences

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- perplexity is based on the importance sampled NLL

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- At each step, an RNNLM parameterises a categorical distribution over the vocabulary, i.e. $X_i | x_{<i} \sim \mathrm{Cat}\left(f\left(x_{<i}; \theta\right)\right)$ and

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- Embedding layer (emb), one (or more) GRU cell(s) ($h_0 \in \theta$ is a parameter of the model), and an affine layer to map from the dimensionality of the GRU to the vocabulary size.

Data

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- Section 24 as validation

Results

	NLL↓	PPL↓
RNN-LM	118.7±0.12	107.1±0.46
VAE	118.4±0.09	105.7±0.36
Annealing	117.9±0.08	103.7±0.31
Free-bits	117.5±0.18	101.9±0.77

Samples

- decode greedily from a prior sampl and the variability is due to the generator's reliance on the latent sample.

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- The VAE ignores z and greedy generation from a prior sample is essentially deterministic in that case

Sample	Closest training instance
For example, the Dow Jones Industrial Average fell almost 80 points to close at 2643.65.	*By futures-related program buying, the Dow Jones Industrial Average gained 4.92 points to close at 2643.65.*
The department store concern said it expects to report profit from continuing operations in 1990.	*Rolls-Royce Motor Cars Inc. said it expects its U.S. sales to remain steady at about 1,200 cars in 1990.*
The new U.S. auto makers say the accord would require banks to focus on their core businesses of their own account.	*International Minerals said the sale will allow Mallinckrodt to focus its resources on its core businesses of medical products, specialty chemicals and flavors.*

Samples

- Homotopy, decode greedily from points lying between a posterior sample conditioned on the first sentence and a posterior sample conditioned on the last sentence.

The inquiry soon focused on the judge.
The judge declined to comment on the floor.
The judge was dismissed as part of the settlement.
The judge was sentenced to death in prison.
The announcement was filed against the SEC.
The offer was misstated in late September.
The offer was filed against bankruptcy court in New York.
The letter was dated Oct. 6.

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